

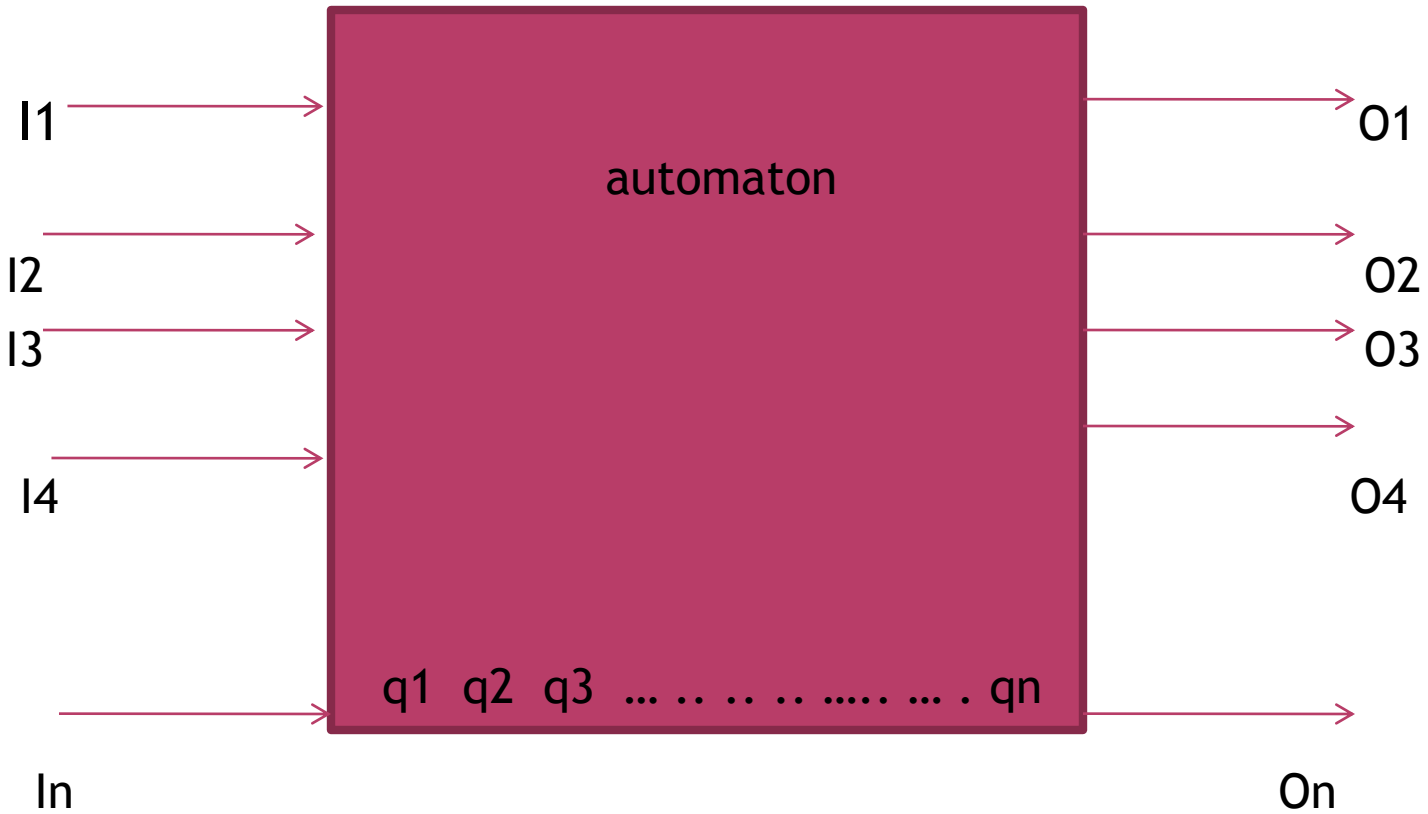
**COURSE:
THEORY OF
AUTOMATA
COMPUTATION**

TOPICS TO BE COVERED

- ◉ Definition Of an automata
- ◉ Finite Automaton
- ◉ State(transition) Diagram

DEFINITION OF AN AUTOMATON

- ⦿ An automaton is a system where energy, material and information are transformed, transmitted and used for performing some function without direct participation of man.



