

# LECTURE 4

# Induced Emf in a synchronous machine

- $E(\text{average}) = PZN\phi / 60A$
- $E(\text{rms}) / E(\text{average}) = 1.11$
- $E(\text{rms}) = 2.22P\phi NT / 60$  ( $Z = 2T$ )
- $N = 120f / P$
- $2f = PN / 60$
- $E = 2.22\phi T * 2f$
- $E = 4.44\phi fT$

## Generated Voltage(OCC)

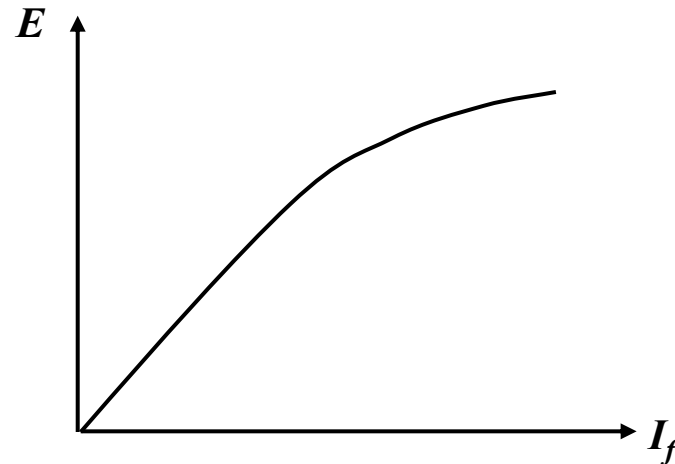
The generated voltage of a synchronous generator is given by

$$E = K_c \phi f_e$$

where  $\phi$  = flux in the machine (function of  $I_f$ )

