

DEPARTMENT OF MECHANICAL ENGINEERING  
KINEMATICS OF MACHINES  
QUESTION BANK  
SEMESTER:- IV

- 1 What is a machine ? Giving example, differentiate between a machine and a structure.
- 2 Explain and Give the classification of the terms kinematic link, Pairs, Chain and Mechanisms
- 3 Explain with neat sketches the different types of Constrained motions.
- 4 What is the significance of degrees of freedom of a kinematic chain when it functions as a mechanism? Give examples.
- 5 Explain Grubler's criterion for plane mechanisms.
- 6 Explain Kutzbach's criterion for plane mechanisms.
- 7 *In a crank and slotted lever quick return motion mechanism, the distance between the fixed centres is 240 mm and the length of the driving crank is 120 mm. Find the inclination of the slotted bar with the vertical in the extreme position and the time ratio of cutting stroke to the return stroke. If the length of the slotted bar is 450 mm, find the length of the stroke if the line of stroke passes through the extreme positions of the free end of the lever.*
- 8 Sketch a pantograph, explain its working and show that it can be used to reproduce to an enlarged scale a given figure.
- 9 What are straight line mechanisms ? Describe all types of exact straight line motion Mechanism with the help of a sketch
- 10 What is the condition for correct steering ? Sketch and show the two main types of steering Gears and discuss their relative advantages.
- 11 What do you understand by the instantaneous centre of rotation (centro) in kinematics of machines? Answer briefly.
- 12 *In a pin jointed four bar mechanism, as shown in Fig.  $AB = 300$  mm,  $BC = CD = 360$  mm, and  $AD = 600$  mm. The angle  $BAD = 60^\circ$ . The crank  $AB$  rotates uniformly at 100 r.p.m. Locate all the instantaneous centres and find the angular velocity of the link  $BC$*
- 13 *Locate all the instantaneous centres of the slider crank mechanism as shown in Fig. The lengths of crank  $OB$  and connecting rod  $AB$  are 100 mm and 400 mm respectively. If the crank rotates clockwise with an angular velocity of 10 rad/s, find: **1.** Velocity of the slider  $A$ , and **2.** Angular velocity of the connecting rod  $AB$ .*
- 14 *In a four bar chain  $ABCD$ ,  $AD$  is fixed and is 150 mm long. The crank  $AB$  is 40 mm long and rotates at 120 r.p.m. clockwise, while the link  $CD = 80$  mm oscillates about  $D$ .  $BC$  and  $AD$  are of equal length. Find the angular velocity of link  $CD$  when angle  $BAD = 60^\circ$ .*

15 The crank of a slider crank mechanism rotates clockwise at a constant speed of 300 r.p.m. The crank is 150 mm and the connecting rod is 600 mm long. Determine : **1.** Linear velocity and acceleration of the midpoint of the connecting rod, and **2.** angular velocity and angular acceleration of the connecting rod, at a crank angle of  $45^\circ$  from inner deadcentre position.

16 Explain and Give the classification with examples of Toothed Gears.

17 State and prove the law of gearing. Show that involute profile satisfies the conditions for Correct gearing.

18 What do you understand by the term 'interference' as applied to gears? Derive an expression for the minimum number of teeth required on the pinion in order to avoid interference in involute gear teeth when it meshes with wheel.

19 What do you understand by the term 'interference' as applied to gears? Derive an expression for minimum number of teeth required on a pinion to avoid interference when it gears with a rack

20 Derive an expression for the length of the Path of contact, length of the arc of contact and contact Ratio in a pair of meshed spur gears.

21 Derive an expression for the maximum length of the Path of contact, length of the arc of contact and contact Ratio in a pair of meshed spur gears in order to avoid interference.

22 What do you understand by the term 'interference' as applied to gears? Derive an expression for the minimum number of teeth required on the gear in order to avoid interference in involute gear teeth when it meshes with pinion.

23 A pinion of 20 involute teeth and 125 mm pitch circle diameter drives a rack. The addendum of both pinion and rack is 6.25 mm. What is the least pressure angle which can be used to avoid interference? With this pressure angle, find the length of the arc of contact and the minimum number of teeth in contact at a time.

