



ANTENNAS , WAVE PROPAGATION &TV ENGG



Topics to be covered

- Radiation from a small current element

RADIATION FROM A SMALL CURRENT ELEMENT

- An alternating current element or oscillating current dipole possesses electromagnetic field.
- We will find these fields everywhere around using the concept of Retard Vector Potential.

- Let the elemental length ($d\mathbf{l}$) of the wire be placed at the origin of the spherical coordinate and I be current flowing through it as shown in the figure 2.20.
- The length is so short that current is constant along the length.

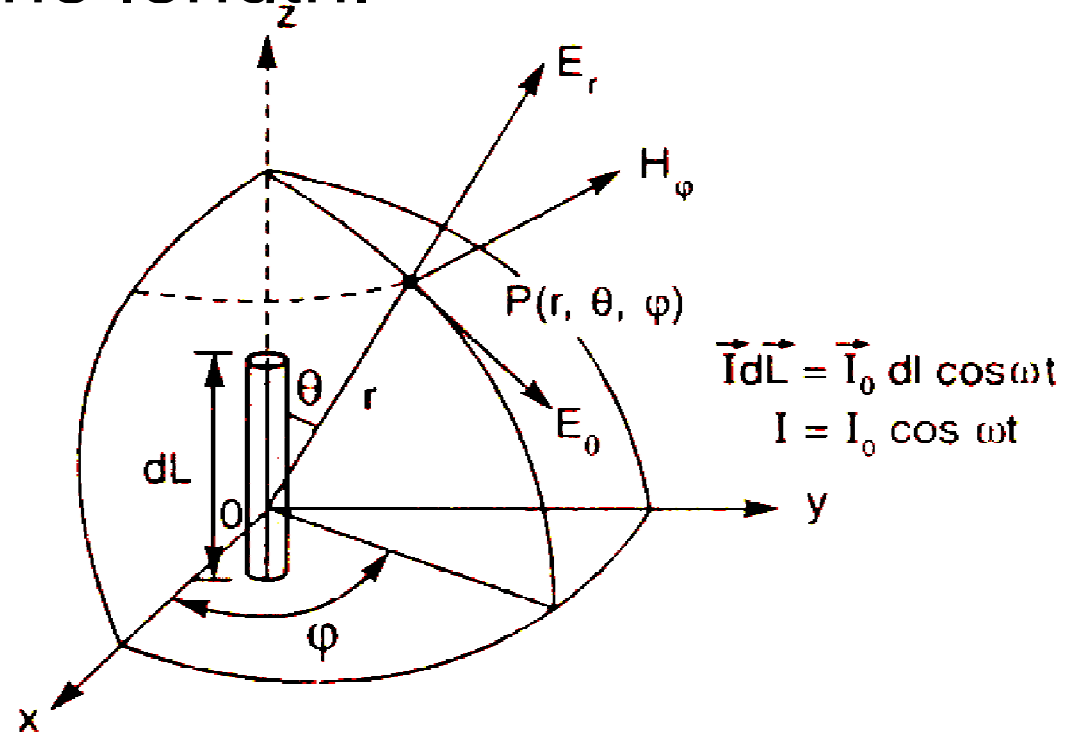


Fig. 2.20. Current element ($d\mathbf{l}$) at the origin of sphere

Magnetic Field Components

- To find the electromagnetic field at any arbitrary point $P(r, \theta, \phi)$, first we will calculate the vector potential $\vec{\mathbf{A}}$
- The general expression for magnetic vector potential is given by

$$\vec{\mathbf{A}}(r) = \frac{\mu}{4\pi} \int \frac{\vec{\mathbf{J}}\left(t - \frac{r}{c}\right)}{r} dv \dots(2.169)$$

- The vector potential \vec{A} is acting along z direction so it will have only z component
e.g., A_z retarded in time by (r/c) seconds.

- Since the current element is excited by the current $I = I_0 \cos \omega t$, so $\int_V \vec{J} dv$ in Eqn. (2.169) may be replaced by $I d\vec{l}$

thus

$$\begin{aligned} \vec{A}_z &= \frac{\mu}{4\pi} \int \frac{I_0 dL \cos \omega \left(t - \frac{r}{c} \right)}{r} \\ A_z &= \frac{\mu}{4\pi} \int_V \frac{\vec{J} \left(t - \frac{r}{c} \right) dv}{r} \\ &= \frac{\mu}{4\pi} \int_V \frac{\vec{J} \left(t - \frac{r}{c} \right) d\vec{s} d\vec{l}}{r} = \frac{\mu}{4\pi} \int \frac{I \left(t - \frac{r}{c} \right)}{r} \end{aligned} \quad \dots(2.170)$$