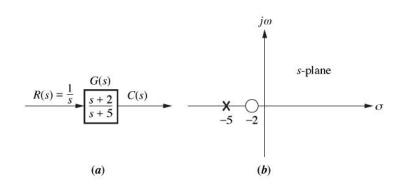
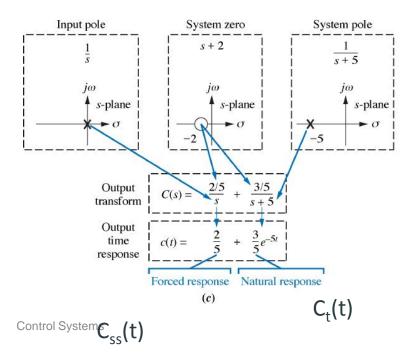
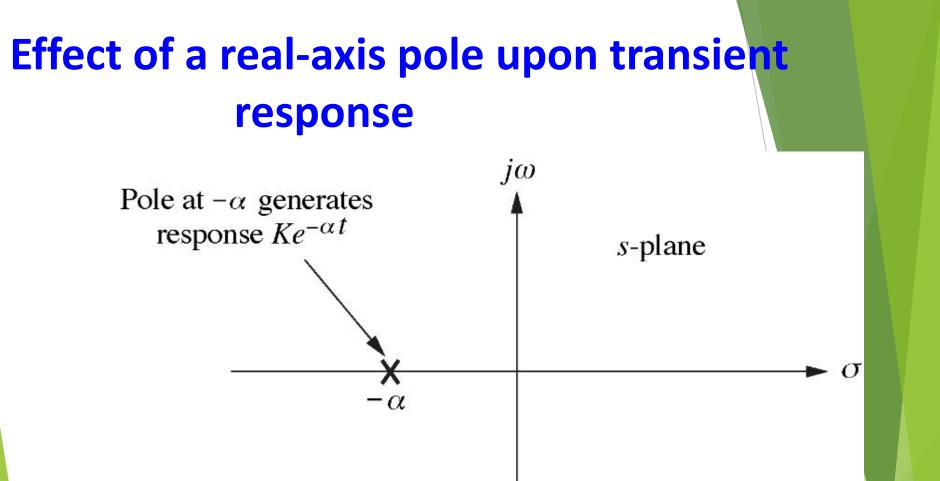
Poles and zeros

- 1. A pole of the input function generates the form of the forced response (that is the pole at the origin generated a step function at the output).
- 2. A pole of the transfer function generate the form of the exponential response
- 3. The zeros and poles generate the amplitudes for both the transit and steady state responses (see A, B in partial fraction extension)

