



Information Security System

EC-415-F

6/30/2015



Lecture 1

Topics Covered

- Approaches to Message Authentication
- Secure Hash Functions and HMAC
- Public-Key Cryptography Principles
- Public-Key Cryptography Algorithms
- Digital Signatures
- Key Management

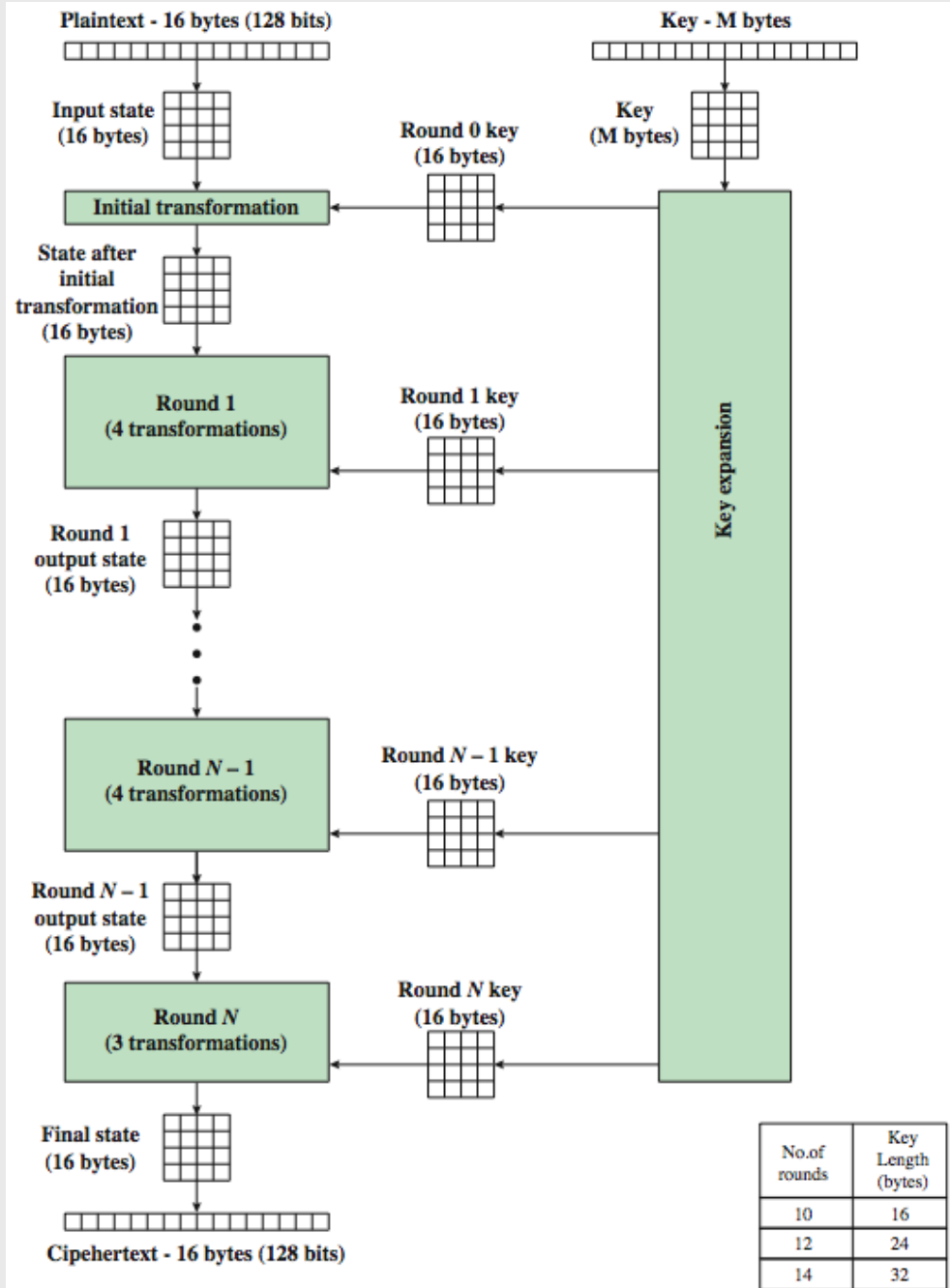
AES Origins

- clear a replacement for DES was needed
 - have theoretical attacks that can break it
 - have demonstrated exhaustive key search attacks
- can use Triple-DES – but slow, has small blocks
- US NIST issued call for ciphers in 1997
- 15 candidates accepted in Jun 98
- 5 were shortlisted in Aug-99
- Rijndael was selected as the AES in Oct-2000
- issued as FIPS PUB 197 standard in Nov-2001

