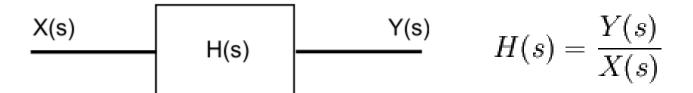
# Chapter:2

Mathematical Modelling

- Transfer Function reveals how the circuit modifies the input amplitude in creating output amplitude.
- Therefore, transfer function describes how the circuit processes the input to produce output.



Transfer Function is the ratio of the output of a system to the input of a system, in the Laplace domain considering its initial conditions to be zero.

## **Frequency Domain**

$$v_R(t) = Ri(t)$$
  $V_R(s) = RI(s)$ 
 $v_L(t) = L\frac{di}{dt}$   $V_L(s) = sLI(s)$ 
 $v_C(t) = \frac{1}{C}\int idt$   $V_C(s) = \frac{1}{sC}I(s)$ 

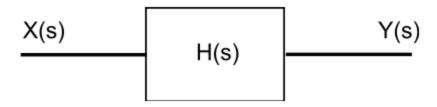
#### **Time constants:**

$$T_{RC} = RC = \frac{V}{A} \frac{Q}{V} = \frac{VQ}{\frac{Q}{\sec V}} = \sec$$

$$T_{RL} = \frac{L}{R} = \frac{\frac{V}{A}}{\frac{V}{A}} = \sec$$

## **Frequency Domain**

Transfer Function is the ratio of the output of a system to the input of a system, in the Laplace domain considering its initial conditions to be zero.



$$H(s) = \frac{Y(s)}{X(s)}$$

## **Frequency Domain**

$$V(s) = RI(s)$$
  $V = RI$ 

$$V = RI$$

$$V(s) = sLI(s)$$
  $V = sLI$ 

$$V = sLI$$

$$V(s) = \frac{1}{sC}I(s)$$
  $V = \frac{1}{sC}I$ 

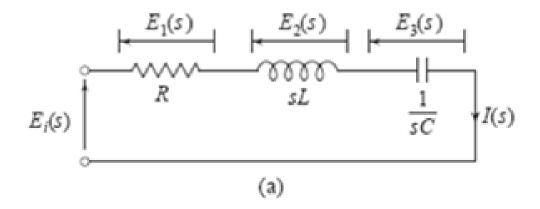
$$V = \frac{1}{sC}I$$

$$\frac{V(s)}{I(s)} = R$$

$$\frac{V(s)}{I(s)} = sL$$

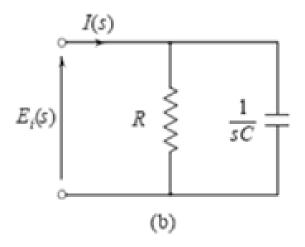
$$\frac{V(s)}{I(s)} = \frac{1}{sC}$$

## Impedances in series



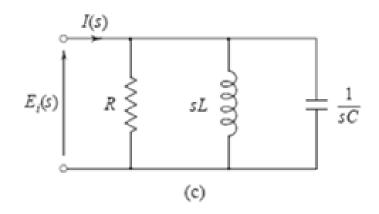
$$Z(s)_{eq} = \frac{Ei(s)}{I(s)} = R + \frac{1}{sC} + Ls$$

## Impedances in parallel



$$Z(s)_{eq} = \frac{Ei(s)}{I(s)} = \frac{R}{C(R + \frac{1}{Cs})s}$$

## Impedance Approach



$$\frac{1}{Z(s)_{eq}} = Y(s)_{eq} = \frac{I(s)}{Ei(s)} = \frac{1}{R} + Cs + \frac{1}{Ls}$$
 or

$$Z(s)_{eq} = \frac{Ei(s)}{I(s)} = \frac{LR}{C(R + \frac{1}{Cs}) \left(\frac{R}{C(R + \frac{1}{Cs})s} + Ls\right)}$$

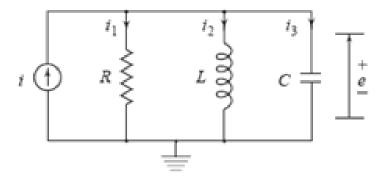
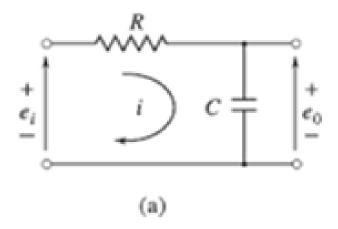
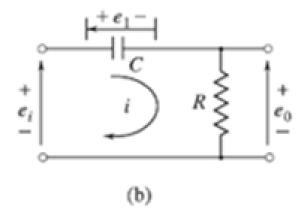


Fig. 2.28 An RLC circuit

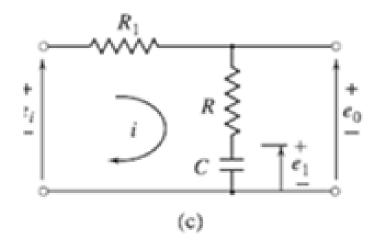
$$H(s) = \frac{\frac{L}{C(\frac{1}{Cs} + Ls)}}{R + \frac{L}{C(\frac{1}{Cs} + Ls)}}$$



$$H(s) = \frac{1}{C(R + \frac{1}{Cs}) s}$$



$$H(s) = \frac{R}{R + \frac{1}{Cs}}$$



$$H(s) = \frac{R + \frac{1}{Cs}}{R + R1 + \frac{1}{Cs}}$$

 Define transfer function. derive transfer function of an armature controlled D. C motor