

GENERAL DESCRIPTION OF SIGNALS

- **Time Constant** It refers only to exponential waveforms .It is a useful measure of the decay of an exponential .
- Defined as the time interval for an exponential function to decrease to 37 % of its initial value or increase to 63% of its final value
- Consider an exponential waveform described by
$$r (t) = K e^{-t/T} u (t)$$
from the plot of this function we see that when $t = T$,
$$r (t) = 0.37 r (0)$$
also $r (4 T) = 0.02 r (0)$. This shows that the larger the time constant ,the longer it requires for the waveform to reach 37 % of its peak value. In circuit analysis ,the common time constants are the factors RC and RL .
- **RMS Value , D-C Value , Duty Cycle and Crest Factor** are other terms which describe only Periodic Waveforms.

GENERAL DESCRIPTION OF SIGNALS (CONTD.)

- **RMS Value** The rms or root mean square value of a periodic waveform $e(t)$ is defined

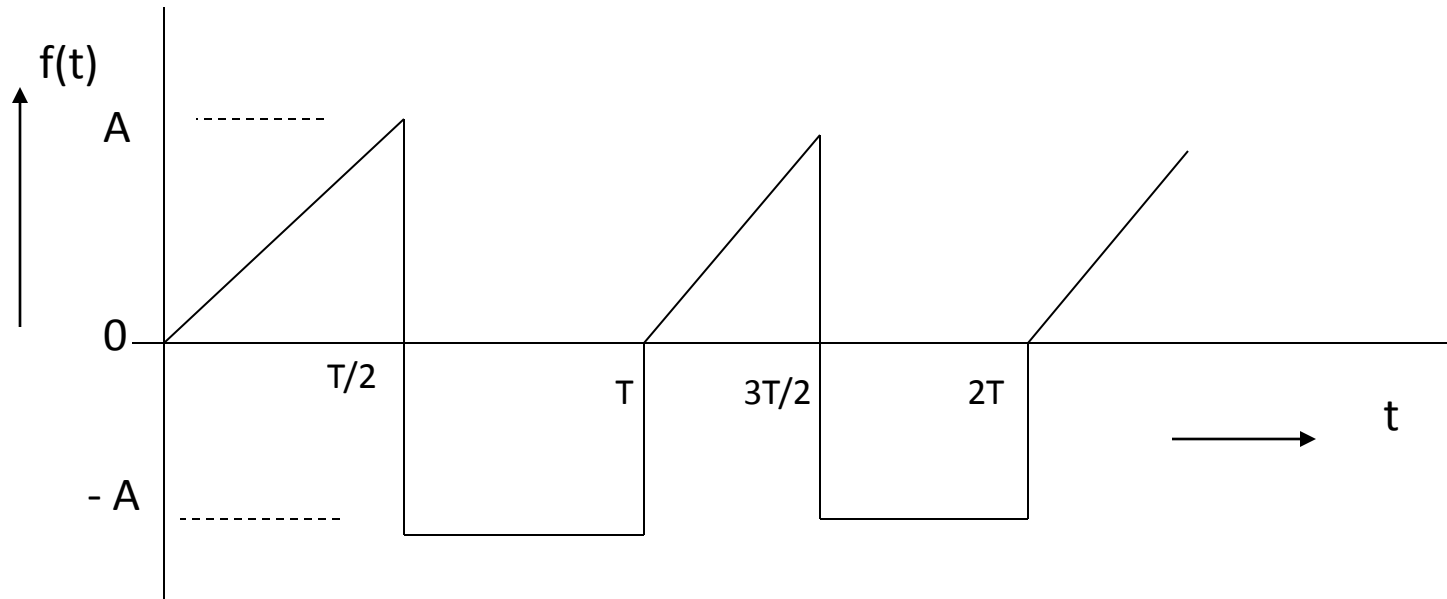
$$e_{\text{rms}} = \left[\frac{1}{T} \int_0^T e^2(t) dt \right]^{1/2} \text{ where } T \text{ is the period. If the}$$

waveform is not periodic, the term rms does not apply.