24 Two gear wheels mesh externally and are to give a velocity ratio of 3 to 1. The teeth are of involute form; module = 6 mm, addendum = one module, pressure angle =  $20^\circ$ . The pinion rotates at 90 r.p.m. Determine : **1.** The number of teeth on the pinion to avoid interference on it and the corresponding number of teeth on the wheel, **2.** The length of path and arc of contact, **3.** The number of pairs of teeth in contact, and **4.** The maximum velocity of sliding.

25 A pair of  $20^\circ$  full depth involute spur gears having 30 and 50 teeth respectively of module 4 mm are in mesh. The smaller gear rotates at 1000 r.p.m. Determine : **1.** Sliding velocities at engagement and at disengagement of pair of a teeth, and **2.** contact ratio.

26 A pair of involute spur gears with  $16^\circ$  pressure angle and pitch of module 6 mm is in mesh. The number of teeth on pinion is 16 and its rotational speed is 240 r.p.m. When the gear ratio is 1.75, find in order that the interference is just avoided

; **1.** the addenda on pinion and gear wheel ; **2.** the length of path of contact ; and **3.** the maximum velocity of sliding of teeth on either side of the pitch point.

27 Two mating gears have 20 and 40 involute teeth of module 10 mm and  $20^\circ$  pressure angle. The addendum on each wheel is to be made of such a length that the line of contact on each side of the pitch point has half the maximum possible length. Determine the addendum height for each gear wheel, length of the path of contact, arc of contact and contact ratio.

28 The following data relate to a pair of  $20^\circ$  involute gears in mesh :

Module = 6 mm, Number of teeth on pinion = 17, Number of teeth on gear = 49 ; Addenda on pinion and gear wheel = 1 module.

Find : **1.** The number of pairs of teeth in contact ; **2.** The angle turned through by the pinion and the gear wheel when one pair of teeth is in contact, and **3.** The ratio of sliding to rolling motion when the tip of a tooth on the larger wheel (i) is just making contact, (ii) is just leaving contact with its mating tooth, and (iii) is at the pitch point.

29 A pair of gears, having 40 and 20 teeth respectively, are rotating in mesh, the speed of the smaller being 2000 r.p.m. Determine the velocity of sliding between the gear teeth faces at the point of engagement, at the pitch point, and at the point of disengagement if the smaller gear is the driver. Assume that the gear teeth are  $20^\circ$  involute form, addendum length is 5 mm and the module is 5 mm. Also find the angle through which the pinion turns while any pairs of teeth are in contact.

30 What do you understand by 'gear train'? Discuss the various types of gear trains.

31 Explain briefly the differences between simple, compound, and epicyclic gear trains. What

are the special advantages of epicyclic gear trains ?

32 How the velocity ratio of epicyclic gear train is obtained by tabular method?

33 Explain with a neat sketch the 'sun and planet wheel'.

34 What are the various types of the torques in an epicyclic gear train ?

35 An epicyclic gear consists of three gears A, B and C as shown in Fig. The gear A has 72 internal teeth and gear C has 32 external teeth. The gear B meshes with both A and C and is carried on an arm EF which rotates about the centre of A at 18 r.p.m.. If the gear A is fixed, determine the speed of gears B and C

36 An epicyclic train of gears is arranged as shown in Fig. How many revolutions does the arm, to which the pinions B and C are attached, make : **1.** when A makes one revolution clockwise and D makes half a revolution anticlockwise, and **2.** when A makes one revolution clockwise and D is stationary ? The number of teeth on the gears A and D are 40 and 90 respectively.

37 In an epicyclic gear train, the internal wheels A and B and compound wheels C and D rotate independently about axis O. The wheels E and F rotate on pins fixed

to the arm G. E gears with A and C and F gears with B and D. All the wheels have the same module and the number of teeth are :  $T_C = 28$ ;  $T_D = 26$ ;  $T_E = T_F = 18$ .