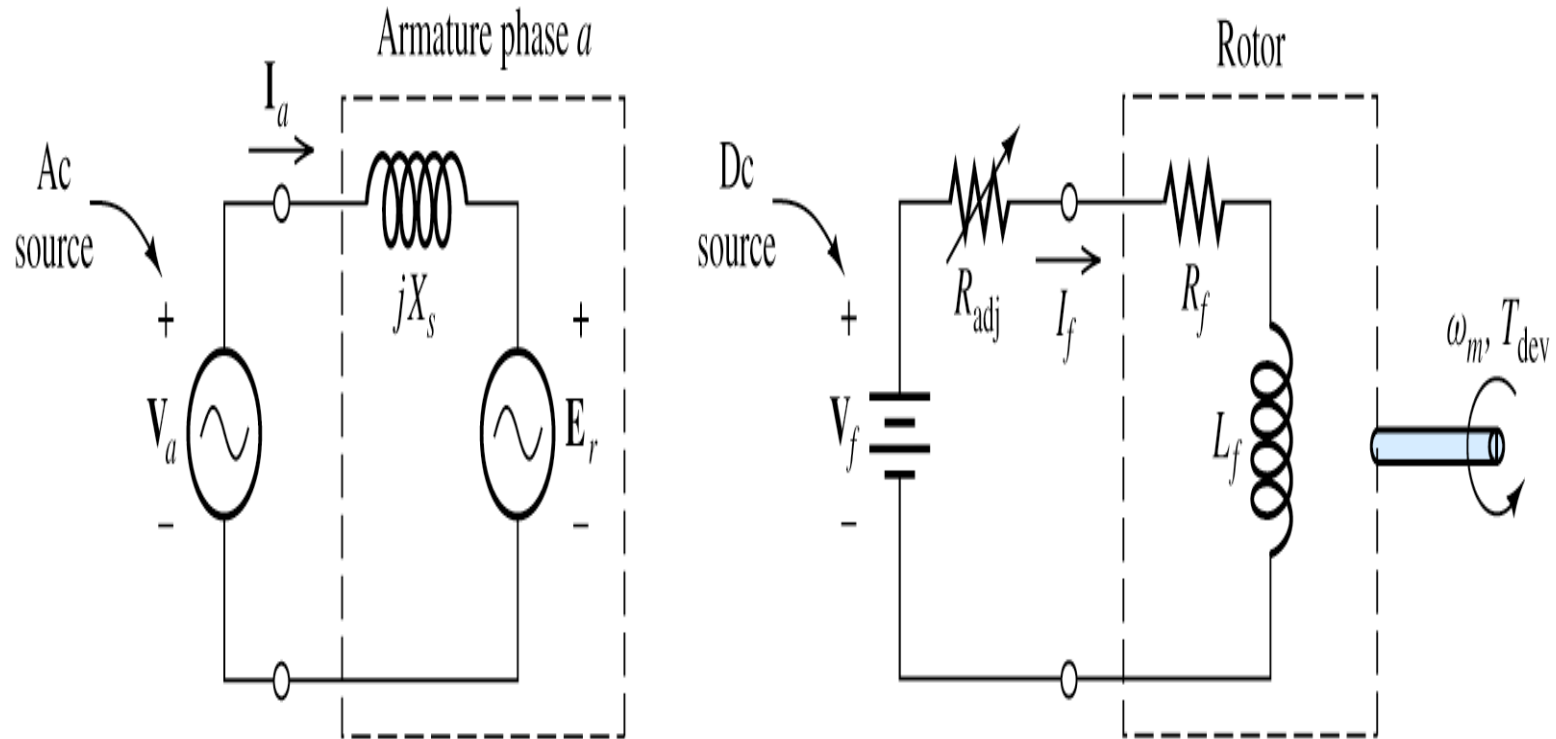
$f_e$  = electrical frequency

$K_c$  = synchronous machine constant



**Saturation characteristic of a synchronous generator.**

# Synchronous Machine Equivalent Circuit



**Figure 17.18** Equivalent circuit for the synchronous motor. The armature circuit is based on Equation 17.42.

# Synchronous Reactance

- Equivalent circuit of a synchronous generator:  
Each phase has resistance  $R$  and inductance  $L$   
Synchronous reactance:  
 $X_s = 2\pi fL$   
 $R$  is typically  $\ll X_s$ , therefore neglected unless interested in efficiency or heating effects

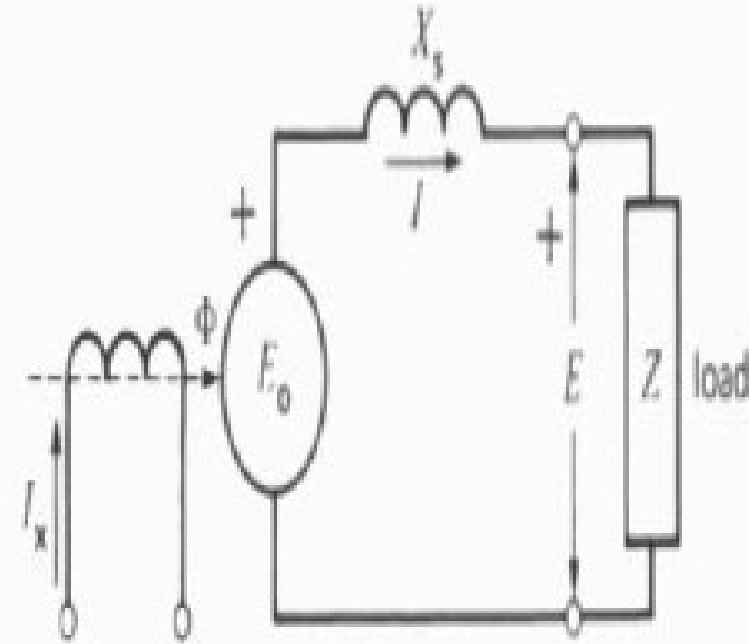


Figure 16.17

Equivalent circuit of a 3-phase generator, showing only one phase.

