

# Mobile Radio Propagation





# Outline

---

- Speed, Wavelength, Frequency
  - Types of Waves
  - Radio Frequency Bands
  - Propagation Mechanisms
  - Radio Propagation Effects
  - Free-Space Propagation
  - Land Propagation
  - Path Loss
  - Fading: Slow Fading / Fast Fading
  - Delay Spread
  - Doppler Shift
  - Co-Channel Interference
  - The Near-Far Problem
  - Digital Wireless Communication System
  - Analog and Digital Signals
  - Modulation Techniques
- 



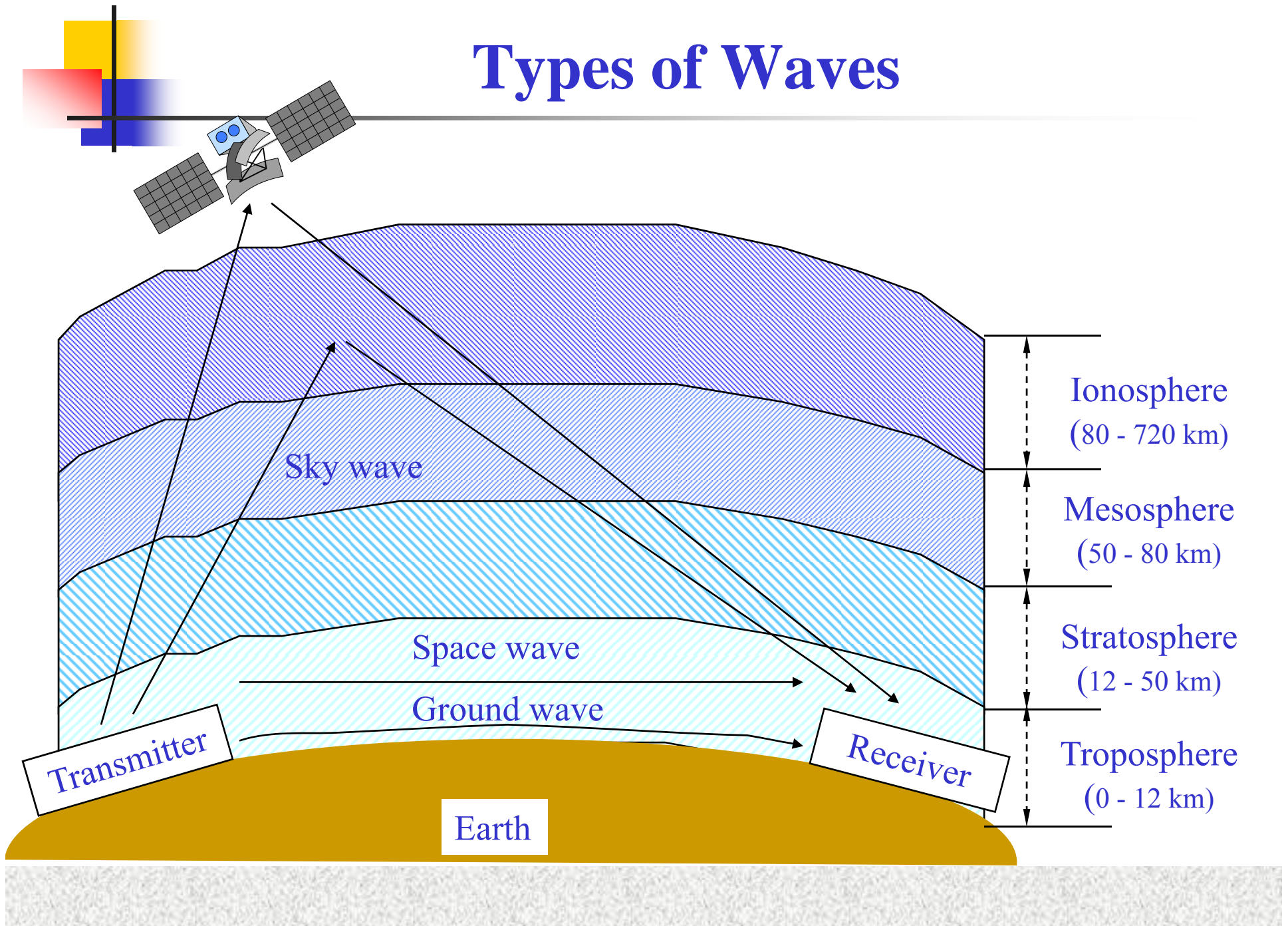
# Speed, Wavelength, Frequency

Light speed = Wavelength x Frequency

$$= 3 \times 10^8 \text{ m/s} = 300,000 \text{ km/s}$$

System	Frequency	Wavelength
AC current	60 Hz	5,000 km
FM radio	100 MHz	3 m
Cellular	800 MHz	37.5 cm
Ka band satellite	20 GHz	15 mm
Ultraviolet light	$10^{15}$ Hz	$10^{-7}$ m

# Types of Waves





# Radio Frequency Bands

Classification Band	Initials	Frequency Range	Characteristics
Extremely low	ELF	< 300 Hz	Ground wave
Infra low	ILF	300 Hz - 3 kHz	
Very low	VLF	3 kHz - 30 kHz	
Low	LF	30 kHz - 300 kHz	
Medium	MF	300 kHz - 3 MHz	Ground/Sky wave
High	HF	3 MHz - 30 MHz	Sky wave
Very high	VHF	30 MHz - 300 MHz	Space wave
Ultra high	UHF	300 MHz - 3 GHz	
Super high	SHF	3 GHz - 30 GHz	
Extremely high	EHF	30 GHz - 300 GHz	
Tremendously high	THF	300 GHz - 3000 GHz	



# Propagation Mechanisms

---

- Reflection

- Propagation wave impinges on an object which is large as compared to wavelength
  - e.g., the surface of the Earth, buildings, walls, etc.

- Diffraction

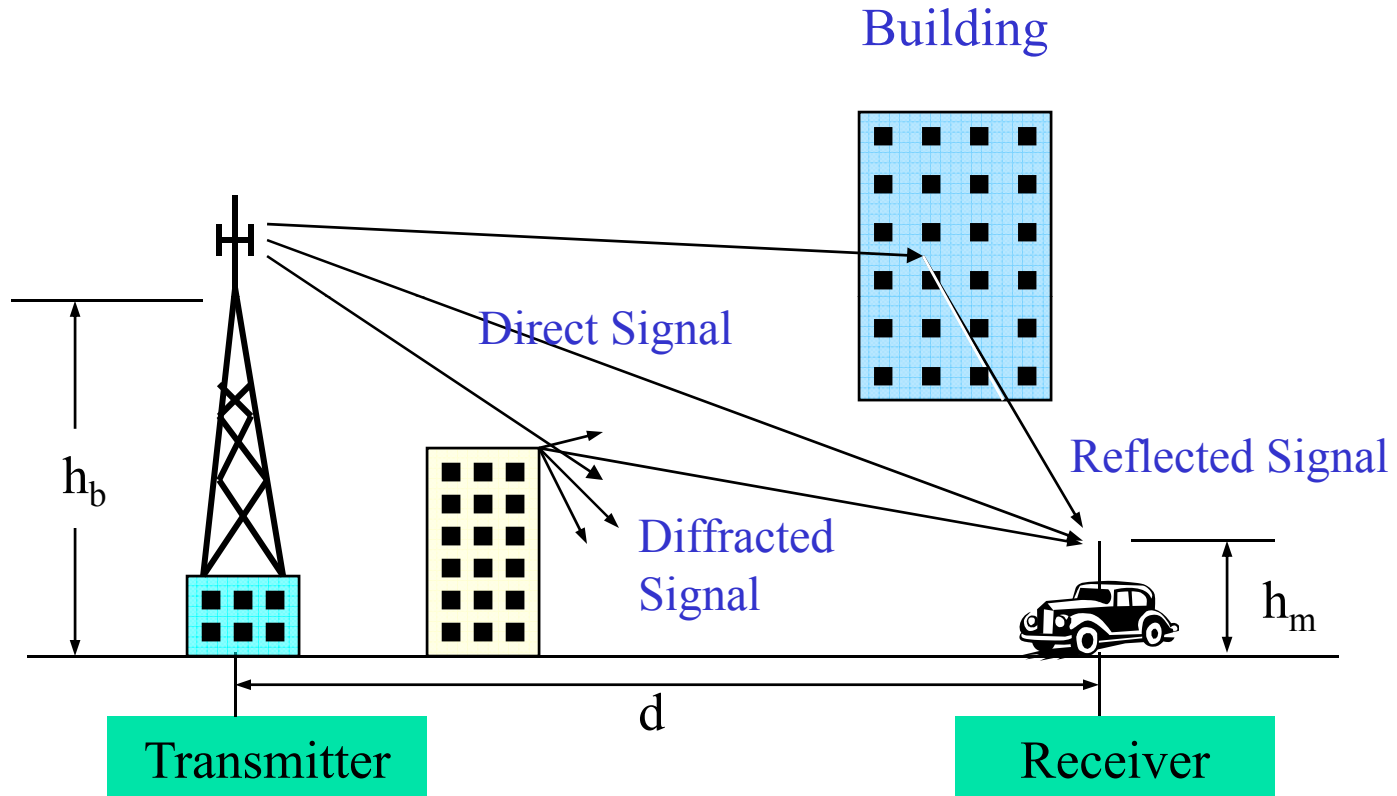
- Radio path between transmitter and receiver obstructed by surface with sharp irregular edges
- Waves bend around the obstacle, even when LOS (line of sight) does not exist