**1.** Sketch the arrangement  
**2.** Find the number of teeth on A and B ; **3.** If the arm G makes 100 r.p.m. clockwise and A is fixed, find the speed of B ; and **4.** If the arm G makes 100 r.p.m.

clockwise and wheel A makes 10 r.p.m. counter clockwise ; find the speed of wheel B  
38 In an epicyclic gear of the 'sun and planet' type shown in Fig. the pitch circle diameter of the internally toothed ring is to be 224 mm and the module 4 mm. When the ring D is stationary, the spider A, which carries three planet wheels C of equal size, is to make one revolution in the same sense as the sun wheel B for every five revolutions of the driving spindle carrying the sun wheel B. Determine suitable numbers of teeth for all the wheels.

39 An epicyclic gear train consists of a sun wheel S, a stationary internal gear E and three identical planet wheels P carried on a star-shaped planet carrier C. The size of different toothed wheels are such that the planet carrier C rotates at 1/5th of the speed of the sun wheel S. The minimum number of teeth on any wheel is 16. The driving torque on the sun wheel is 100 N-m. Determine : **1.** Number of teeth on different wheels of the train, and **2.** torque necessary to keep the internal gear stationary.

40 Write short notes on cams and followers.

41 Explain with sketches the different types of cams and followers.

42 Why a roller follower is preferred to that of a knife-edged follower ?

43 Define the following terms as applied to cam with a neat sketch

(a) Base circle, (b) Pitch circle, (c) Pressure angle, and (d) Stroke of the follower.

44 What are the different types of motion with which a follower can move ?

45 Draw the displacement, velocity and acceleration diagrams for a follower when it moves with simple harmonic motion. Derive the expression for velocity and acceleration during outstroke and return stroke of the follower.

46 Draw the displacement, velocity and acceleration diagrams for a follower when it moves with uniform acceleration and retardation. Derive the expression for velocity and acceleration during outstroke and return stroke of the follower.

**47** Draw the displacement, velocity and acceleration diagrams for a follower when it moves with uniform velocity. Derive the expression for velocity and acceleration during outstroke and return stroke of the follower.

48 A cam operating a knife-edged follower has the following data :

(a) Follower moves outwards through 40 mm during  $60^\circ$  of cam rotation.

(b) Follower dwells for the next  $45^\circ$ .

(c) Follower returns to its original position during next  $90^\circ$ .

(d) Follower dwells for the rest of the rotation.

The displacement of the follower is to take place with simple harmonic motion during both

The outward and return strokes. The least radius of the cam is 50 mm. Draw the profile of the cam when 1. the axis of the follower passes through the cam axis, and 2. the axis of the follower is offset 20 mm towards right from the cam axis. If the cam rotates at 300 r.p.m., determine maximum velocity and acceleration of the follower during the outward stroke and the return stroke.

49 A disc cam rotating in a clockwise direction is used to move a reciprocating roller with

Simple harmonic motion in a radial path, as given below :

(i) Outstroke with maximum displacement of 25 mm during  $120^\circ$  of cam rotation, (ii) Dwell for  $60^\circ$  of cam rotation,

(iii) Return stroke with maximum displacement of 25 mm during  $90^\circ$  of cam rotation, and (iv) Dwell during remaining  $90^\circ$  of cam rotation. The line of reciprocation of follower passes through the camshaft axis. The maximum radius of cam is 20 mm. If the cam rotates at a uniform speed of 300 r.p.m. find the maximum velocity and acceleration during outstroke and return stroke. The roller diameter is 8 mm. Draw the profile of the cam when the line of reciprocation of the follower is offset by 20 mm towards right from the cam shaft axis.

50 A cam rotating clockwise at a uniform speed of 100 r.p.m. is required to give motion to knife-edge follower as below :

(a) Follower to move outwards through 25 mm during  $120^\circ$  of cam rotation,

(b) Follower to dwell for the next  $60^\circ$  of cam rotation,

(c) Follower to return to its starting position during next  $90^\circ$  of cam rotation, and

(d) Follower to dwell for the rest of the cam rotation.

The minimum radius of the cam is 50 mm and the line of stroke of the follower passes through the axis of the cam shaft. If the displacement of the follower takes place with uniform and equal acceleration and retardation on both the outward and return strokes, find the maximum velocity and acceleration during outstroke and return stroke.

51 Explain Freudenstein's method of three point synthesis of mechanisms.

52 Explain synthesis of mechanism with examples.

53 What do you understand by

(a) Type synthesis ; (b) Number synthesis ; and (c) dimensional synthesis.