## Voltage Regulation

A convenient way to compare the voltage behaviour of two generators is by their *voltage regulation* ( $VR$ ). The  $VR$  of a synchronous generator at a given load, power factor, and at rated speed is defined as

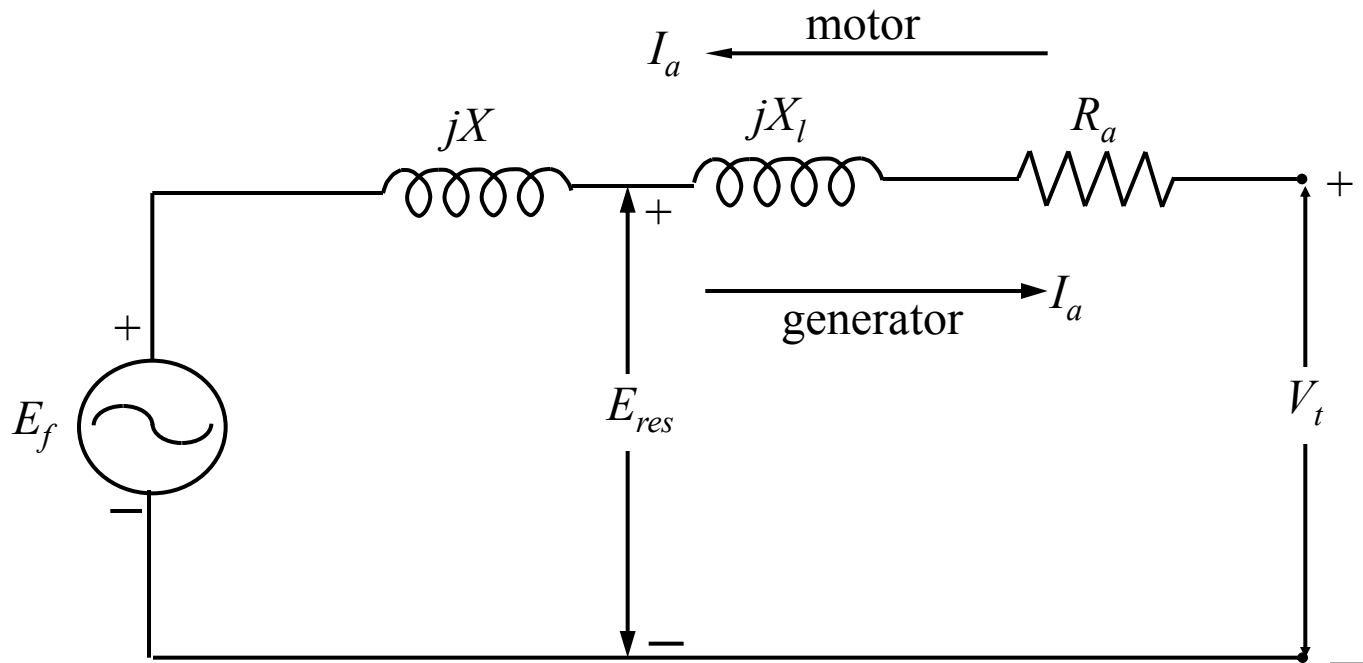
$$VR = \frac{E_{nl} - V_{fl}}{V_{fl}} \times 100\%$$

Where  $V_{fl}$  is the full-load terminal voltage, and  $E_{nl}$  (equal to  $E_f$ ) is the no-load terminal voltage (internal voltage) at rated speed when the load is removed without changing the field current. For lagging power factor ( $PF$ ),  $VR$  is fairly positive, for unity  $PF$ ,  $VR$  is small positive and for leading  $PF$ ,  $VR$  is negative.

# Equivalent Circuit 1

- o The internal voltage  $E_f$  produced in a machine is not usually the voltage that appears at the terminals of the generator.
- o The only time  $E_f$  is same as the output voltage of a phase is when there is no armature current flowing in the machine.
- o There are a number of factors that cause the difference between  $E_f$  and  $V_t$ :
  - The distortion of the air-gap magnetic field by the current flowing in the stator, called the armature reaction
  - The self-inductance of the armature coils.
  - The resistance of the armature coils.
  - The effect of salient-pole rotor shapes.