- Scattering

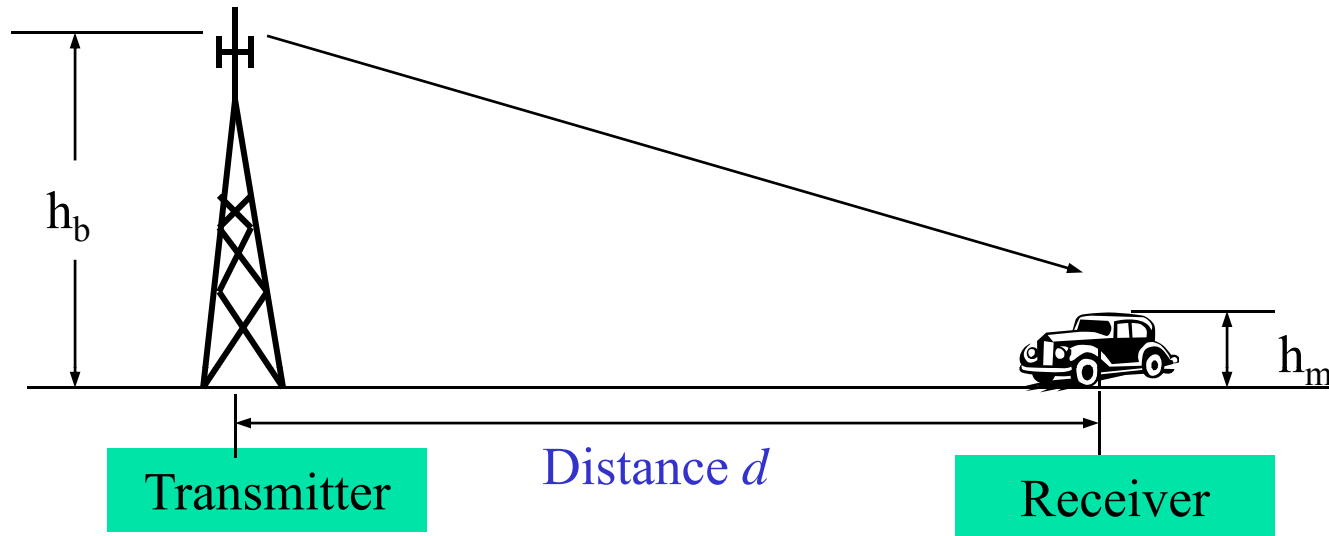
- Objects smaller than the wavelength of the propagation wave
  - e.g. foliage, street signs, lamp posts



# Radio Propagation Effects



# Free-space Propagation



- The received signal power at distance  $d$ :

$$P_r = \frac{A_e G_t P_t}{4\pi d^2}$$

where  $P_t$  is transmitting power,  $A_e$  is effective area, and  $G_t$  is the transmitting antenna gain. Assuming that the radiated power is uniformly distributed over the surface of the sphere.





# Antenna Gain

---

- For a circular reflector antenna

$$\text{Gain } G = \eta (\pi D / \lambda)^2$$

$\eta$  = net efficiency (depends on the electric field distribution over the antenna aperture, losses, ohmic heating, typically 0.55)

$D$  = diameter

thus,  $G = \eta (\pi D f / c)^2$ ,  $c = \lambda f$  ( $c$  is speed of light)

Example:

- Antenna with diameter = 2 m, frequency = 6 GHz, wavelength = 0.05 m  
 $G = 39.4$  dB
- Frequency = 14 GHz, same diameter, wavelength = 0.021 m  
 $G = 46.9$  dB

\* Higher the frequency, higher the gain for the same size antenna



# Land Propagation

---

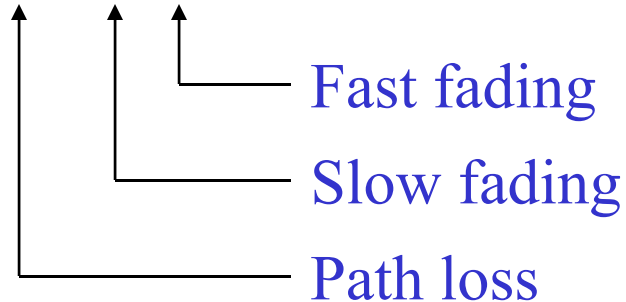
- The received signal power:

$$P_r = \frac{G_t G_r P_t}{L}$$

where  $G_r$  is the receiver antenna gain,

$L$  is the propagation loss in the channel, i.e.,

$$L = L_p L_S L_F$$





# Path Loss (Free-space)

---

- Definition of path loss  $L_P$ :

$$L_P = \frac{P_t}{P_r},$$

Path Loss in Free-space:

$$L_{PF} (dB) = 32.45 + 20 \log_{10} f_c (MHz) + 20 \log_{10} d (km),$$

where  $f_c$  is the carrier frequency.

This shows greater the  $f_c$ , more is the loss.





# Path Loss (Land Propagation)

---

- Simplest Formula:

$$L_p = A d^{-\alpha}$$

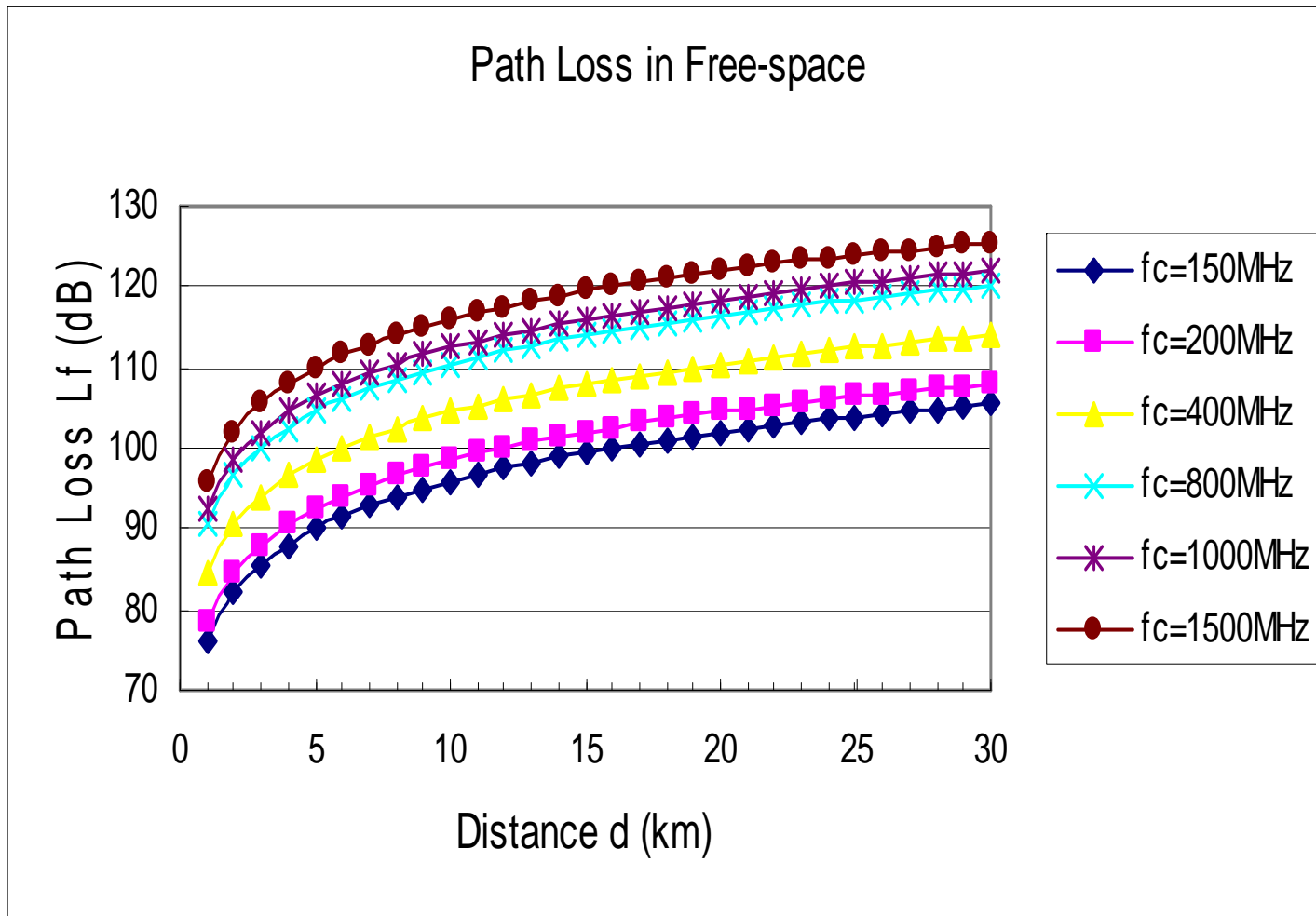
where

$A$  and  $\alpha$ : propagation constants

$d$ : distance between transmitter and receiver

$\alpha$ : value of 3 ~ 4 in typical urban area

# Example of Path Loss (Free-space)





# Path Loss (Urban, Suburban and Open areas)

- Urban area:

$$L_{PU} (dB) = 69.55 + 26.16 \log_{10} f_c (MHz) - 13.82 \log_{10} h_b (m) - \alpha [h_m (m)] \\ + [44.9 - 6.55 \log_{10} h_b (m)] \log_{10} d (km)$$

where

$$\alpha [h_m (m)] = \begin{cases} [1.1 \log_{10} f_c (MHz) - 0.7] h_m (m) - [1.56 \log_{10} f_c (MHz) - 0.8], & \text{for large city} \\ \left. \begin{aligned} &8.29 [\log_{10} 1.54 h_m (m)]^2 - 1.1, & \text{for } f_c \leq 200 MHz \\ &3.2 [\log_{10} 11.75 h_m (m)]^2 - 4.97, & \text{for } f_c \geq 400 MHz \end{aligned} \right\}, & \text{for small \& medium city} \end{cases}$$

- Suburban area:

$$L_{PS} (dB) = L_{PU} (dB) - 2 \left[ \log_{10} \frac{f_c (MHz)}{28} \right]^2 - 5.4$$

- Open area:

$$L_{PO} (dB) = L_{PU} (dB) - 4.78 [\log_{10} f_c (MHz)]^2 + 18.33 \log_{10} f_c (MHz) - 40.94$$

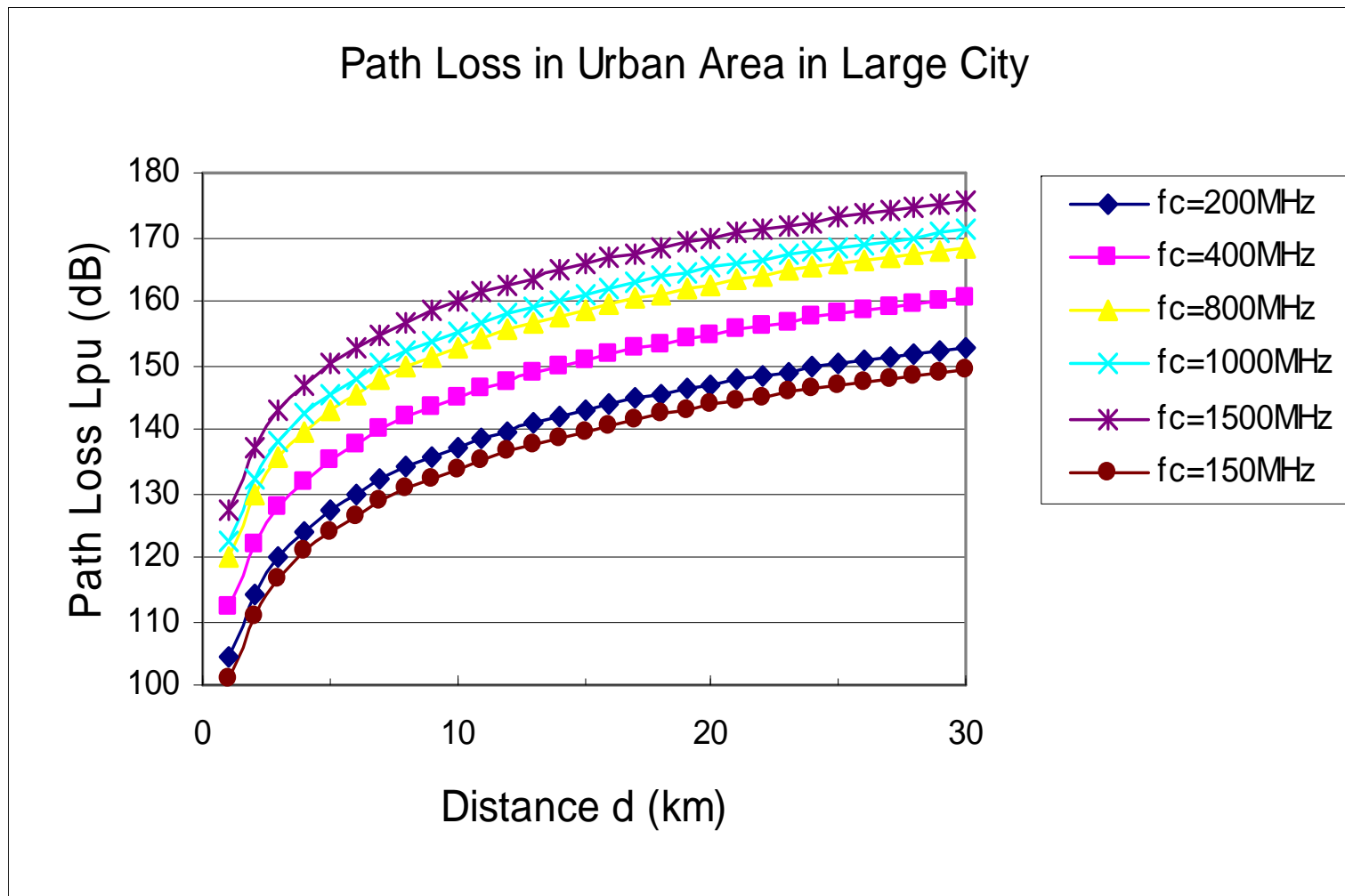



# Path Loss

---

- Path loss in decreasing order:
  - Urban area (large city)
  - Urban area (medium and small city)
  - Suburban area
  - Open area

