

Signal Analysis

Section -A

- Signal Analysis
- Complex Frequency and Network Analysis
- General Characteristics and Descriptions of signal
- Step Function and Associated Wave Forms
- The Unit Impulse
- Introduction to network analysis
- Network elements
- Initial and final conditions
- Step and Impulse response
- Solution of network equation

Signal

- Any physical quantity that varies with respect to time, space or any other independent variables is called a signal
- A function of one or more independent variable that convey information on the nature of physical phenomena
- Sinusoidal signal - $s(t) = A \sin(\omega_0 t + \Theta)$
 - A = amplitude
 - ω_0 = radian frequency
 - Θ = phase
- Now suppose that the signal is made up of $2n+1$ sinusoidal components

$$s(t) = \sum_{i=-n}^n A_i \sin(\omega_i t + \theta_i)$$

- In continuous case,

$$s(t) = \int_{-\infty}^{\infty} A(\omega) \sin[\omega t + \theta(\omega)] d\omega$$

Complex Frequency

- Complex frequency variable – $S = \sigma + j\omega$
 - Real part = σ = growth of the amplitude of signal
 - Imaginary part = $j\omega$ = angular frequency
- Ideal of complex frequency is $s(t) = A e^{j\omega t}$
- Any function which may be written in the form $f(t) = K e^{st}$
 - K and s are complex constant

- CASE-I = A constant current, $i(t) = I_0$ may be written as $i(t) = I_0 e^{(0)t}$
 - The complex frequency of a DC current is zero
- CASE-II = Exponential function, $i(t) = I_0 e^{\sigma t}$
 - The complex frequency of this current is therefore σ , $s = \sigma + j0$
- CASE-III = A sinusoidal current=
 - $i(t) = I_m \cos(\omega t + \Theta)$

Classification of system

- Linear or Non Linear
- Passive or Active
- Reciprocal
- Causal and Non Causal
- Time – Invariant and Time Varying System
- Derivative and Integral property

Linear or Non Linear

- A system(network) is linear if (a) the principle of SUPERPOSITION and(b) the principle of PROPORTIONALITY hold.

- **SUPERPOSITION PRINCIPLE :**

If for a given network, $\{ e_1(t), r_1(t) \}$ and $\{ e_2(t), r_2(t) \}$ are excitation-response pairs, then if the excitation were $e(t) = e_1(t) + e_2(t)$, the response would be $r(t) = r_1(t) + r_2(t)$.

- **PROPORTIONALITY PRINCIPLE :**

If for a given network, $e_1(t), r_1(t)$ are excitation-response pairs, then if the excitation were $c_1 e_1(t)$, then response would be $c_1 r_1(t)$. The constant of proportionality is c_1 is preserved by the linear network. In a system if $c_1 e_1(t) + c_2 e_2(t)$ gives rise to $c_1 r_1(t) + c_2 r_2(t)$. Then the system is a linear system.

- Note

- A linear network consist of linear elements, e.g. resistor, inductor and capacitor.
- A Network is said to be nonlinear if it contains diode, transistor.

Passive and Active network

- A linear network is passive if (a) the energy delivered to the network is non-negative for any arbitrary excitation , and (b) if no voltages or currents appear between any two terminals before an excitation is applied.
- A linear network is active if there is any energy source and a response appear between any two terminal in the absence of an input (excitation) applied.

Reciprocal

- A network is said to be **reciprocal** if when the points of excitation and measurement of response are interchanged , the relationship between excitation and response remains the same. This must be true for any choice of points of excitation & response.

Causal and NonCausal

- A system is causal if the response at any time depends only on values of the excitation at the present and past time. its response is non-anticipatory, i.e. if