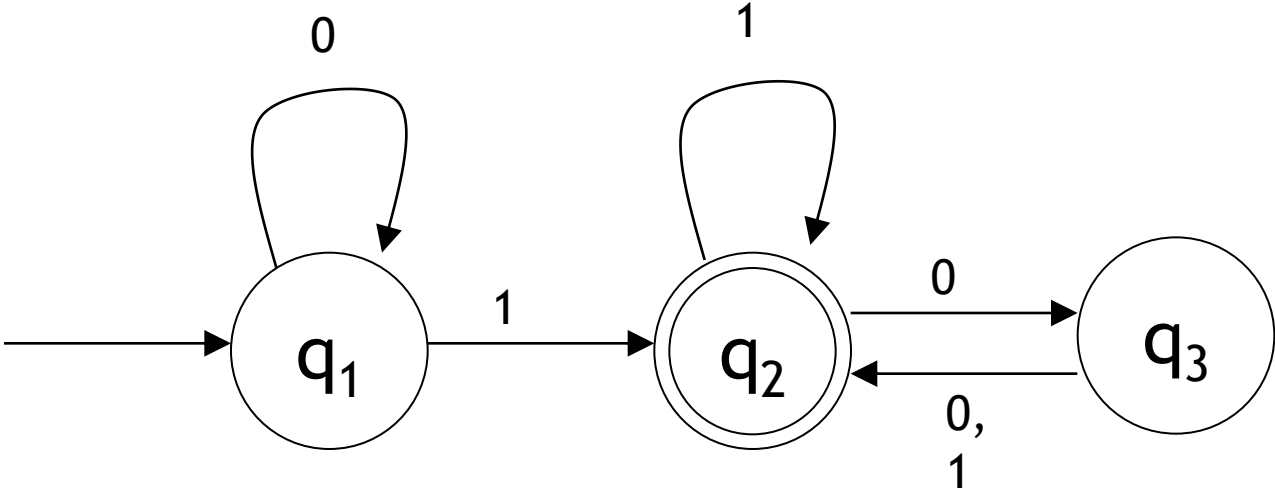
- ⦿ Input
- ⦿ Output
- ⦿ State
- ⦿ State Relation
- ⦿ Output Relation

FINITE AUTOMATON

A *finite automaton* is a 5 - tuple $(Q, \Sigma, \delta, q_0, F)$, where

1. Q is a finite set called the *states* ,
2. Σ is a finite set called the *alphabet*,
3. $\delta : Q \times \Sigma \rightarrow Q$ is the *transition function*,
4. $q_0 \in Q$ is the *start state* , and
5. $F \subseteq Q$ is the *set of accept states* .