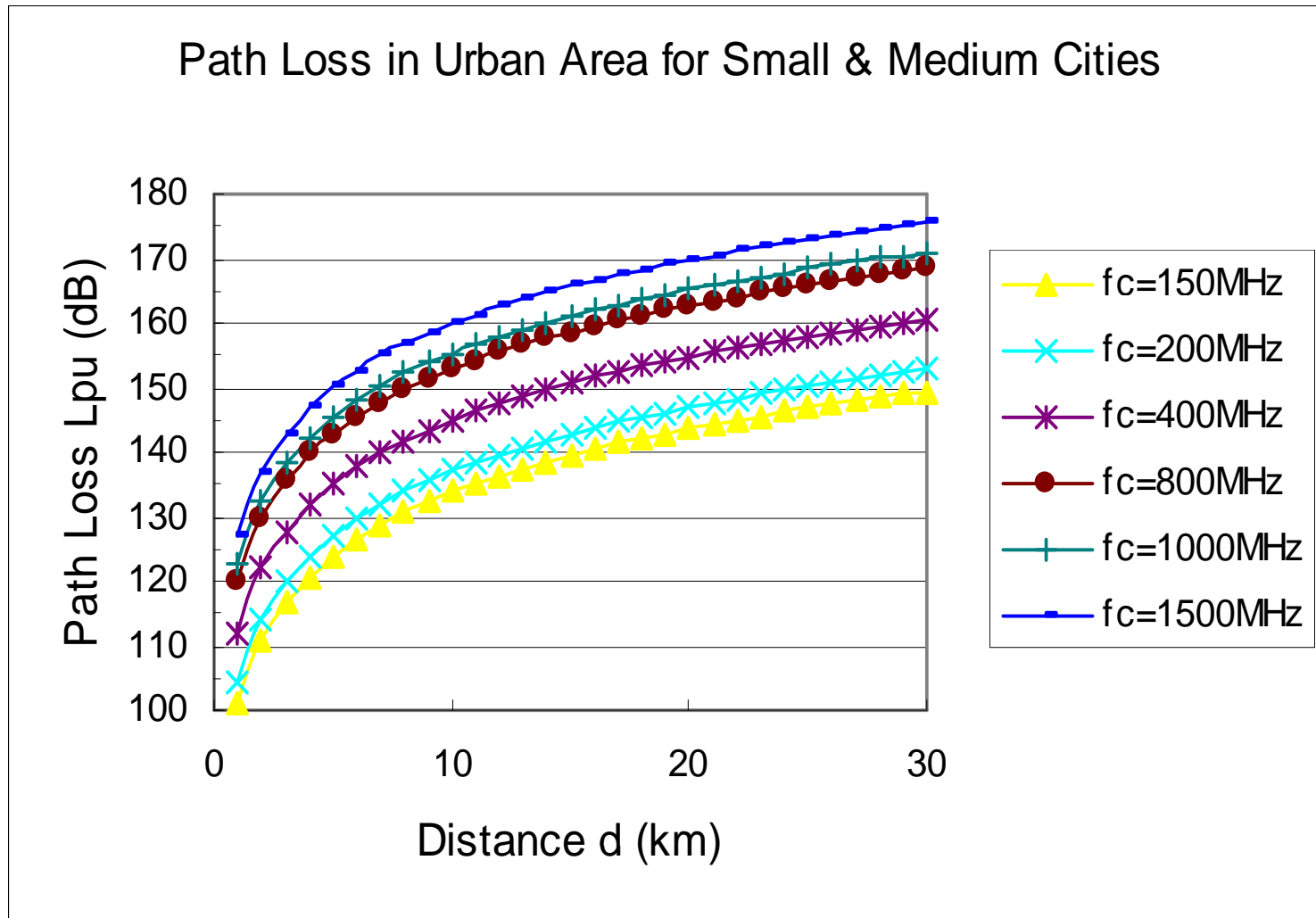
# Example of Path Loss (Urban Area: Large City)