Poles and zeros of a first order system

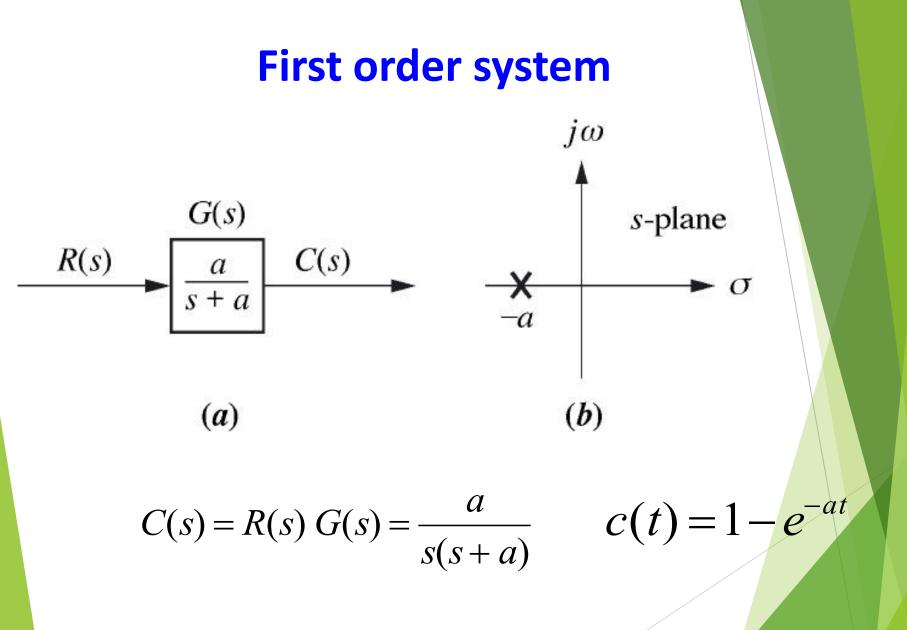






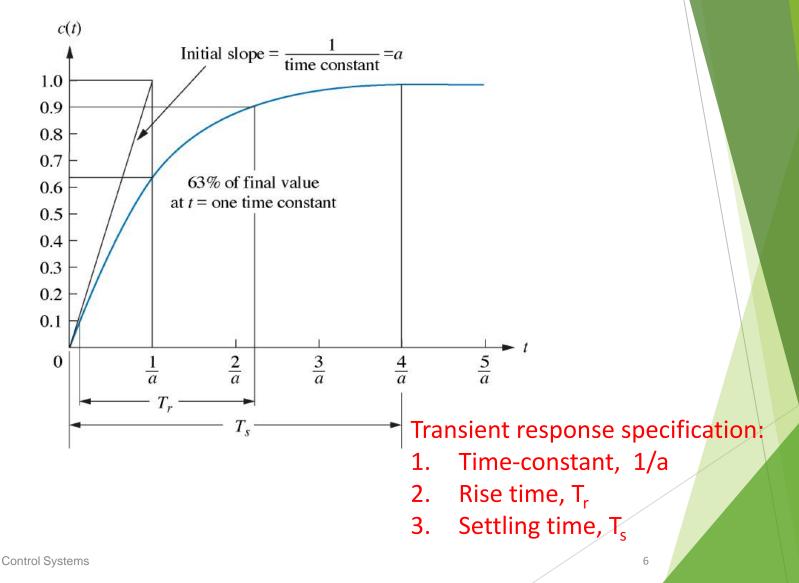
A pole on the real axis generate an exponential response of the form $\text{Exp}[-\alpha t]$ where $-\alpha$ is the pole location on real axis. The farther to the left a pole is on the negative real axis, the faster the exponential transit response will decay to zero.

Evaluating response using poles $R(s) = \frac{1}{s}$ (s+3) C(s) (s+2)(s+4)(s+5) $C(s) = \frac{K_1}{s} + \frac{K_2}{s+2} + \frac{K_3}{s+4} + \frac{K_4}{s+5}$ $C_{ss}(t)$ $C_{t}(t)$ $c(t) = K_1 + K_2 e^{-2t} + K_3 e^{-4t} + K_4 e^{-5t}$ Control Syster



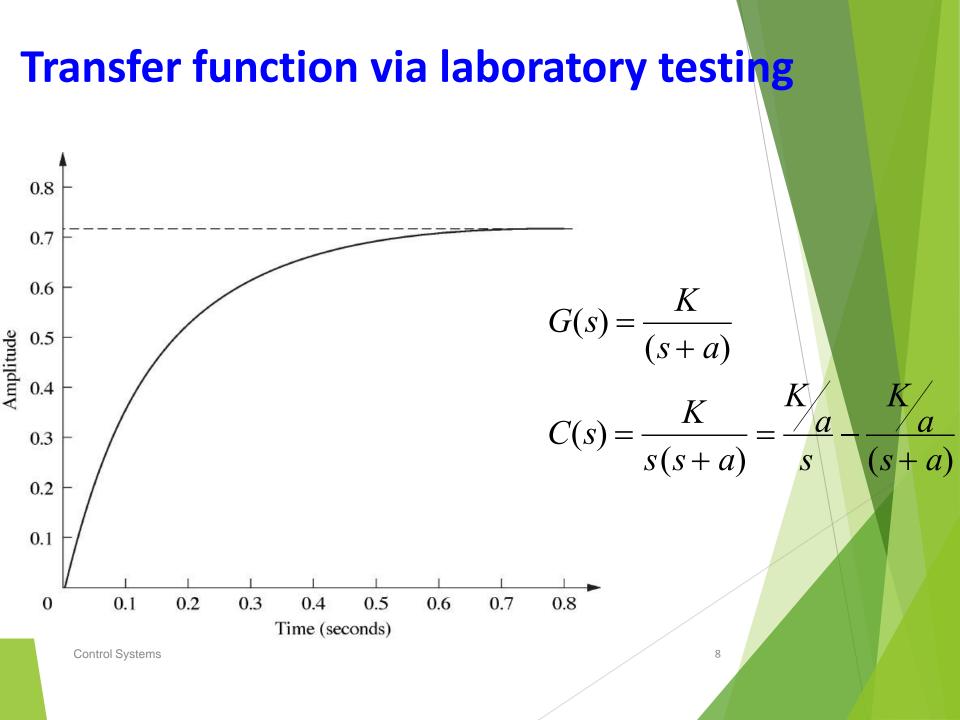
Control Systems

First-order system response to a unit step



Transient response specification for a first-order system

- Time-constant, 1/a Can be described as the time for (1 -Exp[- a t]) to rise to 63 % of initial value.
- Rise time, T_r = 2.2/a The time for the waveform to go from 0.1 to 0.9 of its final value.
- 3. Settling time, T_s = 4/a The time for response to reach, and stay within, 2% of its final value



Identify K and a from testing

The time for amplitude to reach 63% of its final value: 63 x 0.72 = 0.45, or about 0.13 sec , a = 1/0.13 = 7.7

From equation, we see that the forced response reaches a steady-state value of K/a =0.72.

K= 0.72 x 7.7= 5.54

G(s) = 5.54/(s+7.7).