STATE(TRANSITION) DIAGRAM



DATA REPRESENTATION

1. $Q = \{q_1, q_2, q_3\}$

2. $\Sigma = \{0, 1\}$

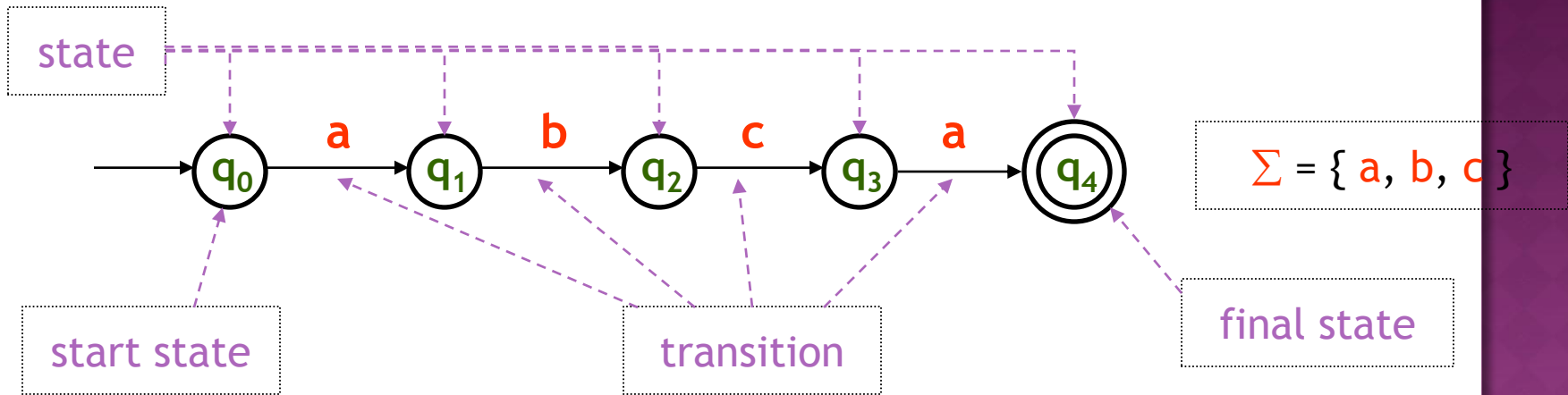
3. δ is described as

	0	1
q_1	q_1	q_2
q_2	q_3	q_2
q_3	q_2	q_2

4. q_1 is the start state, and

5. $F = \{q_2\}$.

FINITE-STATE AUTOMATA



- **Representation**

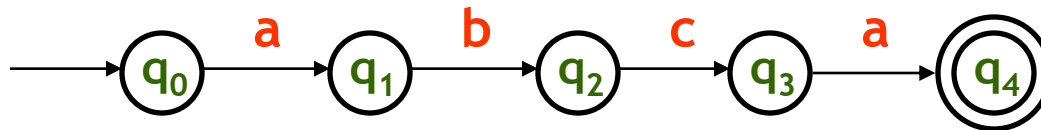
(continued)

- An FSA may also be represented with a **state-transition table**. The table for the above FSA:

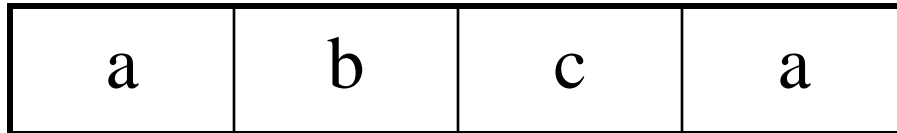
State	Input		
	a	b	c
0	1	\emptyset	\emptyset
1	\emptyset	2	\emptyset
2	\emptyset	\emptyset	3
3	4	\emptyset	\emptyset
4	\emptyset	\emptyset	\emptyset

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



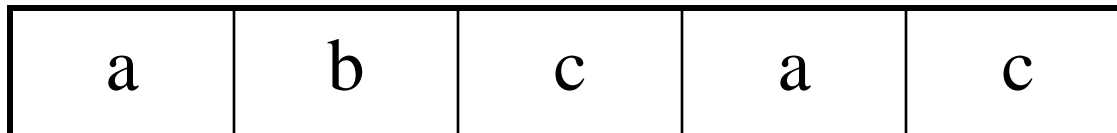
IS₁:



IS₂:



