Lecture 28

Op- Amp

Input Impedance

Input Impedance can be regarded as,

$$R_{in} = R_a + R_\pi \, // \, R'$$

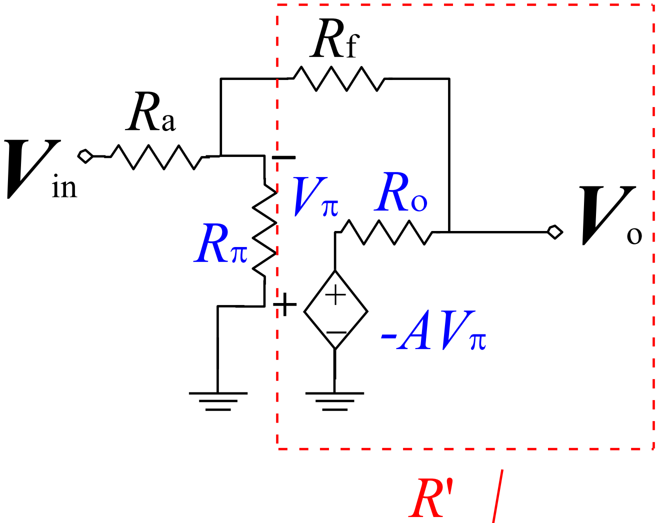
where R' is the equivalent impedance of the red box circuit, that is

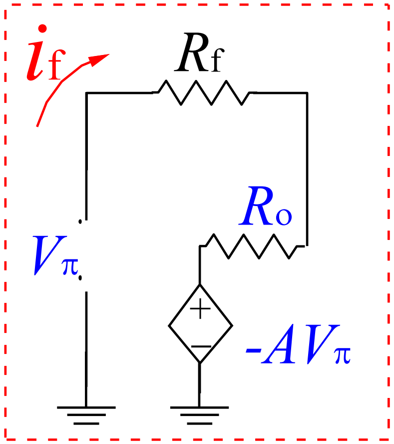
$$R' = \frac{V_\pi}{i_f}$$

However, with the below circuit,

$$V_\pi - (-AV_\pi) = i_f (R_f + R_o)$$

$$\Rightarrow R' = \frac{V_\pi}{i_f} = \frac{R_f + R_o}{1 + A}$$





Input Impedance

Finally, we find the input impedance as,

$$R_{in} = R_a + \left[\frac{1}{R_\pi} + \frac{1+A}{R_f + R_o} \right]^{-1} \quad \Rightarrow \quad R_{in} = R_a + \frac{R_\pi (R_f + R_o)}{R_f + R_o + (1+A) R_\pi}$$

Since, $R_f + R_o << (1+A) R_\pi$, R_{in} become,

$$R_{in} \sim R_a + \frac{(R_f + R_o)}{(1+A)}$$

Again with $R_f + R_o << (1+A)$

$$R_{in} \sim R_a$$

Note: The op-amp can provide an impedance isolated from input to output

Output Impedance

Only source-free output impedance would be considered, i.e. V_i is assumed to be 0

Firstly, with figure (a),

$$V_\pi = \frac{R_a // R_\pi}{R_f + R_a // R_\pi} V_o \Rightarrow V_\pi = \frac{R_a R_\pi}{R_a R_f + R_a R_\pi + R_f R_\pi} V_o$$

By using KCL, $i_o = i_1 + i_2$

$$i_o = \frac{V_o}{R_f + R_a // R_f} + \frac{V_o - (-AV_\pi)}{R_o}$$

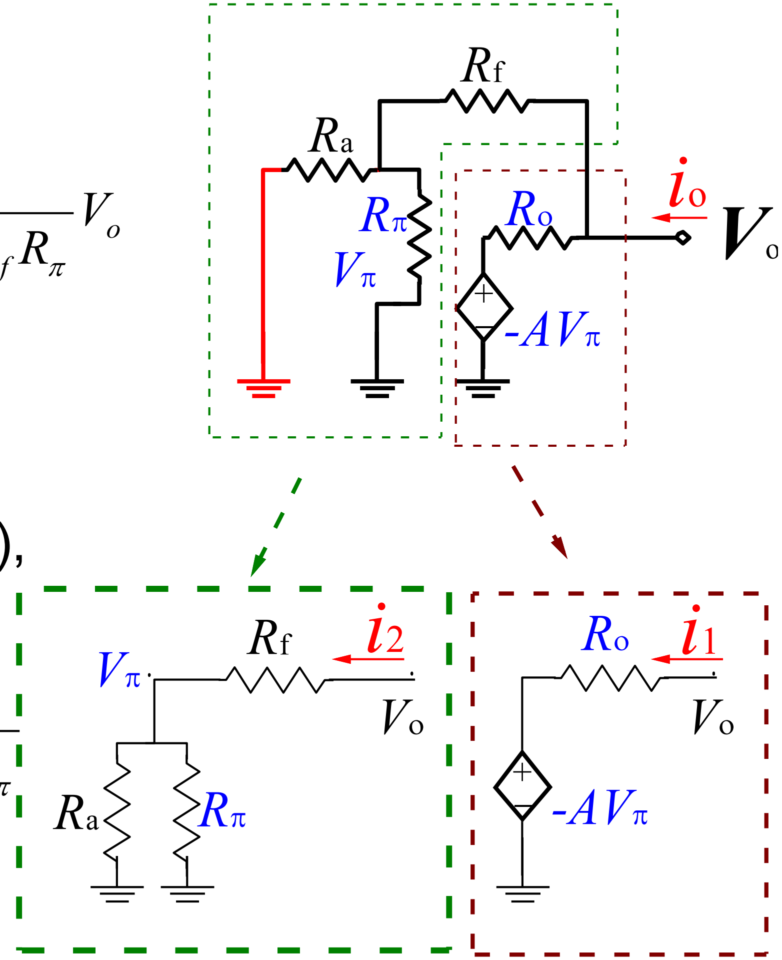
By substitute the equation from Fig. (a),

The output impedance, R_{out} is

$$\frac{V_o}{i_o} = \frac{R_o(R_a R_f + R_a R_\pi + R_f R_\pi)}{(1+R_o)(R_a R_f + R_a R_\pi + R_f R_\pi) + (1+A) R_a R_\pi}$$

$\therefore R_\pi$ and A comparably large,

$$R_{out} \sim \frac{R_o(R_a + R_f)}{AR_a}$$



(a) (b)