

# Introduction to CMOS VLSI Design

## CMOS Transistor Theory

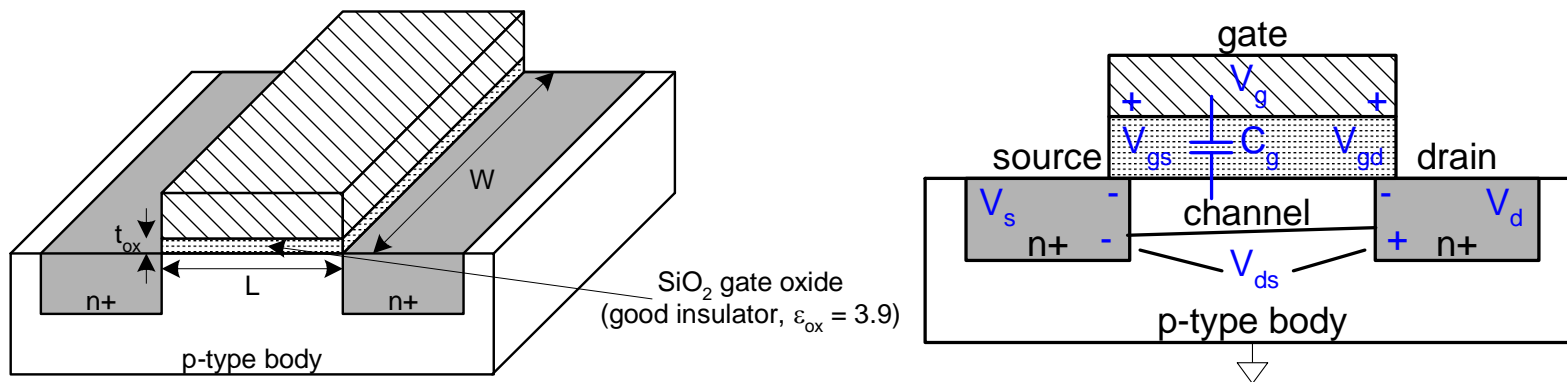
# I-V Characteristics

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- In Linear region,  $I_{ds}$  depends on
  - How much charge is in the channel?
  - How fast is the charge moving?