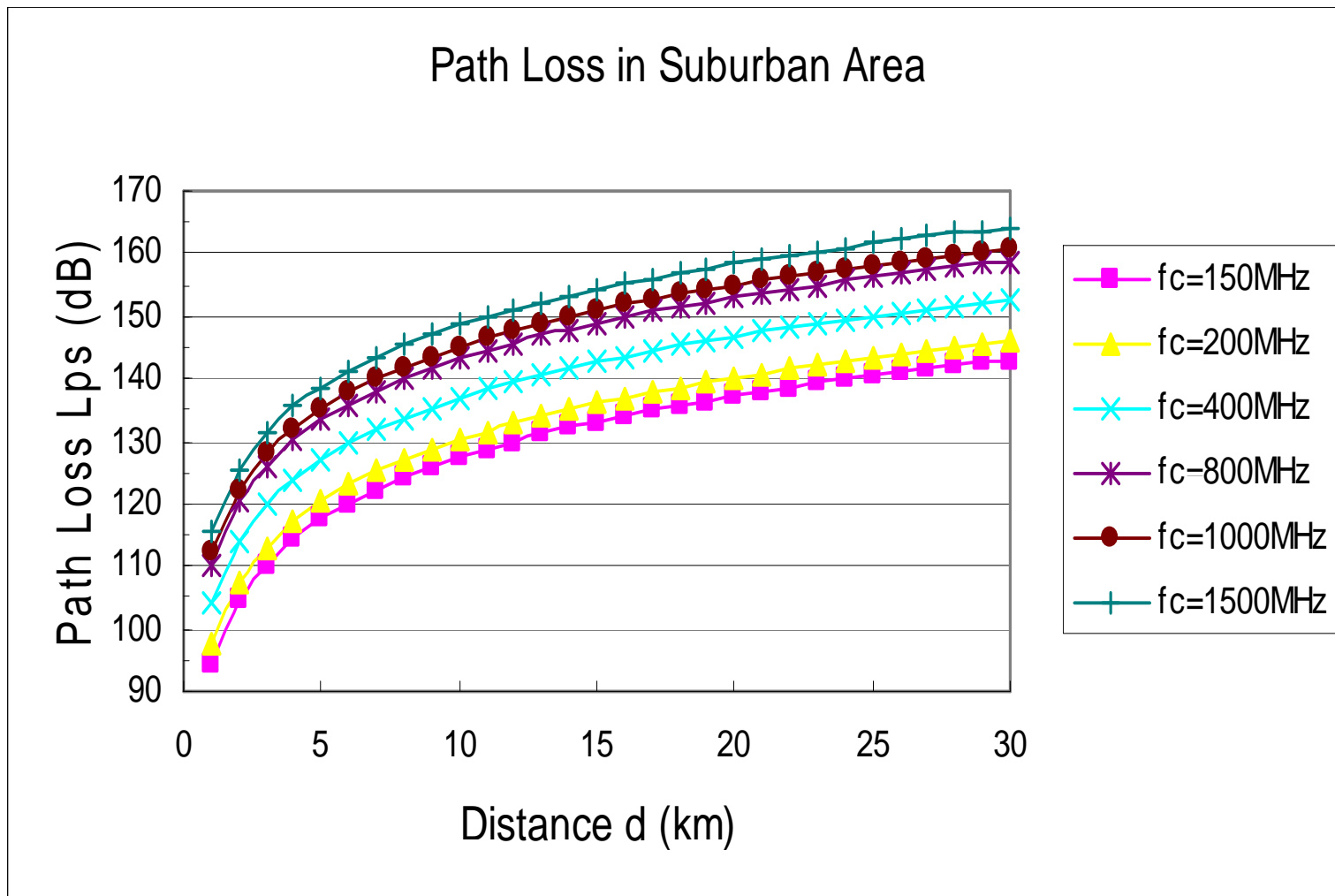


# Example of Path Loss

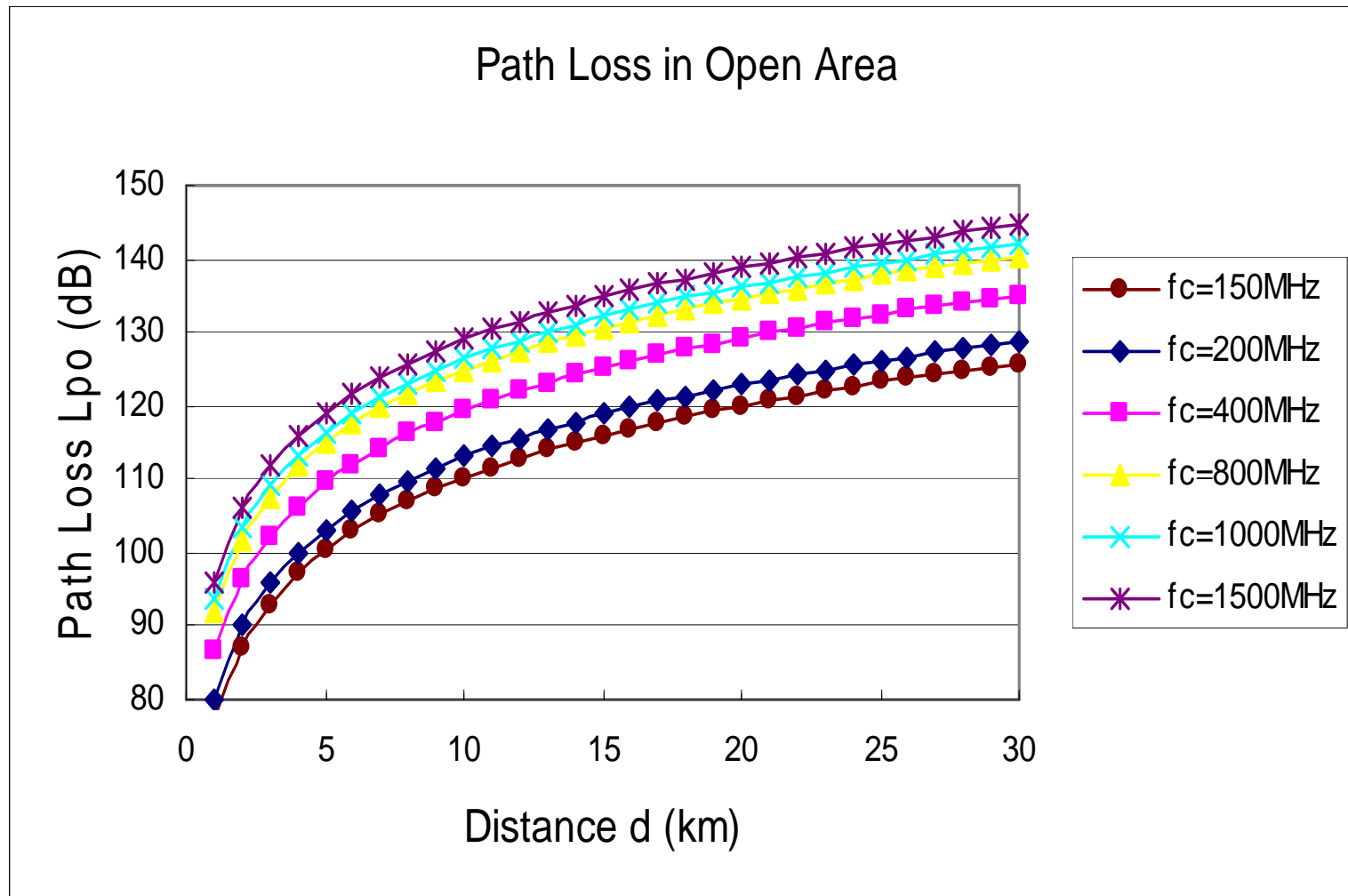
## (Urban Area: Medium and Small Cities)



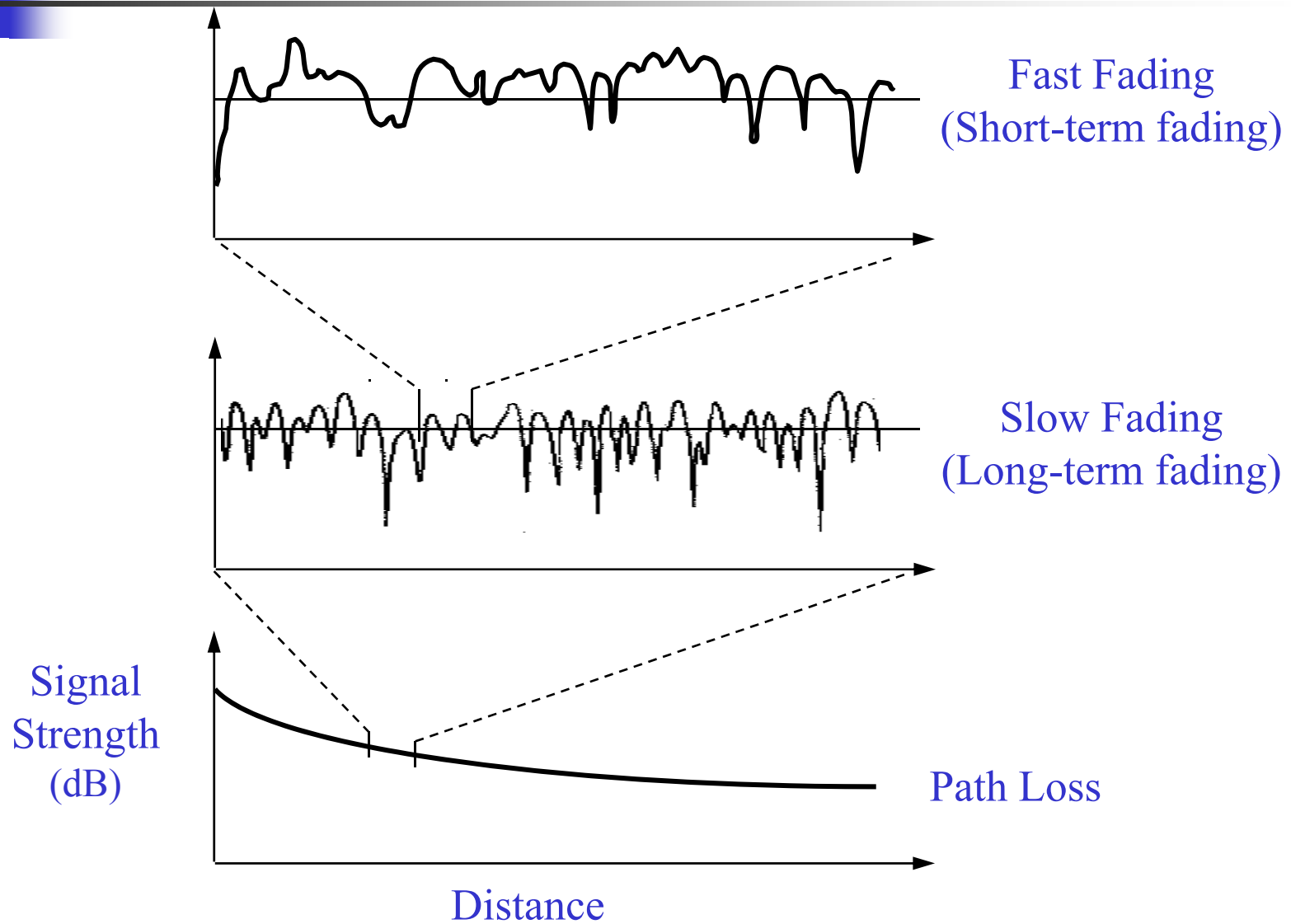
# Example of Path Loss (Suburban Area)



# Example of Path Loss (Open Area)



# Fading





# Slow Fading

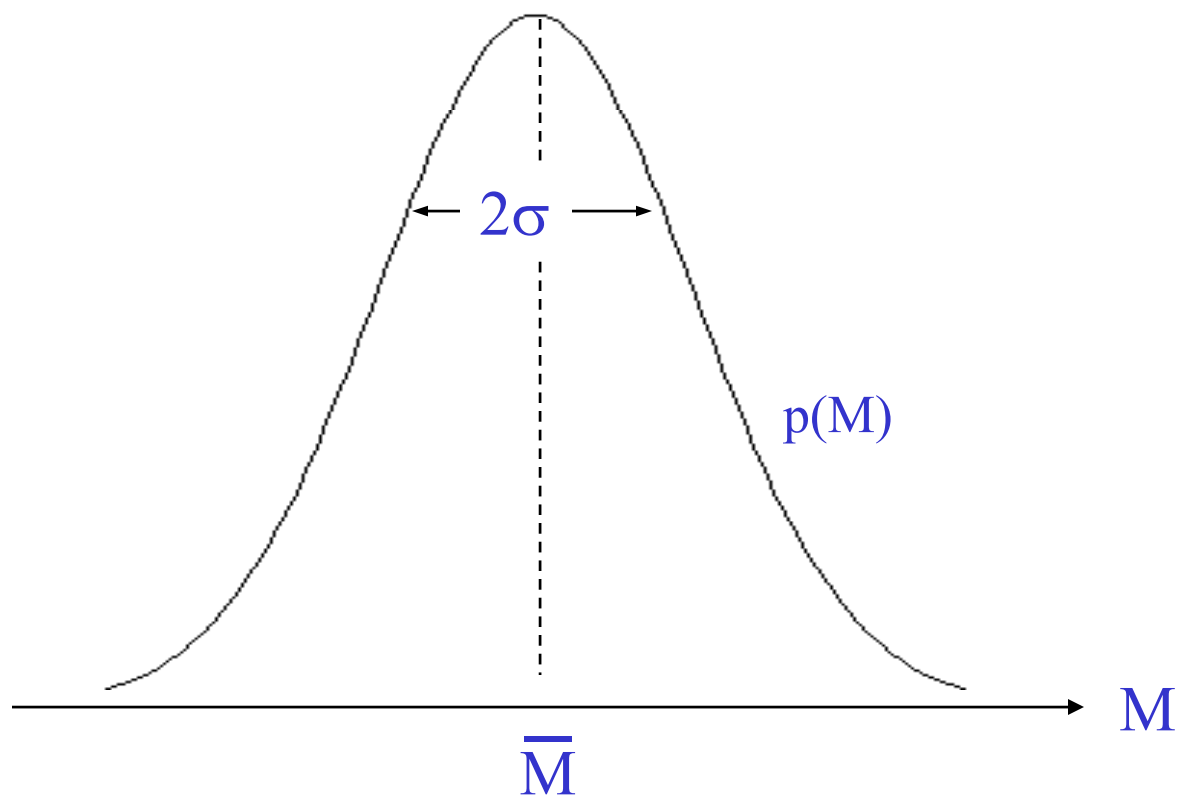
---

- The long-term variation in the mean level is known as slow fading (shadowing or log-normal fading). This fading caused by shadowing.
- Log-normal distribution:
  - The pdf of the received signal level is given in decibels by