The AES Cipher - Rijndael

- designed by Rijmen-Daemen in Belgium
- has 128/192/256 bit keys, 128 bit data
- an **iterative** rather than Feistel cipher
 - processes data as block of 4 columns of 4 bytes
 - operates on entire data block in every round
- designed to have:
 - resistance against known attacks
 - speed and code compactness on many CPUs
 - design simplicity

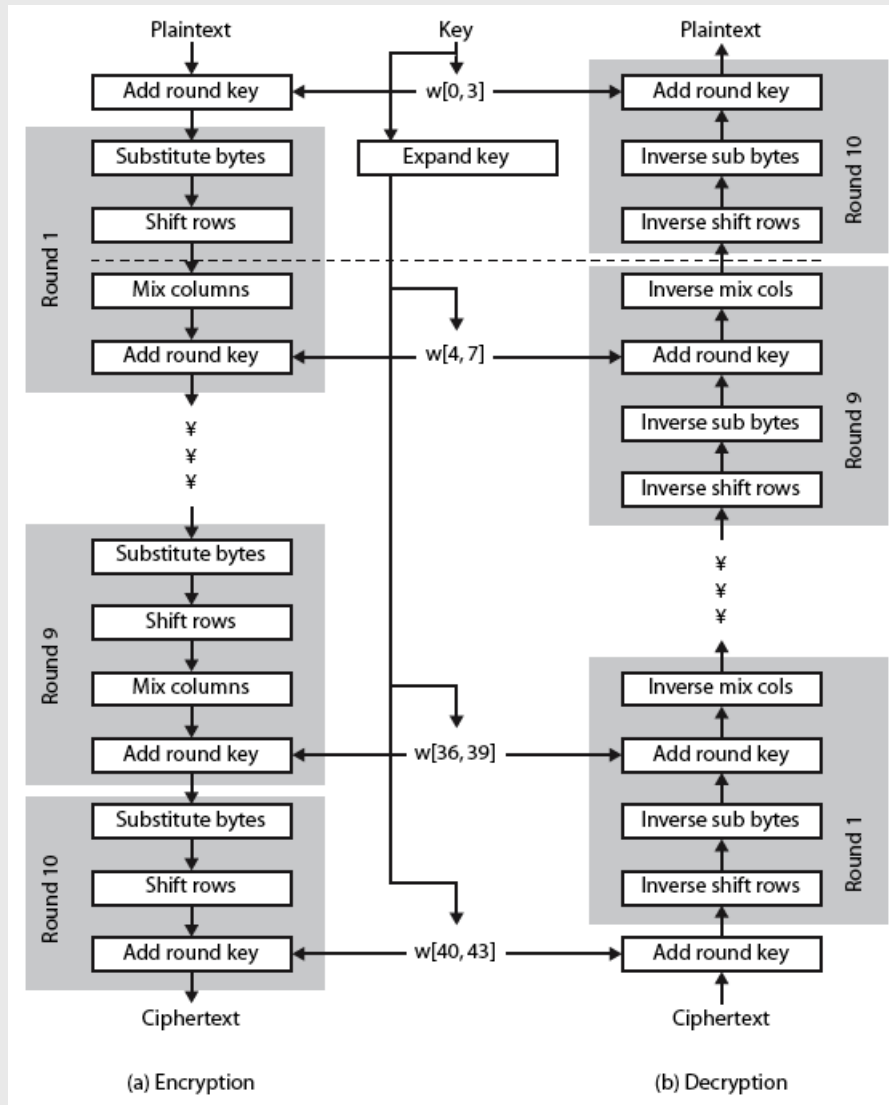
AES Encryption Process



AES Structure

- data block of 4 columns of 4 bytes is state
- key is expanded to array of words
- has 9/11/13 rounds in which state undergoes:
 - byte substitution (1 S-box used on every byte)
 - shift rows (permute bytes between groups/columns)
 - mix columns (subs using matrix multiply of groups)
 - add round key (XOR state with key material)
 - view as alternating XOR key & scramble data bytes
- initial XOR key material & incomplete last round
- with fast XOR & table lookup implementation