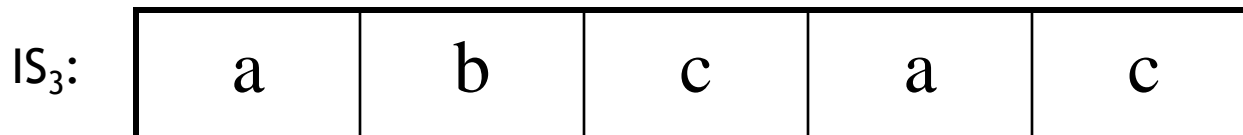
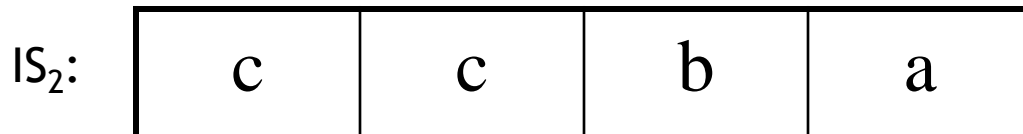
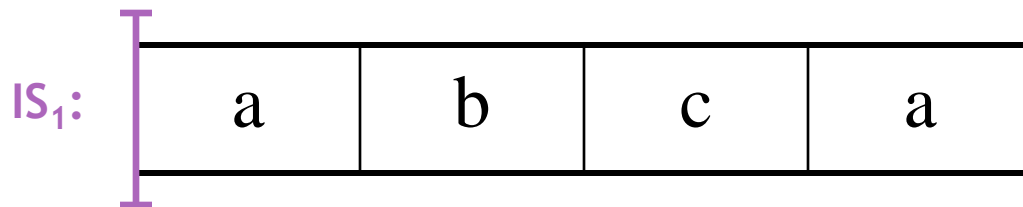
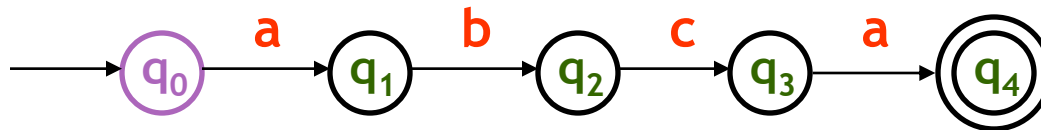
IS₃:



State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

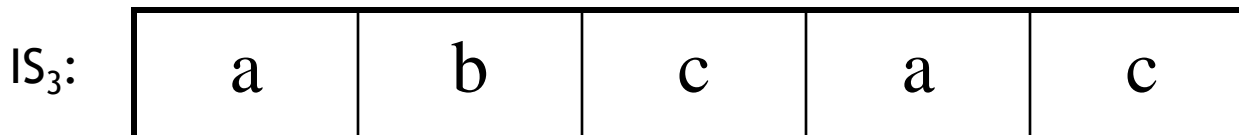
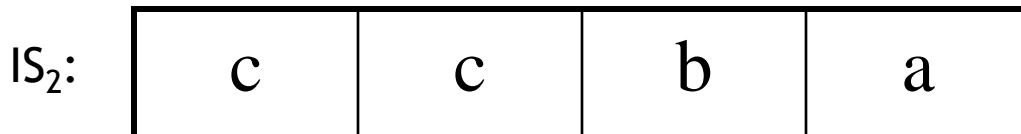
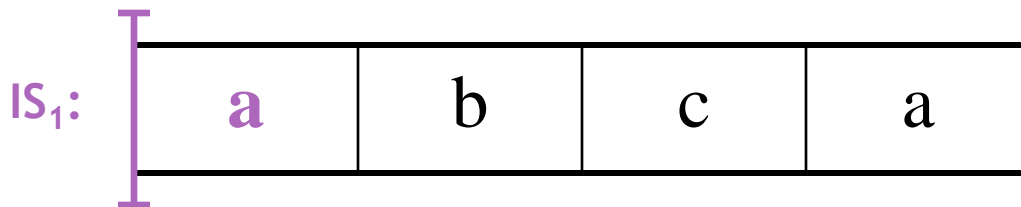
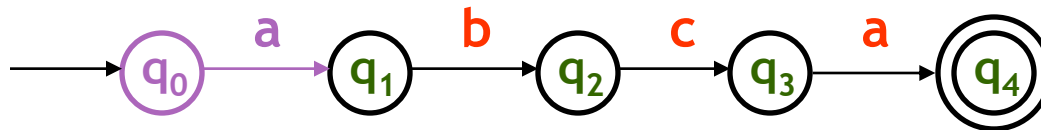
$$\Sigma = \{ a, b, c \}$$