$$p(M) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(M-\bar{M})^2}{2\sigma^2}},$$

where  $M$  is the true received signal level  $m$  in decibels, i.e.,  $10\log_{10}m$ ,  
 $\bar{M}$  is the area average signal level, i.e., the mean of  $M$ ,  
 $\sigma$  is the standard deviation in decibels

# Log-normal Distribution



The pdf of the received signal level



# Fast Fading

---

- The signal from the transmitter may be reflected from objects such as hills, buildings, or vehicles.
  - When MS far from BS, the envelope distribution of received signal is Rayleigh distribution. The pdf is

$$p(r) = \frac{r}{\sigma^2} e^{-\frac{r^2}{2\sigma^2}}, \quad r > 0$$

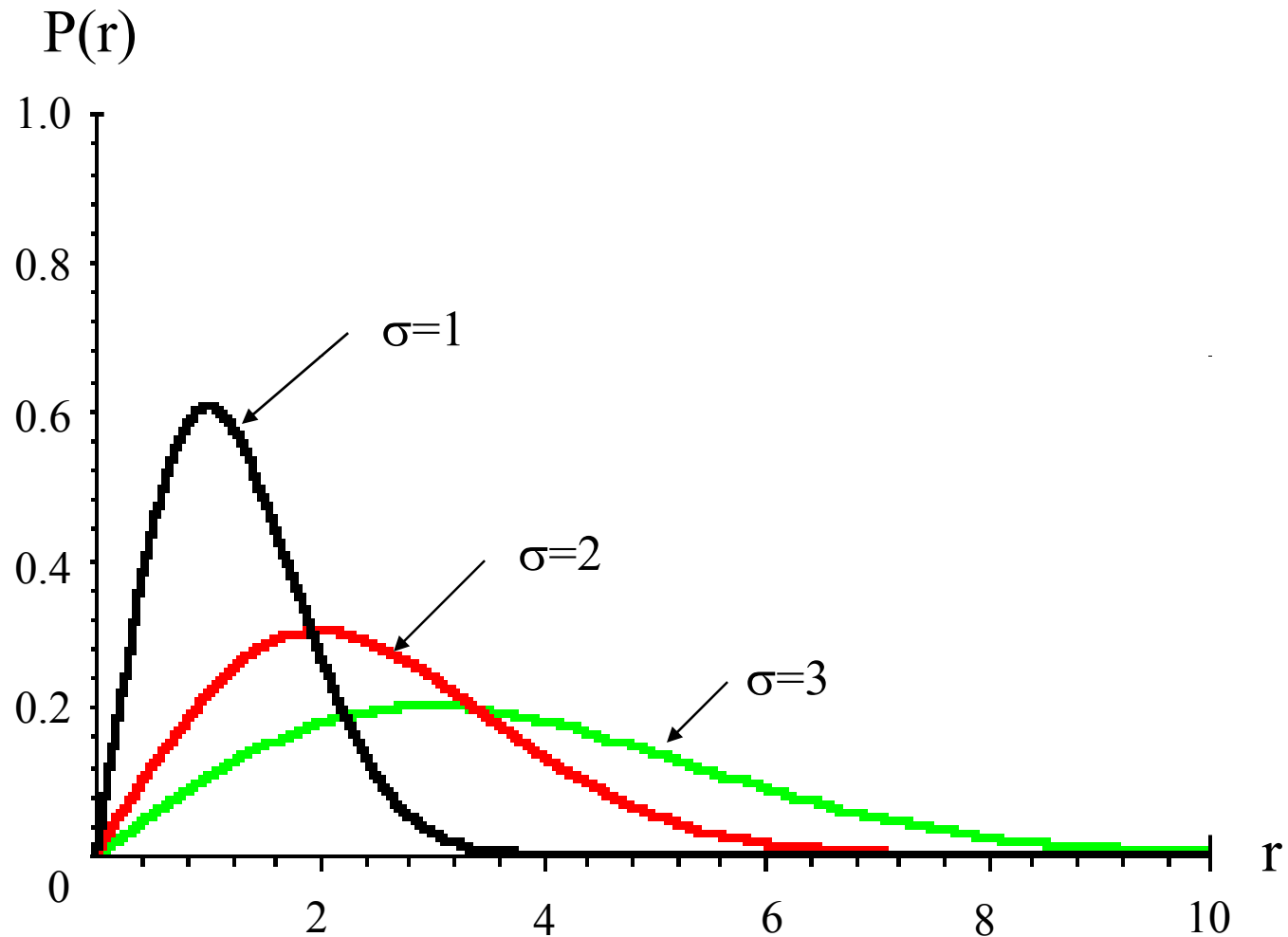
where  $\sigma$  is the standard deviation.

- Middle value  $r_m$  of envelope signal within sample range to be satisfied by

$$P(r \leq r_m) = 0.5.$$

- We have  $r_m = 1.777$ ♦
- 

# Rayleigh Distribution



The pdf of the envelope variation





## Fast Fading (Continued)

---

- When MS far from BS, the envelope distribution of received signal is Rician distribution. The pdf is

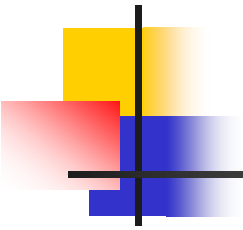
$$p(r) = \frac{r}{\sigma^2} e^{-\frac{r^2 + \alpha^2}{2\sigma^2}} I_0\left(\frac{r\alpha}{\sigma}\right), \quad r \geq 0$$