AES Structure



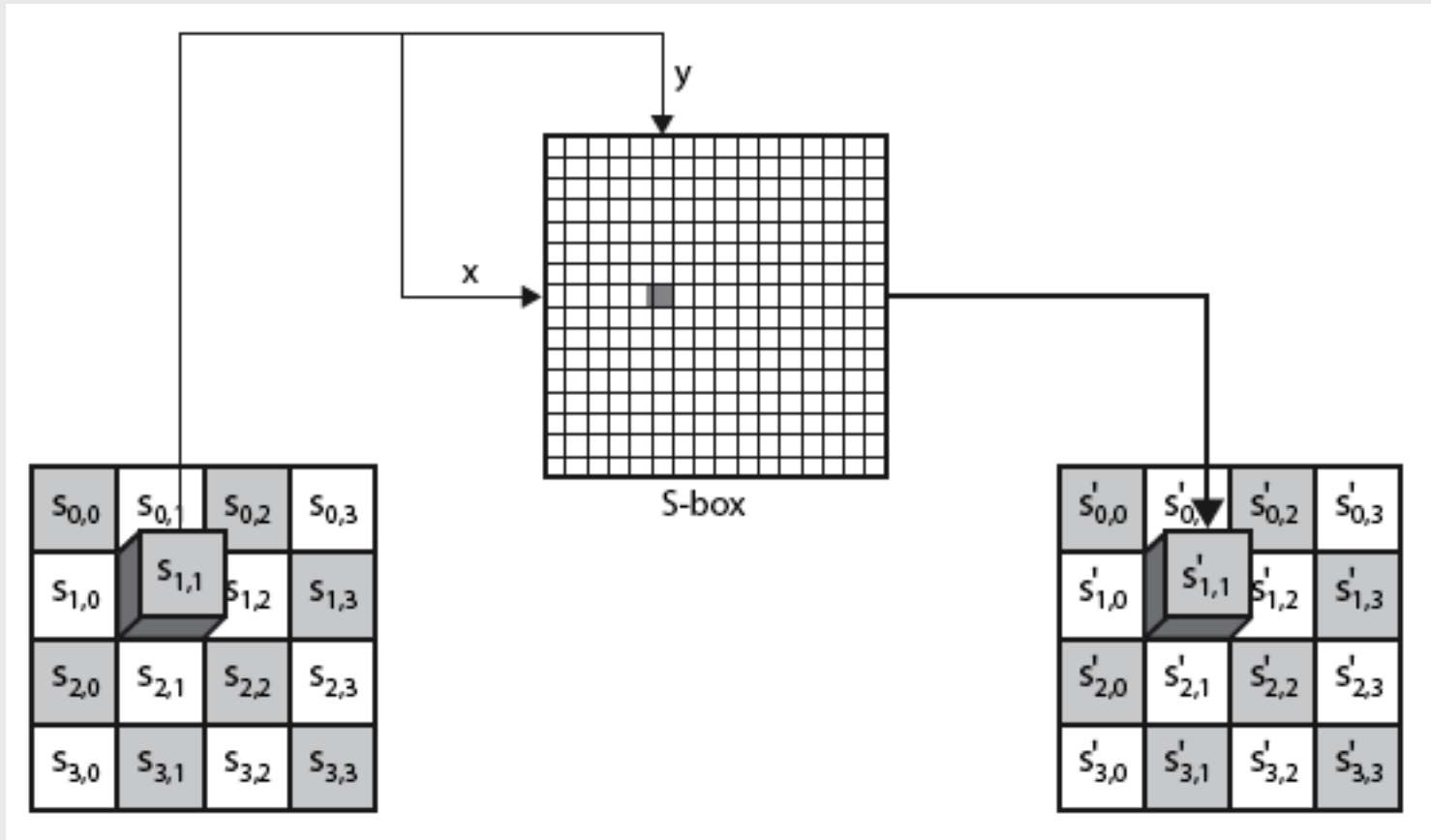
Some Comments on AES

1. an iterative rather than Feistel cipher
2. key expanded into array of 32-bit words
 1. four words form round key in each round
3. 4 different stages are used as shown
4. has a simple structure
5. only AddRoundKey uses key
6. AddRoundKey a form of Vernam cipher
7. each stage is easily reversible
8. decryption uses keys in reverse order
9. decryption does recover plaintext
10. final round has only 3 stages