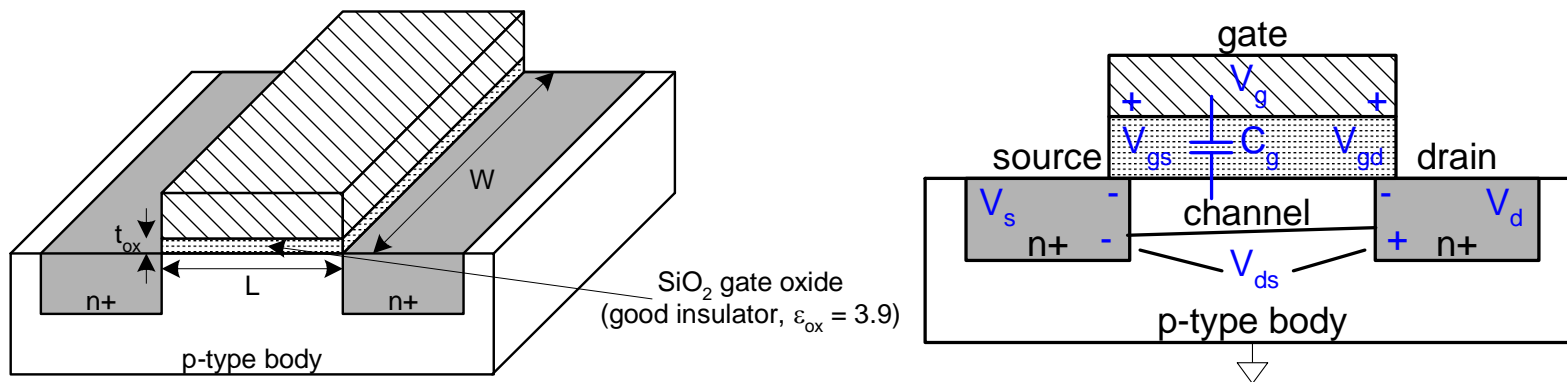
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- ❑ MOS structure looks like parallel plate capacitor while operating in inversion
  - Gate – oxide – channel
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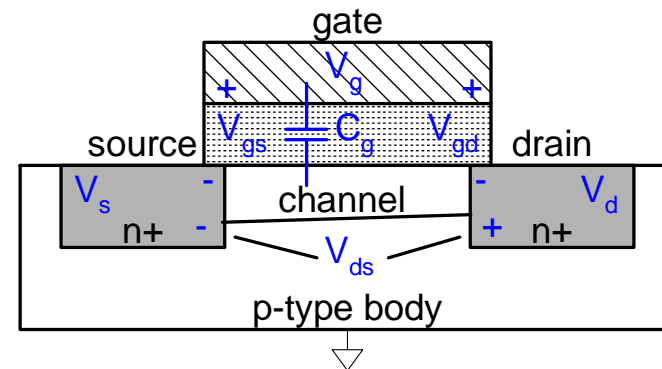
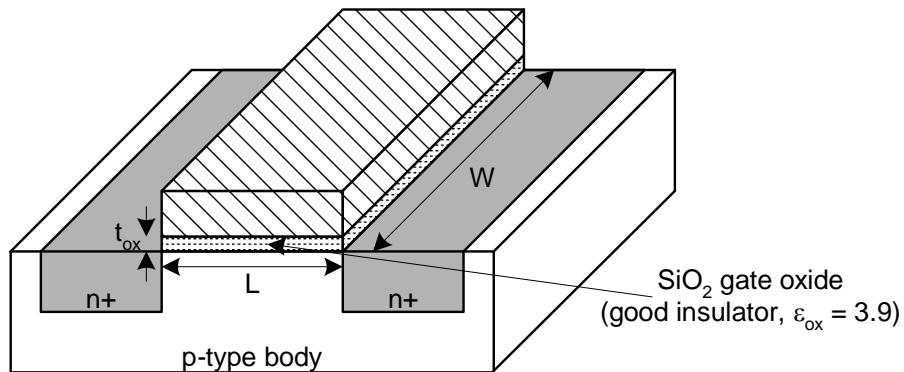
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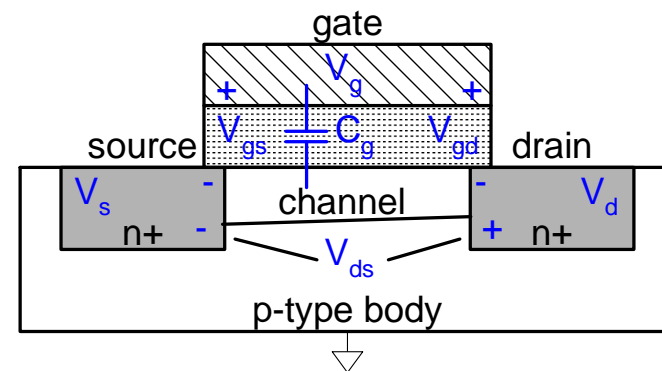
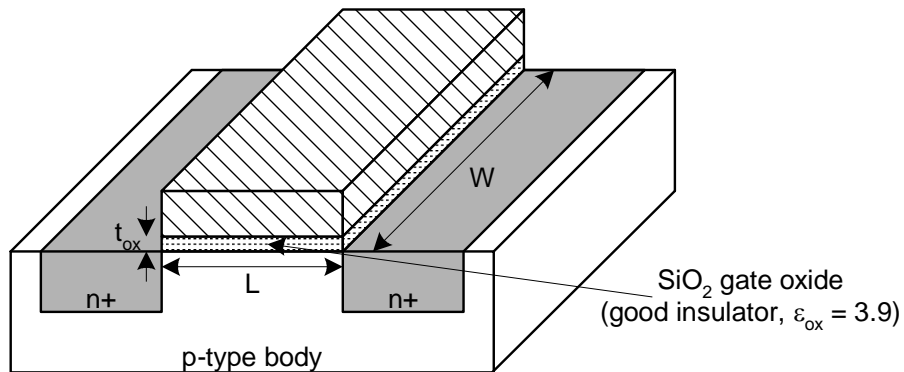
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- ❑  $V = V_{\text{gc}} - V_t = (V_{\text{gs}} - V_{\text{ds}}/2) - V_t$