54 Write an expression for determining the precision points using Chebyshev's spacing.

55 What do you understand by coupler curves ? Describe the method of obtaining the coordinates of a coupler point in a slider crank mechanism.



56 Synthesize a slider crank mechanism so that the displacement of the slider is proportional to the square of the crank rotation in the interval  $45^\circ \leq \theta \leq 135^\circ$ . Use three precision points with Chebyshev's spacing.

57 Synthesize a four-bar mechanism to generate a function  $y = \sin x$  for  $0 \leq x \leq 90^\circ$ . The range of the output crank may be chosen as  $60^\circ$  while that of input crank be  $120^\circ$ . Assume three precision points which are to be obtained from Chebyshev spacing. Assume fixed link to be 52.5 mm long and  $\theta_1 = 105^\circ$  and  $\phi_1 = 66^\circ$ .

58 A four bar mechanism is to be designed, by using three precision points, to generate the function  $y = x^{1.5}$ , for the range  $1 \leq x \leq 4$ . Assuming  $30^\circ$  starting position and  $120^\circ$  finishing position for the input link and  $90^\circ$  starting position and  $180^\circ$  finishing position for the output link, find the values of  $x$ ,  $y$ ,  $\theta$  and  $\phi$  corresponding to the three precision points.

59 A four bar function generator is used to generate the function  $y = 1/x$  for  $1 \leq x \leq 3$  between the input angle of a crank and the angle the follower makes with the frame. Find the three precision points from Chebyshev's spacing if the initial values of input angle (*i.e.* crank angle) and output angle (*i.e.* follower angle) are  $30^\circ$  and  $200^\circ$  respectively. The difference between the final and initial values of the crank and follower angles are each equal to  $90^\circ$ .

60 Discuss briefly the various types of belts used for the transmission of power. 61 How does the velocity ratio of a belt drive effect, when some slip is taking place between

the belt and the two pulleys ?

62 Obtain an expression for the length of a belt in 1. an open belt drive ; and 2. a cross belt drive.

63 Explain the phenomena of 'slip' and 'creep' in a belt drive.

64 For a flat belt, prove that 1

where

$T_1$  = Tension in the tight side of the belt,

$T_2$  = Tension in the slack side of the belt,

$\mu$  = Coefficient of friction between the belt and the pulley, and

$\theta$  = Angle of contact between the belt and the pulley (in radians.)

65 What is centrifugal tension in a belt ? How does it affect the power transmitted.

66 Derive the condition for transmitting the maximum power in a flat belt drive.

67 Explain what do you understand by 'initial tension in a belt'.

68 Derive an expression for the ratio of the driving tensions in a rope drive assuming the angle of the groove of the pulley to be as  $2\beta$ .

69 Discuss relative merits and demerits of belt, rope and chain drive for transmission of power.

70 What are different types of chains ? Explain, with neat sketches, the power transmission chains. Obtain an expression for the length of a chain.

71 Find the width of the belt, necessary to transmit 7.5 kW to a pulley 300 mm diameter, if the pulley makes 1600 r.p.m and the coefficient of friction between the belt and the pulley is 0.22. Assume the angle of contact as  $210^\circ$  and the maximum tension in the belt is not to exceed 8 N/mm width.

72 An open belt 100 mm wide connects two pulleys mounted on parallel shafts with their centres 2.4 m apart. The diameter of the larger pulley is 450 mm and that of the smaller pulley 300 mm. The coefficient of friction between the belt and the pulley is 0.3 and the maximum stress in the belt is limited to 14 N/mm width. If the larger pulley rotates at 120 r.p.m., find the maximum power that can be transmitted.

73 A leather belt 125 mm wide and 6 mm thick, transmits power from a pulley 750 mm diameter which runs at 500 r.p.m. The angle of lap is  $150^\circ$  and  $\mu = 0.3$ . If the mass of  $1 \text{ m}^3$  of leather is 1 Mg and the stress in the belt is not to exceed 2.75 MPa, find the maximum power that can be transmitted.