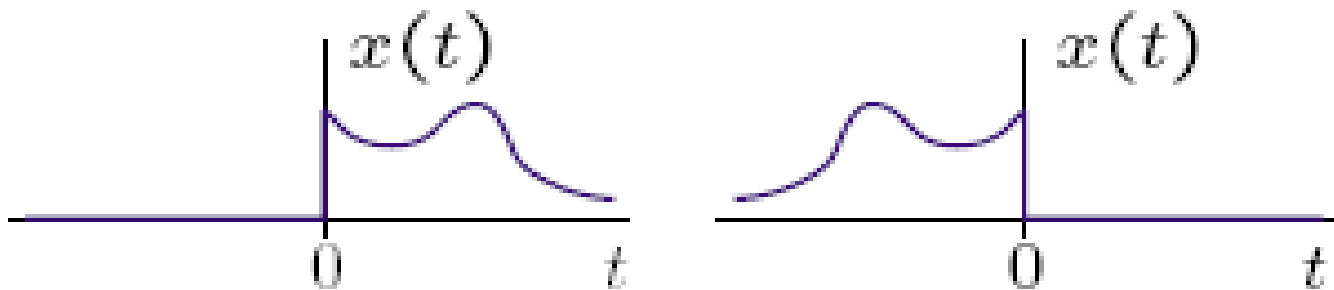
$$e(t) = 0 \quad t < T$$

$$\text{then } r(t) = 0 \quad t < T$$

in other words , a system is causal if before an excitation is applied at $t = T$, the response is zero for $-\infty < t < T$.

A system is called non-causal system if its output at a given time depends on the input at future time.

A **causal** signal is zero for $t < 0$ and a **non-causal** signal is zero for $t > 0$



Time Invariant and time varying system

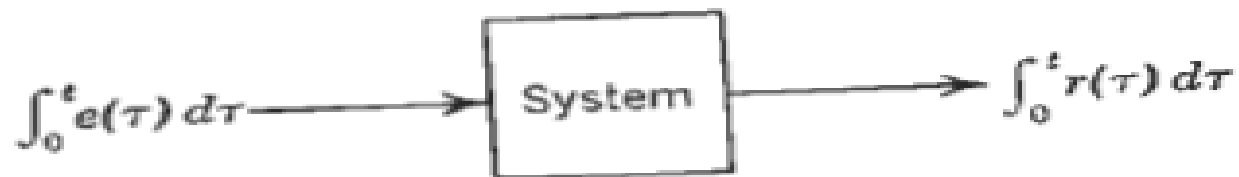
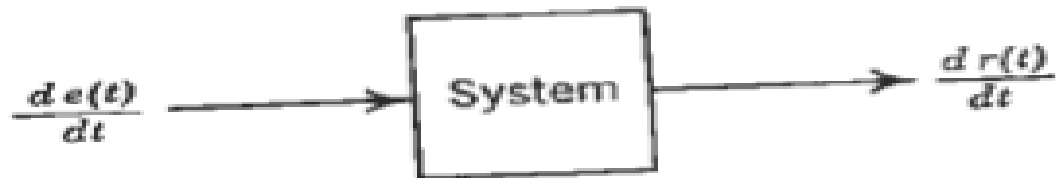
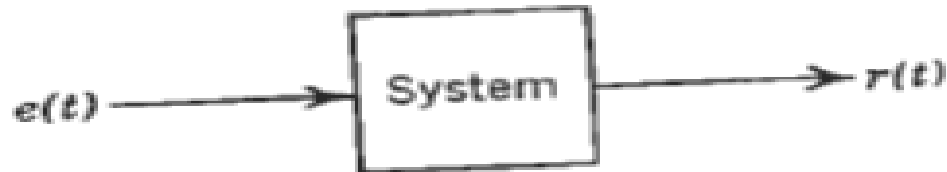
A system is time invariant if a time shift (delay or advance) in the input signal causes the same time shift in output signal, $e(t) \rightarrow r(t)$ implies that $e(t \pm T) \rightarrow r(t \pm T)$. From this property we can show that if $e(t)$ at the input gives rise to $r(t)$ at the output then if the input were $e'(t)$ i.e. the derivative of $e(t)$, the response would be $r'(t)$.

A system which does not satisfy above equation is called a time varying system, i.e. if the input output characteristics of a system change with time

Derivative and Integral Property

- For any time invariant , if $r(t)$ is the response for excitation $e(t)$, then for derivative of $e(t)$, the response would also be derivative of $r(t)$.

Derivative property of the system



Circuit element

- The voltage source
- The current source
- Dependent source
 - Voltage dependent voltage source
 - Voltage dependent Current source
 - Current dependent Current source
 - Current dependent voltage source
- Resistor
- Capacitor
- Inductor