Show that for a periodic waveform which is triangular in period 0 to $T/2$ with amplitude increasing from 0 to A v and rectangular in next half period $T/2$ to T with amplitude $-A$ v during this half period. The rms value works out to be

$$\sqrt{2/3} A \text{ v}$$

Ex : find rms value of the waveform shown below

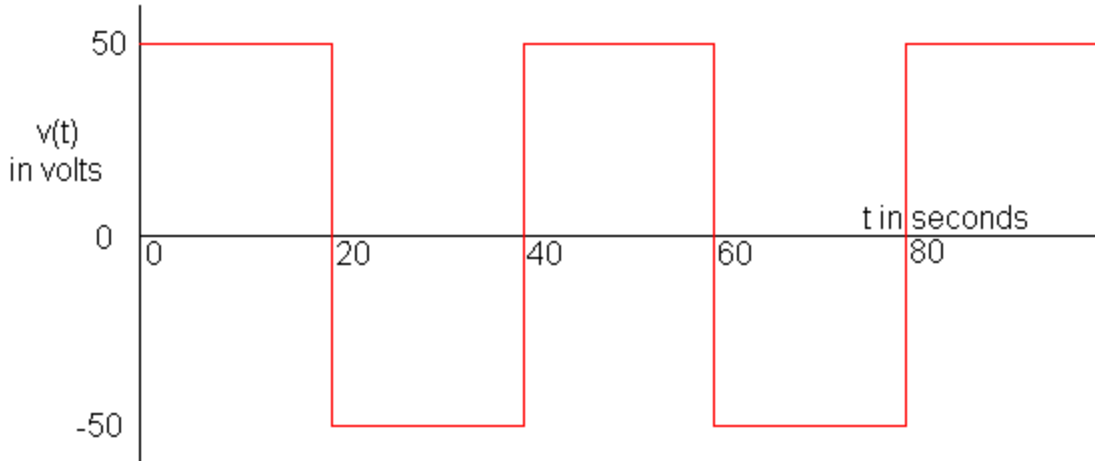


- rms VALUE = $A \sqrt{2/3}$

Solution

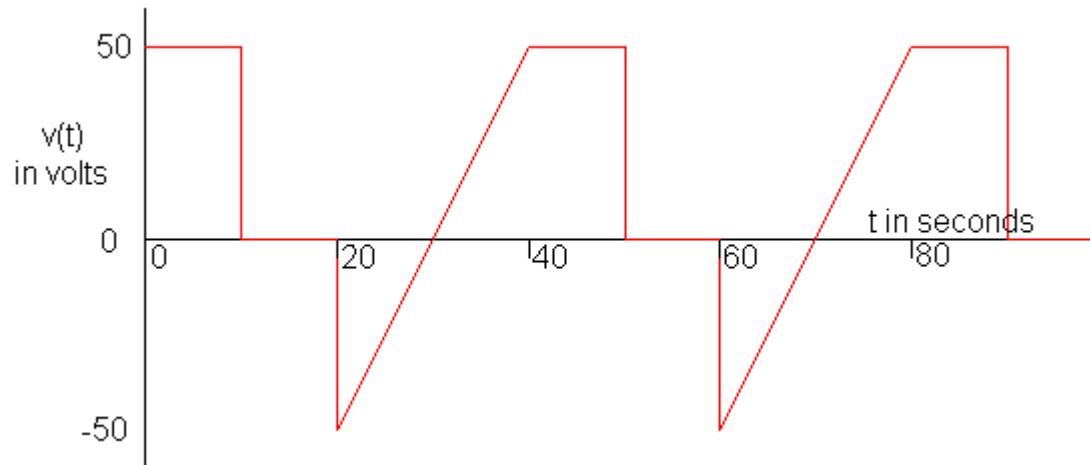
$$\begin{aligned} \bullet E_{\text{rms}} &= \left[\frac{1}{T} \left\{ \int_0^{T/2} (2A t/T)^2 dt + \int_{T/2}^T A^2 dt \right\} \right]^{1/2} \\ &= \left[\frac{1}{T} \left\{ \left(\frac{4A^2}{T^2} \right) \left. \frac{t^3}{3} \right|_0^{T/2} + \left. A^2 t \right|_{T/2}^T \right\} \right]^{1/2} \\ &= A \sqrt{2/3} \end{aligned}$$

- Find rms value of the waveform shown below



$$V_{\text{rms}} = \{[50^2 + (-50)^2]/2\}^{1/2} = \{[2500 + 2500]/2\}^{1/2} = \{2500\}^{1/2} = 50 \text{ V}$$

FIND THE RMS AND VALUE OF THE WAVEFORM SHOWN BELOW



Solution

$$V_{\text{rms}} = \sqrt{\frac{1}{40} \left[\int_0^{t_1} v^2 dt + \int_{t_1}^{t_2} v^2 dt + \int_{t_2}^{40} v^2 dt \right]}$$

$$V_{\text{rms}} = \sqrt{\frac{1}{40} \left[\int_0^{10} v^2 dt + \int_{10}^{20} v^2 dt + \int_{20}^{40} v^2 dt \right]}$$

$$V_{\text{rms}} = \sqrt{\frac{1}{40} \left[\int_0^{10} 2500 dt + \int_{10}^{20} 0 dt + \int_{20}^{40} (5t - 150)^2 dt \right]}$$