State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

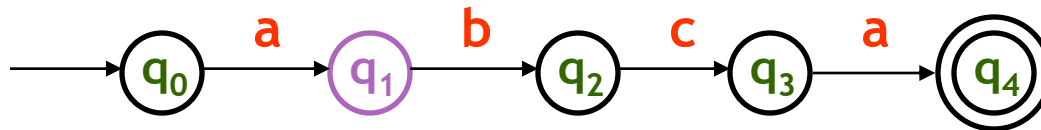
$$\Sigma = \{ a, b, c \}$$



State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



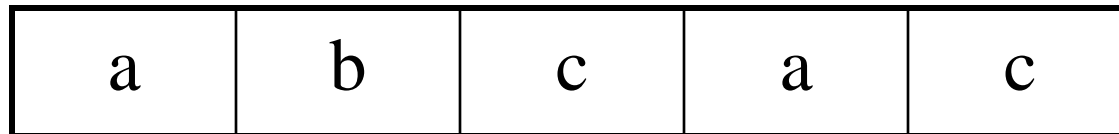
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IS₂:



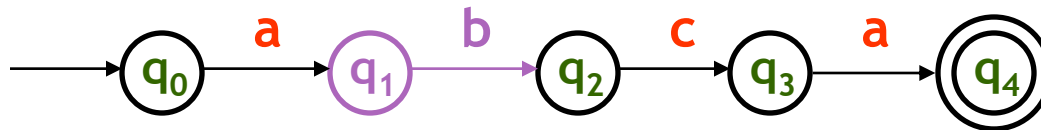
IS₃:



State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



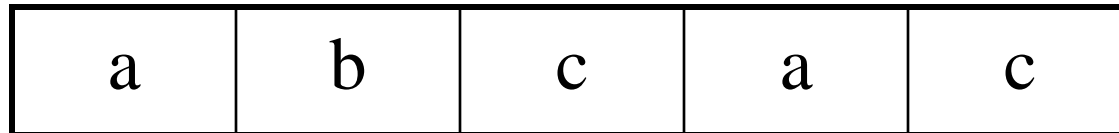
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IS₂:



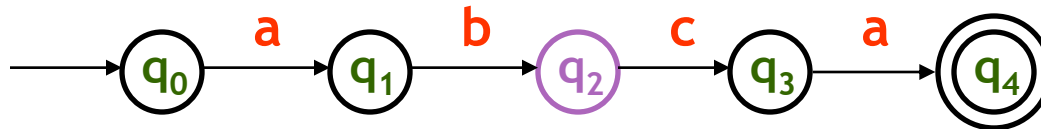
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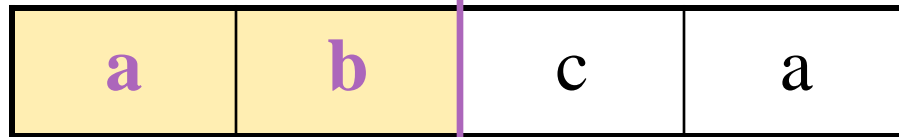
State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



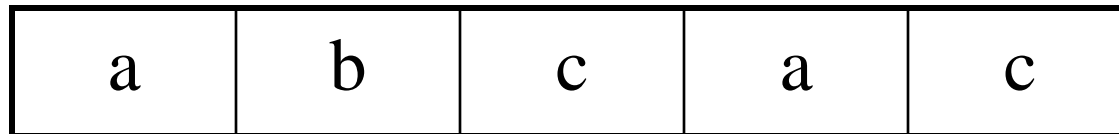
IS₁:



IS₂:



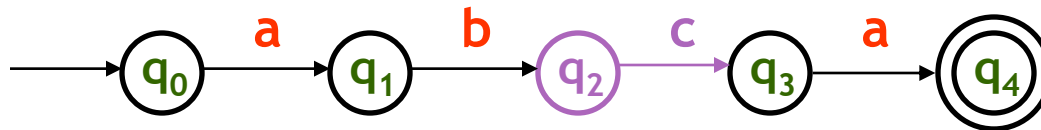
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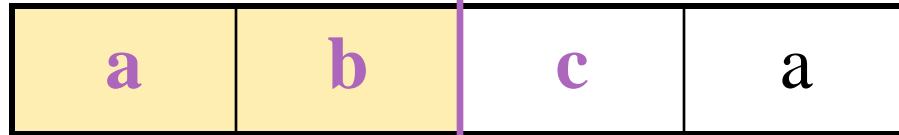
State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