Substitute Bytes

- a simple substitution of each byte
- uses one table of 16x16 bytes containing a permutation of all 256 8-bit values
- each byte of state is replaced by byte indexed by row (left 4-bits) & column (right 4-bits)
 - eg. byte {95} is replaced by byte in row 9 column 5
 - which has value {2A}
- S-box constructed using defined transformation of values in $GF(2^8)$
- designed to be resistant to all known attacks

Substitute Bytes



Substitute Bytes Example

| | | | |
|----|----|----|----|
| EA | 04 | 65 | 85 |
| 83 | 45 | 5D | 96 |
| 5C | 33 | 98 | B0 |
| F0 | 2D | AD | C5 |

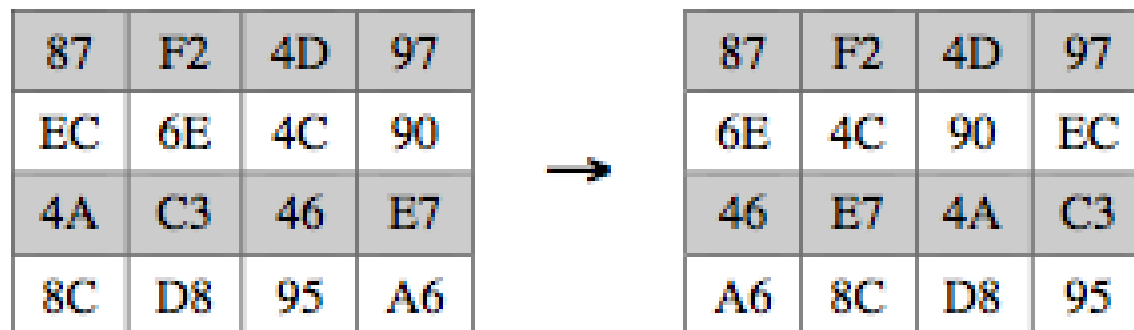
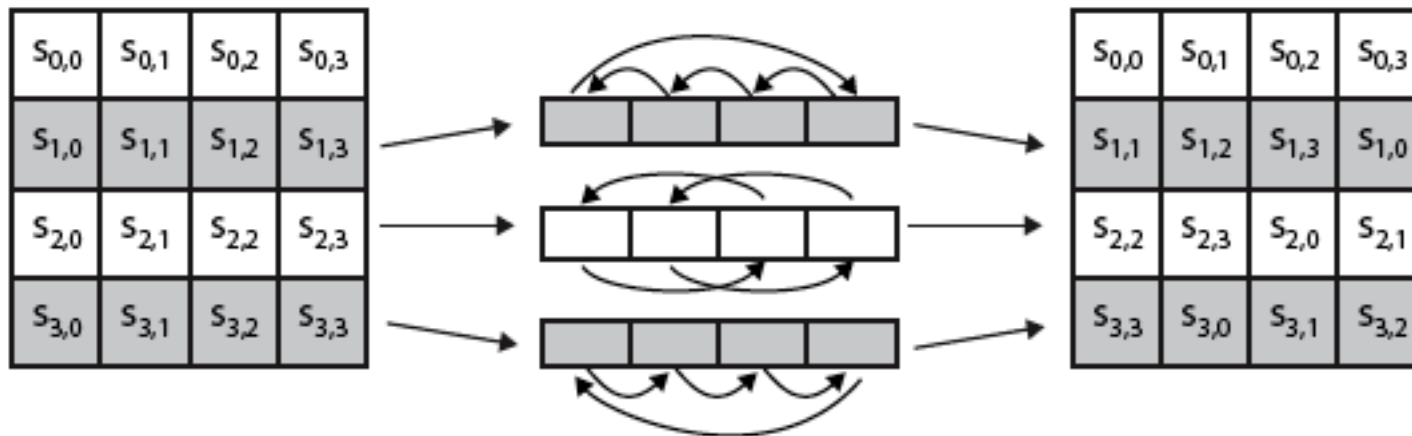