Solution (contd)

$$V_{\text{rms}} = \sqrt{\frac{1}{40} \left[25000 + 0 + 16667 \right]}$$

$$V_{\text{rms}} = \sqrt{41667/40}$$

$$V_{\text{rms}} = 32.27 \text{ V}$$

This rounds off to $V_{\text{rms}} = 32 \text{ V}$

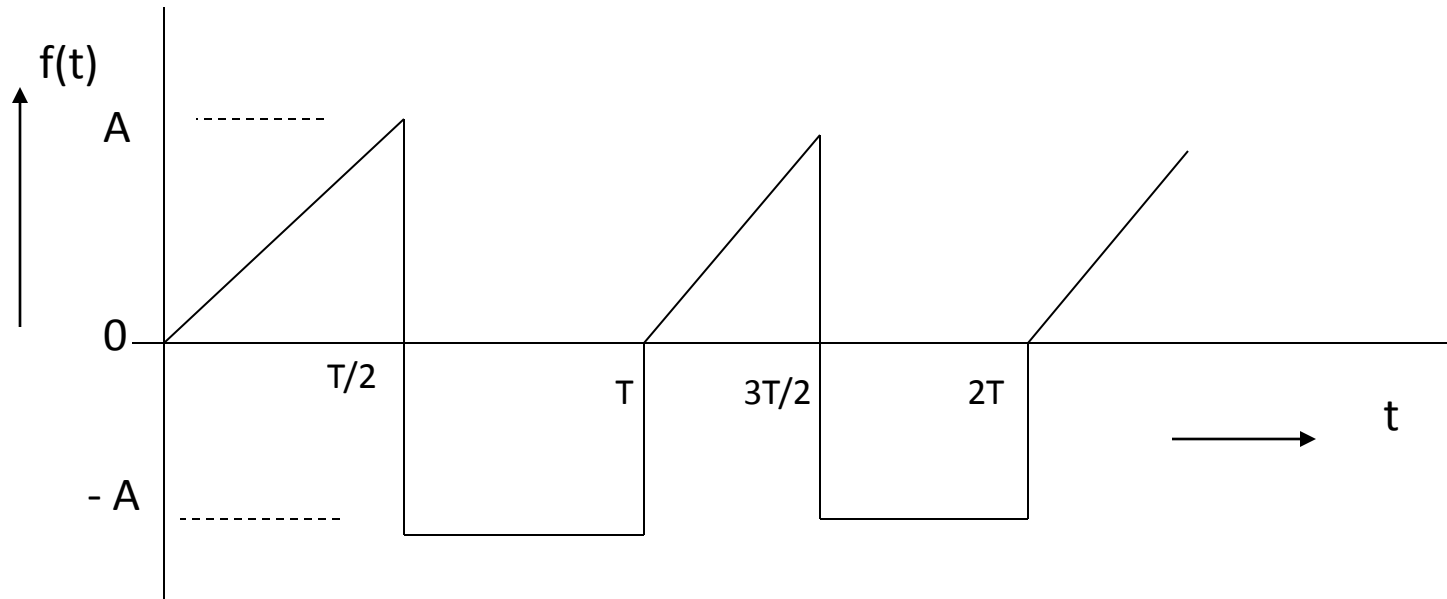
GENERAL DESCRIPTION OF SIGNALS (CONTD)

- **D-C Value** The d-c value (or average value) of a waveform has meaning only when the waveform is periodic . It is the average value of the waveform over one period

$$e_{d-c} = \frac{1}{T} \int_0^T e(t) dt \quad \text{where } T \text{ is the period .}$$

The d-c value of the wave form described earlier works out to be $-A/4$ v.

Ex : find average value of the waveform shown below



$$\text{AVERAGE VALUE} = -A/4$$

Solution

$$\begin{aligned} & T \\ \bullet \quad E_{dc} &= \frac{1}{T} \int_0^T e(t) dt \\ &= \frac{1}{T} \left[\int_0^{T/2} (2A/T) t dt + \int_{T/2}^T (-A) dt \right] \\ &= -A/4 \end{aligned}$$

GENERAL DESCRIPTION OF SIGNALS (CONTD)

- **DUTY CYCLE** The term Duty Cycle , D , is defined as the ratio of the time duration of the POSITIVE CYCLE t_o of a periodic waveform to the period ,T , that is

$$D = \frac{t_o}{T}$$

CREST FACTOR Crest factor is defined as the ratio of the peak voltage(maximum value) of the periodic waveform to the rms value (with the d-c component removed).

Form Factor defined as the ratio of rms value to the average value