where

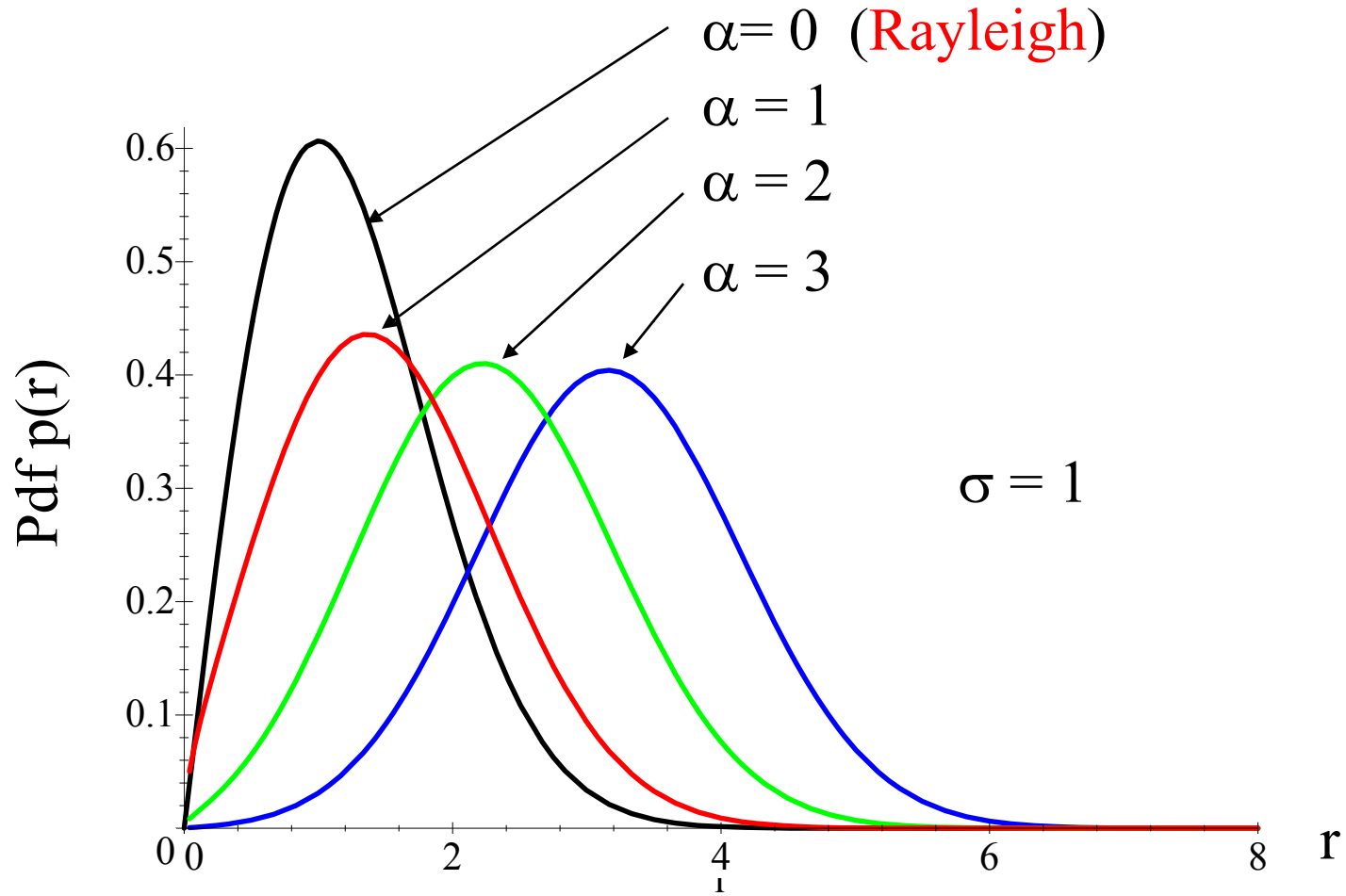
$\sigma$  is the standard deviation,

$I_0(x)$  is the zero-order Bessel function of the first kind,

$\alpha$  is the amplitude of the direct signal



# Rician Distribution



The pdf of the envelope variation





# Characteristics of Instantaneous Amplitude

---

- Level Crossing Rate:
  - Average number of times per second that the signal envelope crosses the level in positive going direction.
- Fading Rate:
  - Number of times signal envelope crosses middle value in positive going direction per unit time.
- Depth of Fading:
  - Ratio of mean square value and minimum value of fading signal.
- Fading Duration:
  - Time for which signal is below given threshold.

# Doppler Shift

- Doppler Effect: When a wave source and a receiver are moving towards each other, the frequency of the received signal will not be the same as the source.
  - When they are moving toward each other, the frequency of the received signal is higher than the source.
  - When they are opposing each other, the frequency decreases.

Thus, the frequency of the received signal is

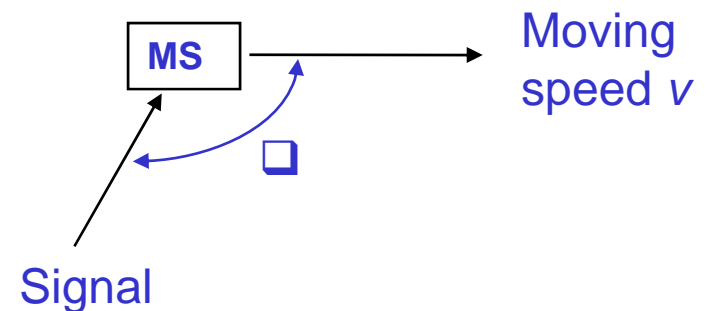
$$f_R = f_C - f_D$$

where  $f_C$  is the frequency of source carrier,  
 $f_D$  is the Doppler frequency.

- Doppler Shift in frequency:

$$f_D = \frac{v}{\lambda} \cos \theta$$


where  $v$  is the moving speed,  
 $\lambda$  is the wavelength of carrier.

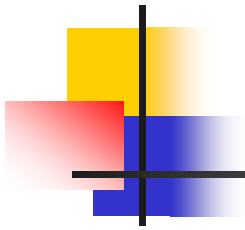




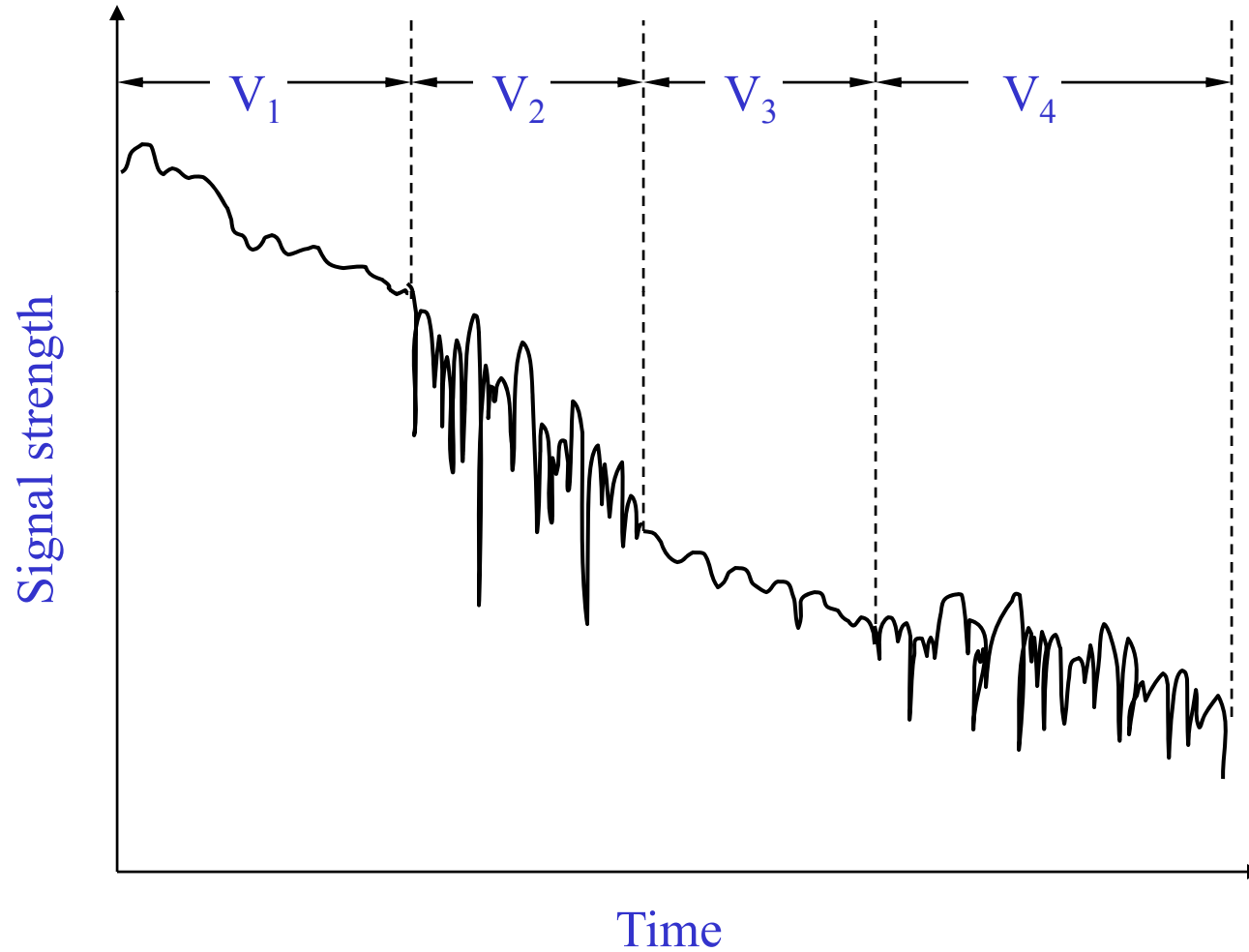
# Delay Spread

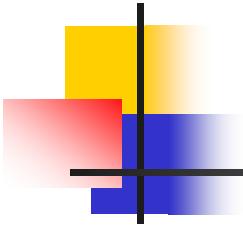
---

- When a signal propagates from a transmitter to a receiver, signal suffers one or more reflections.
  - This forces signal to follow different paths.
  - Each path has different path length, so the time of arrival for each path is different.
  - This effect which spreads out the signal is called “Delay Spread”.
- 