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  - $t = L / v$

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- Now we know
  - How much charge  $Q_{\text{channel}}$  is in the channel
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$$= \mu C_{\text{ox}} \frac{W}{L} \left( V_{gs} - V_t - \frac{V_{ds}}{2} \right) V_{ds}$$

$$= \beta \left( V_{gs} - V_t - \frac{V_{ds}}{2} \right) V_{ds} \quad \beta = \mu C_{\text{ox}} \frac{W}{L}$$

# nMOS Saturation I-V

- If  $V_{gd} < V_t$ , channel pinches off near drain
  - When  $V_{ds} > V_{dsat} = V_{gs} - V_t$
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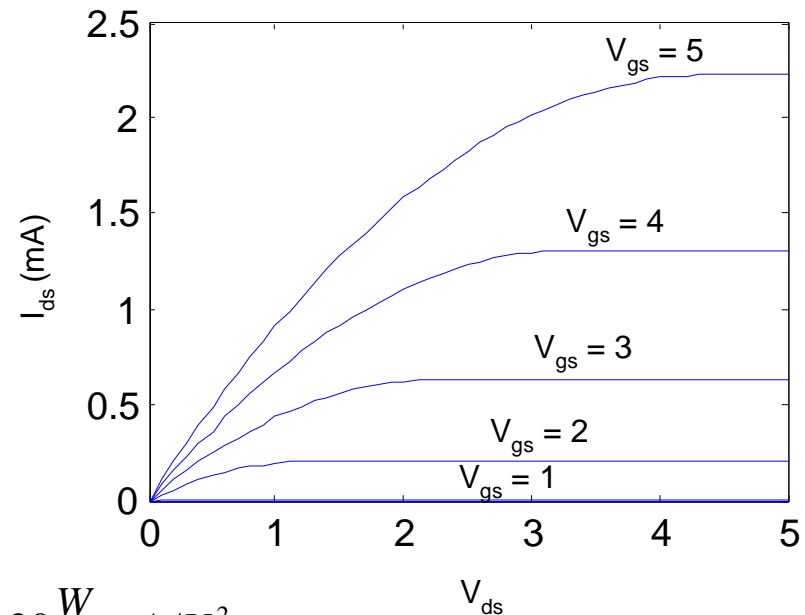
# nMOS I-V Summary

- Shockley 1<sup>st</sup> order transistor models

$$I_{ds} = \begin{cases} 0 & V_{gs} < V_t & \text{cutoff} \\ \beta \left( V_{gs} - V_t - \frac{V_{ds}}{2} \right) V_{ds} & V_{ds} < V_{dsat} & \text{linear} \\ \frac{\beta}{2} (V_{gs} - V_t)^2 & V_{ds} > V_{dsat} & \text{saturation} \end{cases}$$

# Example

- Example: a 0.6  $\mu\text{m}$  process from AMI semiconductor
  - $t_{\text{ox}} = 100 \text{ \AA}$
  - $\mu = 350 \text{ cm}^2/\text{V}^*\text{s}$
  - $V_t = 0.7 \text{ V}$
- Plot  $I_{\text{ds}}$  vs.  $V_{\text{ds}}$ 
  - $V_{\text{gs}} = 0, 1, 2, 3, 4, 5$
  - Use  $W/L = 4/2 \lambda$



$$\beta = \mu C_{\text{ox}} \frac{W}{L} = (350) \left( \frac{3.9 \cdot 8.85 \cdot 10^{-14}}{100 \cdot 10^{-8}} \right) \left( \frac{W}{L} \right) = 120 \frac{W}{L} \mu\text{A}/\text{V}^2$$