| | | | |
|----|----|----|----|
| 87 | F2 | 4D | 97 |
| EC | 6E | 4C | 90 |
| 4A | C3 | 46 | E7 |
| 8C | D8 | 95 | A6 |

Shift Rows

- a circular byte shift in each each
 - 1st row is unchanged
 - 2nd row does 1 byte circular shift to left
 - 3rd row does 2 byte circular shift to left
 - 4th row does 3 byte circular shift to left
- decrypt inverts using shifts to right
- since state is processed by columns, this step permutes bytes between the columns

Shift Rows

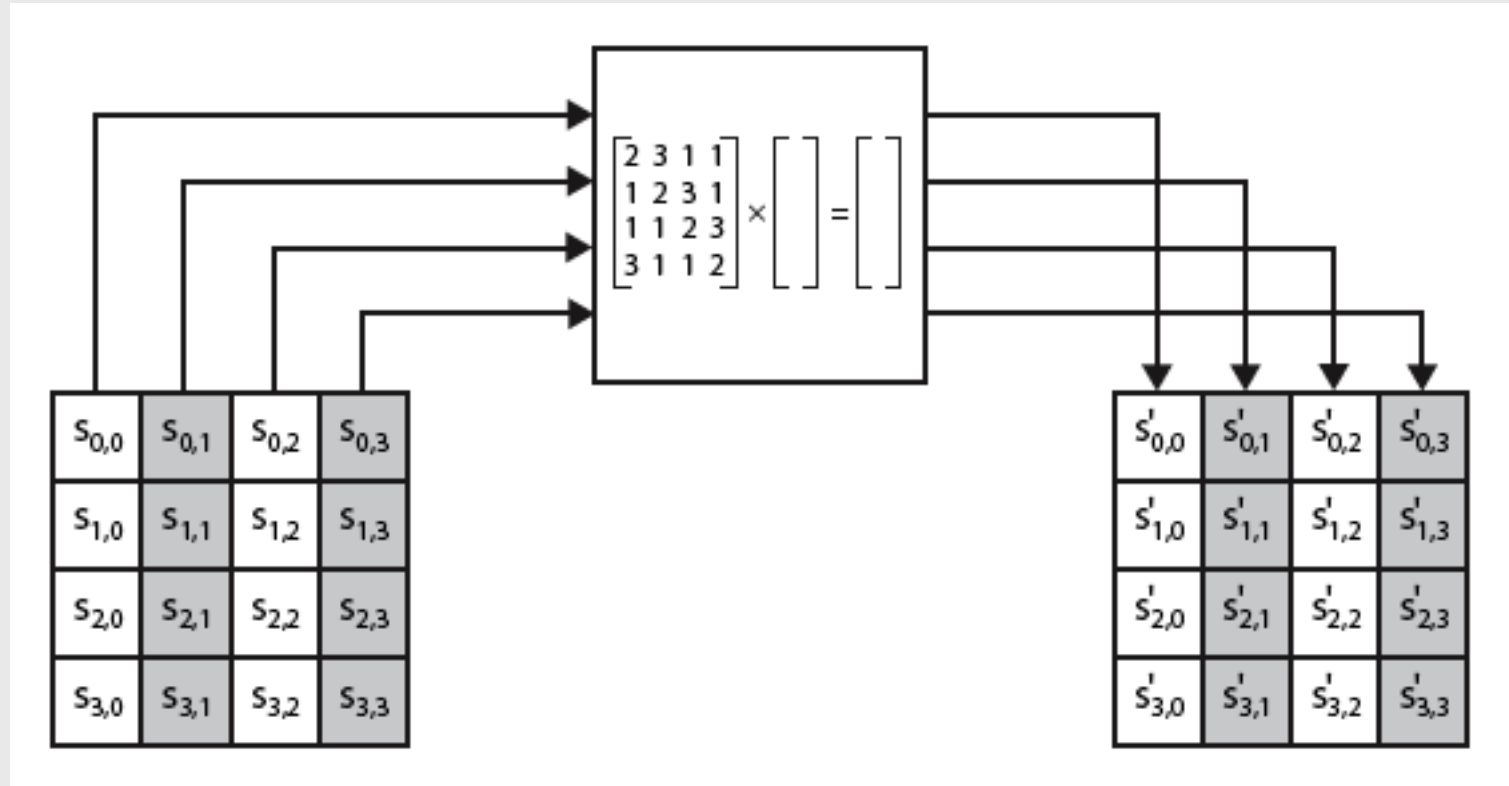


Mix Columns

- each column is processed separately
- each byte is replaced by a value dependent on all 4 bytes in the column
- effectively a matrix multiplication in $GF(2^8)$ using prime poly $m(x) = x^8 + x^4 + x^3 + x + 1$

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ s_{3,0} & s_{3,1} & s_{3,2} & s_{3,3} \end{bmatrix} = \begin{bmatrix} s'_{0,0} & s'_{0,1} & s'_{0,2} & s'_{0,3} \\ s'_{1,0} & s'_{1,1} & s'_{1,2} & s'_{1,3} \\ s'_{2,0} & s'_{2,1} & s'_{2,2} & s'_{2,3} \\ s'_{3,0} & s'_{3,1} & s'_{3,2} & s'_{3,3} \end{bmatrix}$$

Mix Columns



Mix Columns Example

| | | | | | | | | |
|----|----|----|----|---|----|----|----|----|
| 87 | F2 | 4D | 97 | → | 47 | 40 | A3 | 4C |
| 6E | 4C | 90 | EC | | 37 | D4 | 70 | 9F |
| 46 | E7 | 4A | C3 | | 94 | E4 | 3A | 42 |
| A6 | 8C | D8 | 95 | | ED | A5 | A6 | BC |

$$(\{02\} \cdot \{87\}) \oplus (\{03\} \cdot \{6E\}) \oplus \{46\} \oplus \{A6\} = \{47\}$$

$$\{87\} \oplus (\{02\} \cdot \{6E\}) \oplus (\{03\} \cdot \{46\}) \oplus \{A6\} = \{37\}$$