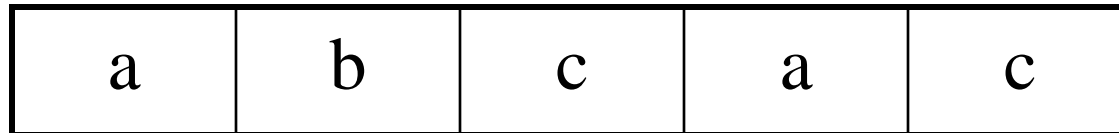
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IS₂:



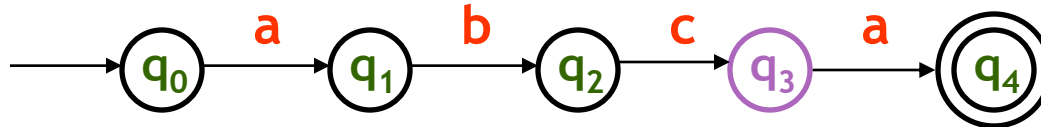
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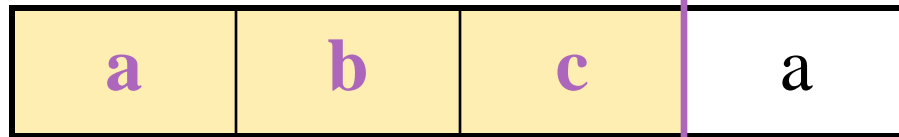
State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



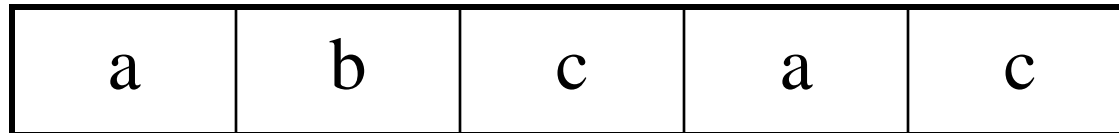
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IS₂:



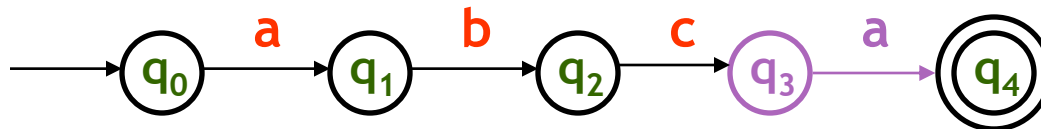
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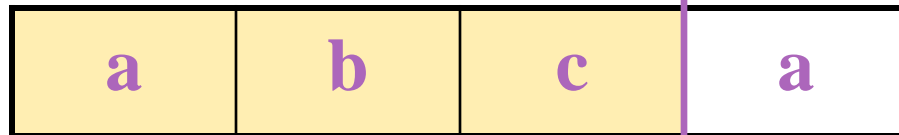
State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



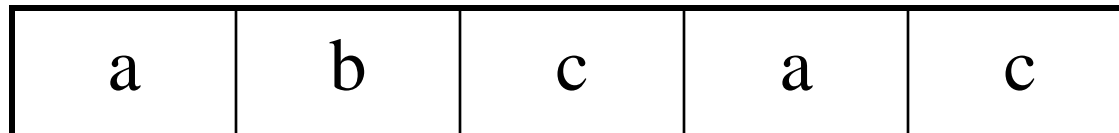
IS₁:



IS₂:



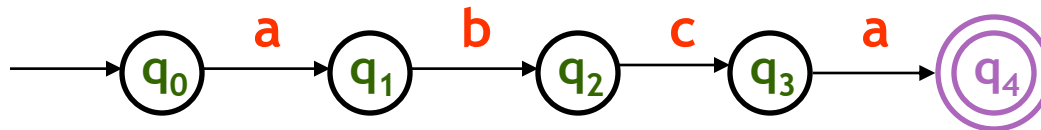
IS₃:



State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

$$\Sigma = \{ a, b, c \}$$



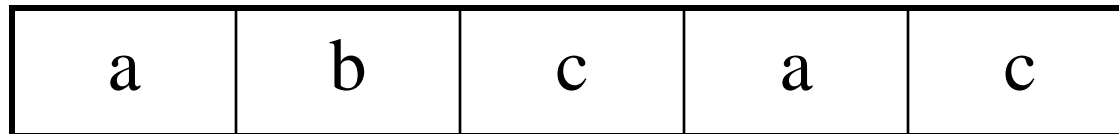
IS₁:



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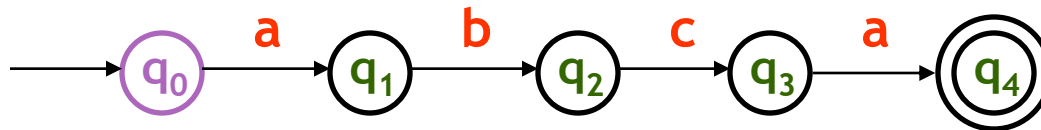
IS₃:



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	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅

FINITE-STATE AUTOMATA

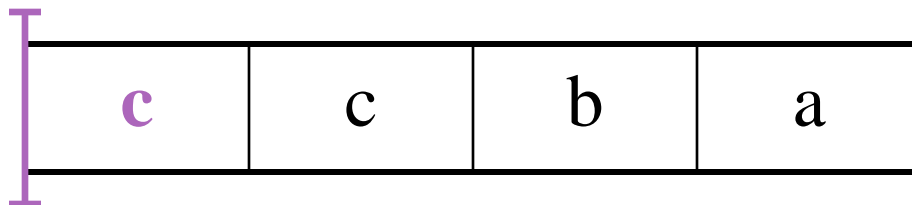
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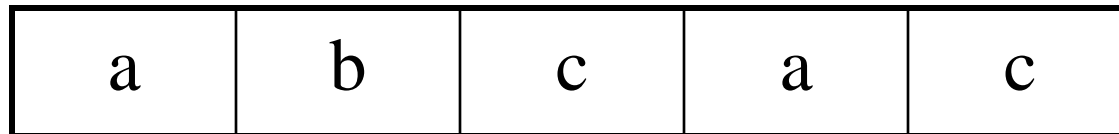
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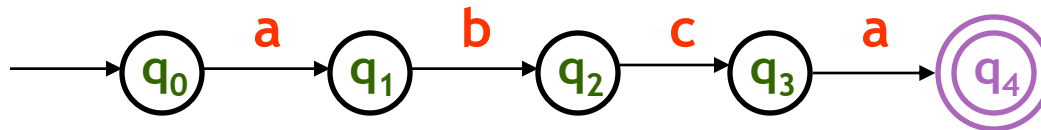
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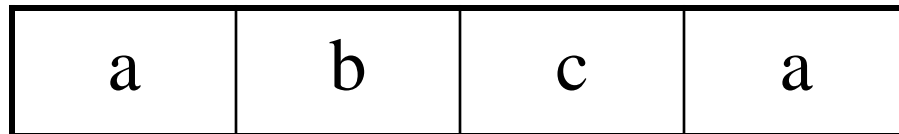
State	Input		
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0	1	∅	∅
1	∅	2	∅
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4	∅	∅	∅

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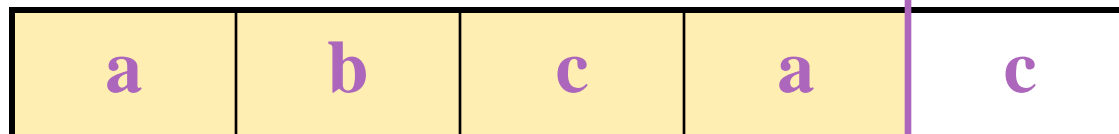
IS₁:



IS₂:



IS₃:



State	Input		
	a	b	c
0	1	∅	∅
1	∅	2	∅
2	∅	∅	3
3	4	∅	∅
4	∅	∅	∅