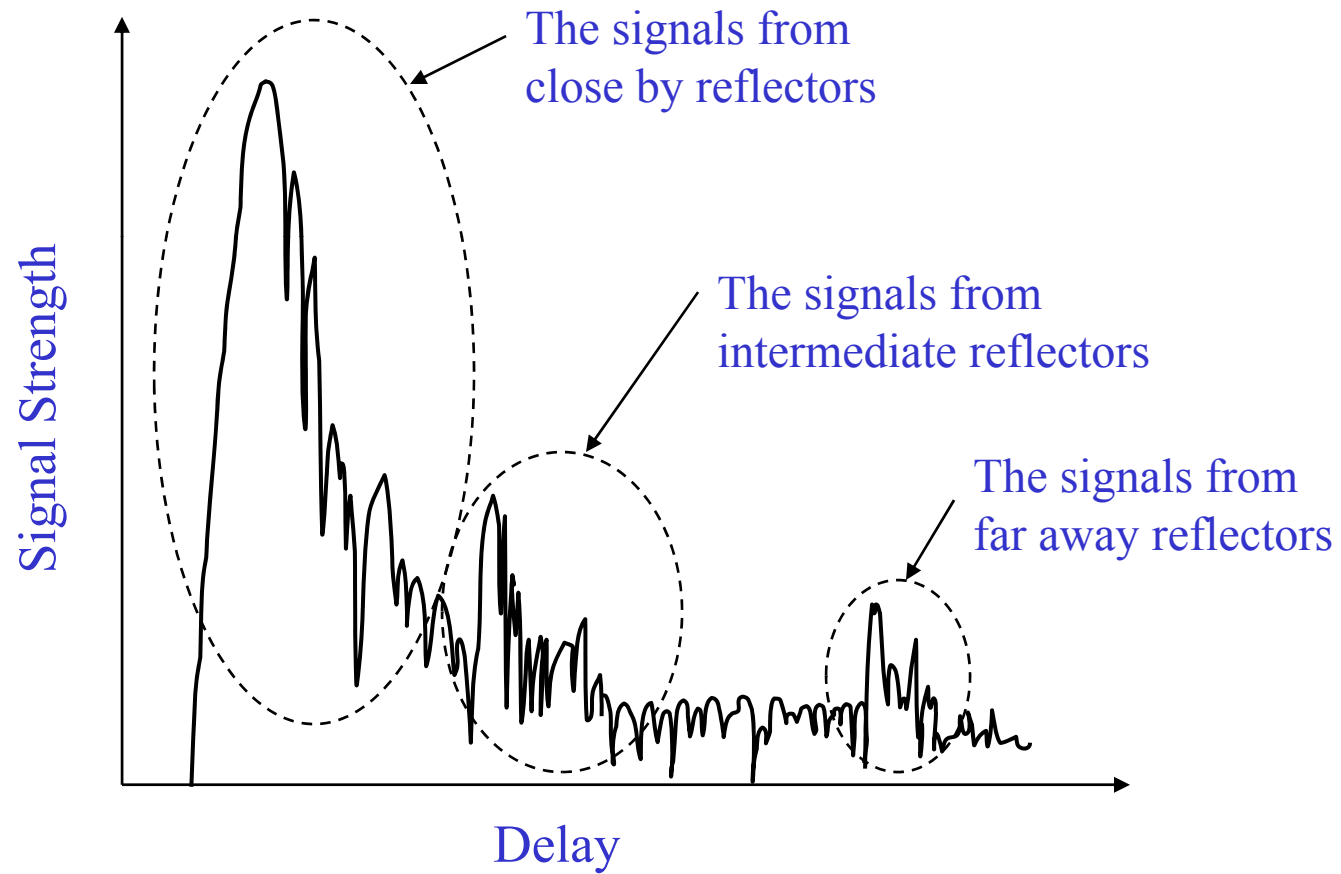


# Moving Speed Effect





# Delay Spread





# Intersymbol Interference (ISI)

---

- Caused by time delayed multipath signals
- Has impact on burst error rate of channel
- Second multipath is delayed and is received during next symbol
- For low bit-error-rate (BER)

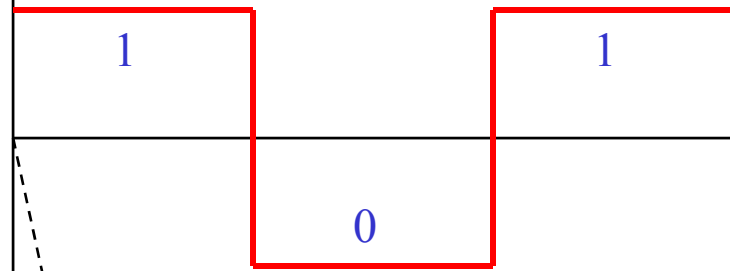
$$R < \frac{1}{2\tau_d}$$

- $R$  (digital transmission rate) limited by delay spread  $\tau_d$ .



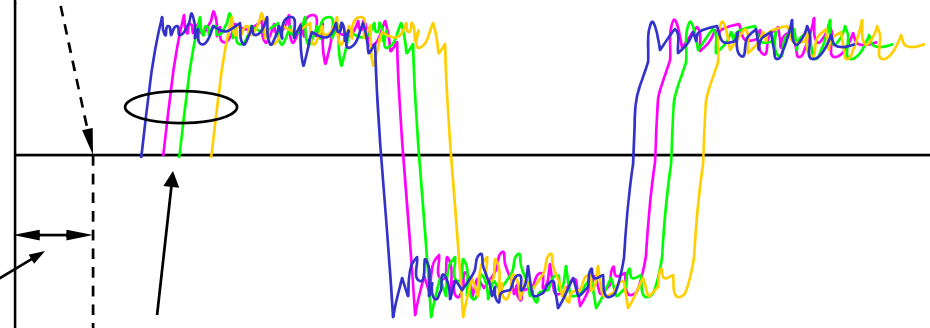
# Intersymbol Interference (ISI)

Transmission  
signal



Time

Received signal  
(short delay)



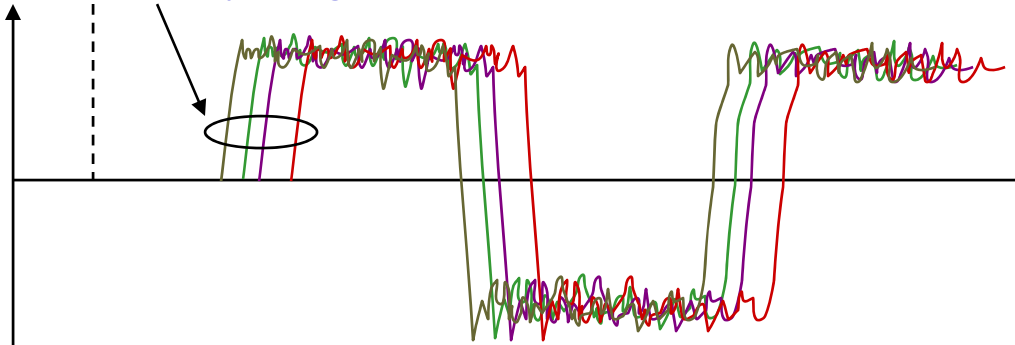
Time

Propagation time



Delayed signals

Received signal  
(long delay)



Time





# Coherence Bandwidth

---

- Coherence bandwidth  $B_c$ :
  - Represents correlation between 2 fading signal envelopes at frequencies  $f_1$  and  $f_2$ .
  - Is a function of delay spread.
  - Two frequencies that are larger than coherence bandwidth fade independently.
  - Concept useful in diversity reception
    - Multiple copies of same message are sent using different frequencies.



# Cochannel Interference

---

- Cells having the same frequency interfere with each other.
- $r_d$  is the desired signal
- $r_u$  is the interfering undesired signal
- $\beta$  is the protection ratio for which  
 $r_d \leq \beta r_u$  (so that the signals interfere the least)
- If  $P(r_d \leq \beta r_u)$  is the probability that  $r_d \leq \beta r_u$ ,  
Cochannel probability  $P_{co} = P(r_d \leq \beta r_u)$