

ACTIVE NETWORK SYNTHESIS

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- IC technology immensely influences the design of networks for voice and data comm.
- It enables the realization of these n/ws with small-size and low cost resistors, capacitors and active elements .
- They eliminate the need for inductors which are relatively bulky and expensive.
- Active R-C n/ws further give advantages such as :
 - (a) Standardisation and modularity of design
 - (b) Switchability
 - (c) Ease of manufacture
 - (d) Better performance vis-a-vis cost
 - (e) Much useful with computer aids
- A wide range of n/ws and filters using active R-C n/ws have been developed during the last two decades.

Elements used in active N /Ws

- Resistors
- Capacitors
- Active Elements like
 - (a) Op-amp (operational amplifier)
 - (b) Gytrators
 - (c) Generalized Impedance Converters
- A Controlled Source is considered a basic active element .The are classified as under:
 - (i) Current controlled current source (cct)- Transistor
 - (ii) Voltage controlled current source (VCT)– Field EffectTransistor
 - (iii) Voltage controlled voltage source (VCT)– op amp
 - (iv) Current controlled voltage source

Operational Amplifier

- Also known as **Op amp**. It is designed to sense the difference
- between the voltage signals applied at its two i/p terminals
- (i.e., $V_b - V_a$), multiply by a voltage gain A and cause the resulting voltage $A (V_b - V_a)$ to appear at o/p terminal.
- **Characteristics of Ideal op – amp**
 - (a) Infinite voltage gain
 - (b) Infinite bandwidth
 - (c) Infinite input impedance
 - (d) Zero output impedance
 - (e) Zero drift (parameter not changing with temp)
 - (f) Infinite slew rate (o/p voltage change occurs simultaneous with the i/p voltage change)
 - (g) Zero common mode gain (the op-amp gives only to the difference signal $V_b - V_a$ and so ignores any signal common to both inputs. i.e if $V_b = V_a = 1V$ then an ideal op-amp has zero common mode gain or equivalently infinite common mode rejection.)

Active Components

- Gyrator : It is a 2-port device which is becoming an integral part of active filter design and inductor simulation . It is a non reciprocal device.

- A gyrator is characterised by the terminal relationships

$$V_1 = - r_1 I_2$$

$$V_2 = - r_2 I_1$$

If $r_1 = r_2$, the power delivered to the gyrator is zero. Such a device is called passive lossless one and is called an ideal gyrator.

If $r_1 \neq r_2$, the power can be made negative and then the device is called an active gyrator. It is also considered as an impedance inverter.

2-port parameters of gyrator are

$$z_{11} = 0 \quad z_{22} = 0 \quad , \quad y_{11} = 0 \quad y_{22} = 0$$

$$z_{12} = - r_1 \quad z_{21} = r_2 \quad , \quad y_{12} = g_2 \quad y_{21} = - g_1$$

Filters

- A **filter** is a device that passes electric signals at certain frequencies or frequency ranges while preventing passage of others .Filters are used in wide range of applications esuch
 - (a) Modem and speech processing
 - (b) Channel selection in telephone central offices
 - (c) Data acquisition systems
 - (d) System power supplies

Types of Filters

- (i) Low Pass Filter (LPF)
- (ii) High Pass Filter (HPF)
- (iii) Band Pass Filter (BPF)
- (iv) Band Stop Filter (BSF)

Band Pass Filter can be realized by connecting LPF and HPF in Series.

Band Stop Filter can be realized by connecting LPF and HPF₆ in Parallel.

decibels

- Decibels are represented by dBs
- Decibels are the unit of power.
- **Power gain in dB = $10 \log(P_2 / P_1)$**
ex input power = 1 w and output power = 100w
Then gain in dBs = 20dBs [$10 \log (100 / 1)$]
- **In terms of voltage**
- **gain = $20 \log(V_2 / V_1)$**
ex input voltage = 1 V and output Voltage = 100V
Then gain in dBs =40 dBs [$20 \log(100 / 1)$]

Attenuation is reverse of Amplification

3 dB reduction means power has attenuated by half

Active Filters

- Advantages of Active R-C filters :
 - (i) Bulky inductors are not used .only R,C and op-amps are used. This saves cost ,makes the design more compact and reduces the loss.
 - (ii) Increased circuit reliability , because all the processing can be automated.
 - (iii) The design process is simpler than that for passive filters.
 - (iv) They have high gain , inherently high input impedance with low output impedance.
 - (v) They can realize a wider class of functions.
 - (vi) They are easily compatible with IC circuits due to absence of inductor in the circuit.
 - (vii) Improvement in performance because high quality components can be realized readily.
 - (viii) A reduction in parasitics , because of the smaller size.

Low Pass Filter

- $(v_0 - v) / R_2 = (v - 0) / R_1$
or $v = v_0 / [1 + (R_2 / R_1)]$ (1)

- $(v_i - v) / R = v / [1 / sC]$ or
 $v = v_i / [1 + RCs]$ (2) From eq (1) and (2)

- $v_0 / [1 + (R_2 / R_1)] = v_i / [1 + RCs]$
or $v_0 / v_i = [1 + (R_2 / R_1)] / [1 + RCs]$ (3)

Gain of the op-amp circuit is

- $A_0 = v_0 / v = 1 + (R_2 / R_1)$ (4) From eq (3) and (4)

- $H(s) = v_0 / v_i = A_0 / [1 + RCs]$
 $= A_0 / [1 + s / \omega_0]$

This is the transfer function of First Order Active Low Pass Filter.

$\omega_0 = 1 / RC$ represents the cut – off frequency.

Hence for given cut-off frequency ω_0 and assumed C , the value of R can be evaluated .
Similarly , for arbitrary gain $A_0 =$ and some value of R_1 , the value of R_2 can be
obtained and hence first

order active low pass filter can be designed.

High Pass Filter

- $(v_0 - v) / R_2 = (v - 0) / R_1$
or $v = v_0 / [1 + (R_2 / R_1)]$ (1)

- $(v_i - v) / [1 / sc] = v / R$ or
 $v = v_i / [1 + (1/ RCs)]$ (2) From eq (1)

and (2)

- $v_0 / [1 + (R_2 / R_1)] = v_i / [1 + RCs]$
or $v_0 / v_i = [1 + (R_2 / R_1)] / [1 + 1/ RCs]$ (3)

Gain of the op-amp circuit is

- $A_0 = v_0 / v = 1 + (R_2 / R_1)$ (4) From eq (3)

and (4)

- $H(s) = v_0 / v_i = A_0 / [1 + 1/ RCs]$
 $= A_0 / [1 + 1/(s / w_0)] = A_0 (s / w_0) / [1 + (s / w_0)]$

Which is the transfer function of First Order Active High Pass Filter.

$w_0 = 1 / RC$ represents the cut – off frequency.

Hence for given cut-off frequency w_0 and assumed C , the value of R can be evaluated . Similarly , for arbitrary gain $A_0 =$ and some value of R_1 , the value of R_2 can be obtained and hence first order active high pass filter can be designed.

The interchanging of R and C in low pass filter results in first order high pass filter.

Band Pass Filter

Active LPF is in Series with active HPF

$f_1 = 1 / 2 R_1 C_1$ high frequency cut-off of LPF

$f_2 = 1 / 2 R_0 C_0$ low frequency cut-off of HPF

Band Stop Filter

- Active LPF is in Parallel with active HPF
- Low frequency cut –off of HPF $f_2 = 1 / 2 R_h C_h$
- High frequency cut –off of LPF $f_1 = 1 / 2 R_l C_l$
- The final op-amp stage acts as a summer.