74 A flat belt is required to transmit 35 kW from a pulley of 1.5 m effective diameter running at 300 r.p.m. The angle of contact is spread over  $11/24$  of the circumference and the coefficient of friction between belt and pulley surface is 0.3. Determine, taking centrifugal tension into account, width of the belt required. It is given that the belt thickness is 9.5 mm, density of its material is  $1.1 \text{ Mg/m}^3$  and the related permissible working stress is 2.5 MPa.

75 A blower is driven by an electric motor through a belt drive. The motor runs at 750 r.p.m. For this power transmission, a flat belt of 8 mm thickness and 250 mm width is used. The diameter of the motor pulley is 350 mm and that of the blower pulley 1350 mm. The centre distance between these pulleys is 1350 mm and an open belt configuration is adopted. The pulleys are made out of cast iron. The frictional coefficient between the belt and pulley is 0.35 and the permissible stress for the belt material can be taken as  $2.5 \text{ N/mm}^2$  with sufficient factor of safety. The mass of a belt is 2 kg per metre length. Find the maximum power transmitted without belt slipping in any one of the pulleys.

76 An open belt drive connects two pulleys 1.2 m and 0.5 m diameter on parallel shafts 3.6 m apart. The belt has a mass of 1 kg/m length and the maximum tension in it is not to exceed 2 kN. The 1.2 m pulley, which is the driver, runs at 200 r.p.m. Due to the belt slip on one of the pulleys, the velocity of the driven shaft is only 450 r.p.m. If the coefficient of friction between the belt and the pulley is 0.3, find : 1. Torque on each of the two shafts, 2. Power transmitted, 3. Power lost in friction, and 4. Efficiency of the drive.

77 The power transmitted between two shafts 3.5 metres apart by a cross belt drive round the two pulleys 600 mm and 300 mm in diameters, is 6 kW. The speed of the larger pulley (driver) is 220 r.p.m. The permissible load on the belt is 25 N/mm width of the belt which is 5 mm thick. The coefficient of friction between the

smaller pulley surface and the belt is 0.35. Determine : 1. necessary length of the belt ; 2. width of the belt, and 3. necessary initial tension in the belt.

78 A flat belt, 8 mm thick and 100 mm wide transmits power between two pulleys, running at 1600 m/min. The mass of the belt is 0.9 kg/m length. The angle of lap in the smaller pulley is  $165^\circ$  and the coefficient of friction between the belt and pulley is 0.3. If the

Maximum permissible stress in the belt is  $2 \text{ MN/m}^2$ , find : 1. maximum power transmitted and 2. initial tension in the belt

79 An open belt connects two flat pulleys. The smaller pulley is 400 mm diameter and runs at 200 r.p.m. The angle of lap on this pulley is  $160^\circ$  and the coefficient of friction between the belt and pulley face is 0.25. The belt is on the point of slipping when 3 kW is being transmitted. Which of the following two alternatives would be more effective in order to

increase the power : 1. Increasing the initial tension in the belt by 10 per cent, and 2. Increasing the coefficient of friction by 10 per cent by the application of a suitable dressing to the belt?

80 A V-belt drive consists of three V-belts in parallel on grooved pulleys of the same size. The angle of groove is  $30^\circ$  and the coefficient of friction 0.12. The cross-sectional area of

each belt is  $800 \text{ mm}^2$  and the permissible safe stress in the material is 3 MPa.

Calculate the power that can be transmitted between two pulleys 400 mm in diameter rotating at 960 r.p.m.

81 A rope drive is required to transmit 230 kW from a pulley of 1 metre diameter running at 450 r.p.m. The safe pull in each rope is 800 N and the mass of the rope is 0.46 kg per metre length. The angle of lap and the groove angle is  $160^\circ$  and  $45^\circ$  respectively. If the coefficient of friction between the rope and the pulley is 0.3, find the number of ropes required.

82 A rope drive transmits 75 kW through a 1.5 m diameter,  $45^\circ$  grooved pulley rotating at 200 r.p.m. The coefficient of friction between the ropes and the pulley grooves is 0.3 and

the angle of lap is  $160^\circ$ . Each rope has a mass of 0.6 kg/m and can safely take a pull of 800 N. Taking centrifugal tension into account determine : 1. the number of ropes required

for the drive, and 2. initial rope tension.