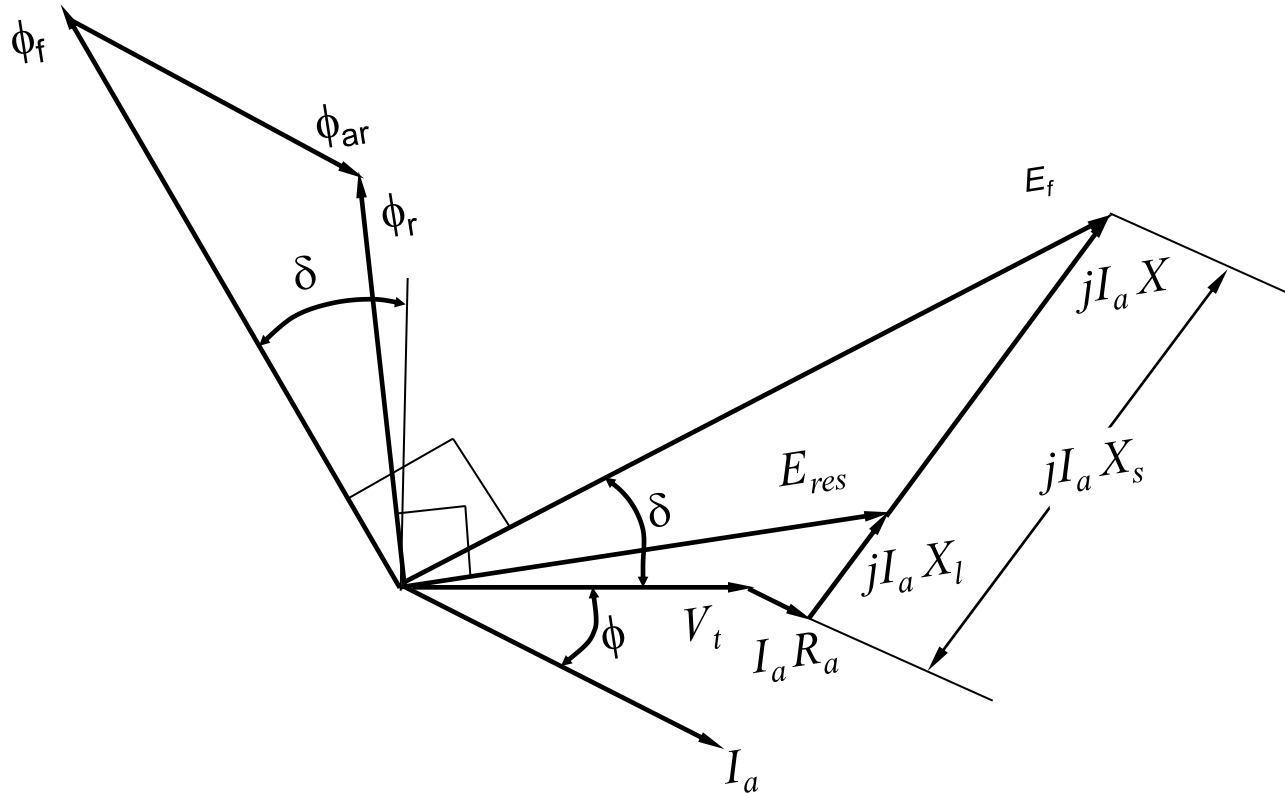
## Equivalent Circuit 2



Equivalent circuit of a cylindrical-rotor synchronous machine



# Phasor Diagram



Phasor diagram of a cylindrical-rotor synchronous generator, for the case of lagging power factor

Lagging PF:  $|V_t| < |E_f|$  for overexcited condition

Leading PF:  $|V_t| > |E_f|$  for underexcited condition

# Three-phase equivalent circuit of a cylindrical-rotor synchronous machine

The voltages and currents of the three phases are  $120^\circ$  apart in angle, but otherwise the three phases are identical.