83 Discuss briefly the various types of friction experienced by a body.

84 State the laws of

(i) Static friction ; (ii) Dynamic friction ; (iii) Solid friction ; and (iv) Fluid friction.

85 Explain the following :

(i) Limiting friction, (ii) Angle of friction, and (iii) Coefficient of friction.



86 Write a short note on journal bearing.

87 What is meant by the expression 'friction circle'? Deduce an expression for the radius of Friction circle in terms of the radius of the journal and the angle of friction.

88 From first principles, deduce an expression for the friction moment of a collar thrust bearing, stating clearly the assumptions made.

89 Derive an expression for the friction moment for a flat collar bearing in terms of the inner radius  $r_1$ , outer radius  $r_2$ , axial thrust  $W$  and coefficient of friction  $\mu$ .

Assume uniform

intensity of pressure.

90 Derive from first principles an expression for the friction moment of a conical pivot Assuming (i) Uniform pressure, and (ii) Uniform wear

91 A truncated conical pivot of cone angle  $\phi$  rotating at speed  $N$  supports a load  $W$ . The smallest and largest diameter of the pivot over the contact area are ' $d$ ' and ' $D$ ' respectively. Assuming uniform wear, derive the expression for the frictional torque.

92 A conical pivot bearing 150 mm in diameter has a cone angle of  $120^\circ$ . If the shaft supports an axial load of 20 kN and the coefficient of friction is 0.03, find the power lost in friction

when the shaft rotates at 200 r.p.m., assuming 1. Uniform pressure, and 2. uniform wear

93 A vertical shaft supports a load of 20 kN in a conical pivot bearing. The external radius of the cone is 3 times the internal radius and the cone angle is  $120^\circ$ . Assuming uniform intensity of pressure as  $0.35 \text{ MN/m}^2$ , determine the dimensions of the bearing.

If the coefficient of friction between the shaft and bearing is 0.05 and the shaft rotates at 120 r.p.m., find the power absorbed in friction.

94 A plain collar type thrust bearing having inner and outer diameters of 200 mm and 450 mm is subjected to an axial thrust of 40 kN. Assuming coefficient of friction between the thrust surfaces as 0.025, find the power absorbed in overcoming friction at a speed of 120 r.p.m. The rate of wear is considered to be proportional to the pressure and rubbing speed.

95 *The thrust of a propeller shaft in a marine engine is taken up by a number of collars integral with the shaft which is 300 mm in diameter. The thrust on the shaft is 200 kN and the speed is 75 r.p.m. Taking  $\mu$  constant and equal to 0.05 and assuming intensity of pressure as uniform and equal to  $0.3 \text{ N/mm}^2$ , find the external diameter of the collars and the number of collars required, if the power lost in friction is not to exceed 16 kW.*

96 *A shaft has a number of collars integral with it. The external diameter of the collars is 400 mm and the shaft diameter is 250 mm. If the intensity of pressure is  $0.35 \text{ N/mm}^2$  (uniform) and the coefficient of friction is 0.05, estimate : 1. power*

*absorbed when the shaft runs at 105 r.p.m. carrying a load of 150 kN ; and 2. number of collars required.*

*97 A conical pivot bearing supports a vertical shaft of 200 mm diameter. It is subjected to a load of 30 kN. The angle of the cone is  $120^\circ$  and the coefficient of friction is 0.025. Find the power lost in friction when the speed is 140 r.p.m., assuming 1. uniform pressure and 2. uniform wear.*

*98 A conical pivot supports a load of 20 kN, the cone angle is  $120^\circ$  and the intensity of normal pressure is not to exceed  $0.3 \text{ N/mm}^2$ . The external diameter is twice the internal diameter. Find the outer and inner radii of the bearing surface. If the shaft rotates at 200 r.p.m. and the coefficient of friction is 0.1, find the power absorbed in friction. Assume uniform pressure.*

*99 A vertical shaft 150 mm in diameter rotating at 100 r.p.m. rests on a flat end footstep bearing. The shaft carries a vertical load of 20 kN. Assuming uniform pressure distribution and coefficient of friction equal to 0.05, estimate power lost in friction.*

*100 Explain the terms*

*a) Over-Hauling of Screws*

*b) Self-Locking of Screws*