$$\{87\} \oplus \{6E\} \oplus (\{02\} \cdot \{46\}) \oplus (\{03\} \cdot \{A6\}) = \{94\}$$

$$(\{03\} \cdot \{87\}) \oplus \{6E\} \oplus \{46\} \oplus (\{02\} \cdot \{A6\}) = \{ED\}$$

AES Arithmetic

- uses arithmetic in the finite field $GF(2^8)$
- with irreducible polynomial

$$m(x) = x^8 + x^4 + x^3 + x + 1$$

which is (100011011) or {11b}

- e.g.

$$\begin{aligned} \{02\} \cdot \{87\} \bmod \{11b\} &= (1\ 0000\ 1110) \bmod \{11b\} \\ &= (1\ 0000\ 1110) \text{ xor } (1\ 0001\ 1011) = (0001\ 0101) \end{aligned}$$

Mix Columns

- can express each col as 4 equations
 - to derive each new byte in col
- decryption requires use of inverse matrix
 - with larger coefficients, hence a little harder
- have an alternate characterisation
 - each column a 4-term polynomial
 - with coefficients in $GF(2^8)$
 - and polynomials multiplied modulo (x^4+1)
- coefficients based on linear code with maximal distance between codewords

Add Round Key

- XOR state with 128-bits of the round key
- again processed by column (though effectively a series of byte operations)
- inverse for decryption identical
 - since XOR own inverse, with reversed keys
- designed to be as simple as possible
 - a form of Vernam cipher on expanded key
 - requires other stages for complexity / security

Add Round Key

| | | | |
|-----------|-----------|-----------|-----------|
| $s_{0,0}$ | $s_{0,1}$ | $s_{0,2}$ | $s_{0,3}$ |
| $s_{1,0}$ | $s_{1,1}$ | $s_{1,2}$ | $s_{1,3}$ |
| $s_{2,0}$ | $s_{2,1}$ | $s_{2,2}$ | $s_{2,3}$ |
| $s_{3,0}$ | $s_{3,1}$ | $s_{3,2}$ | $s_{3,3}$ |

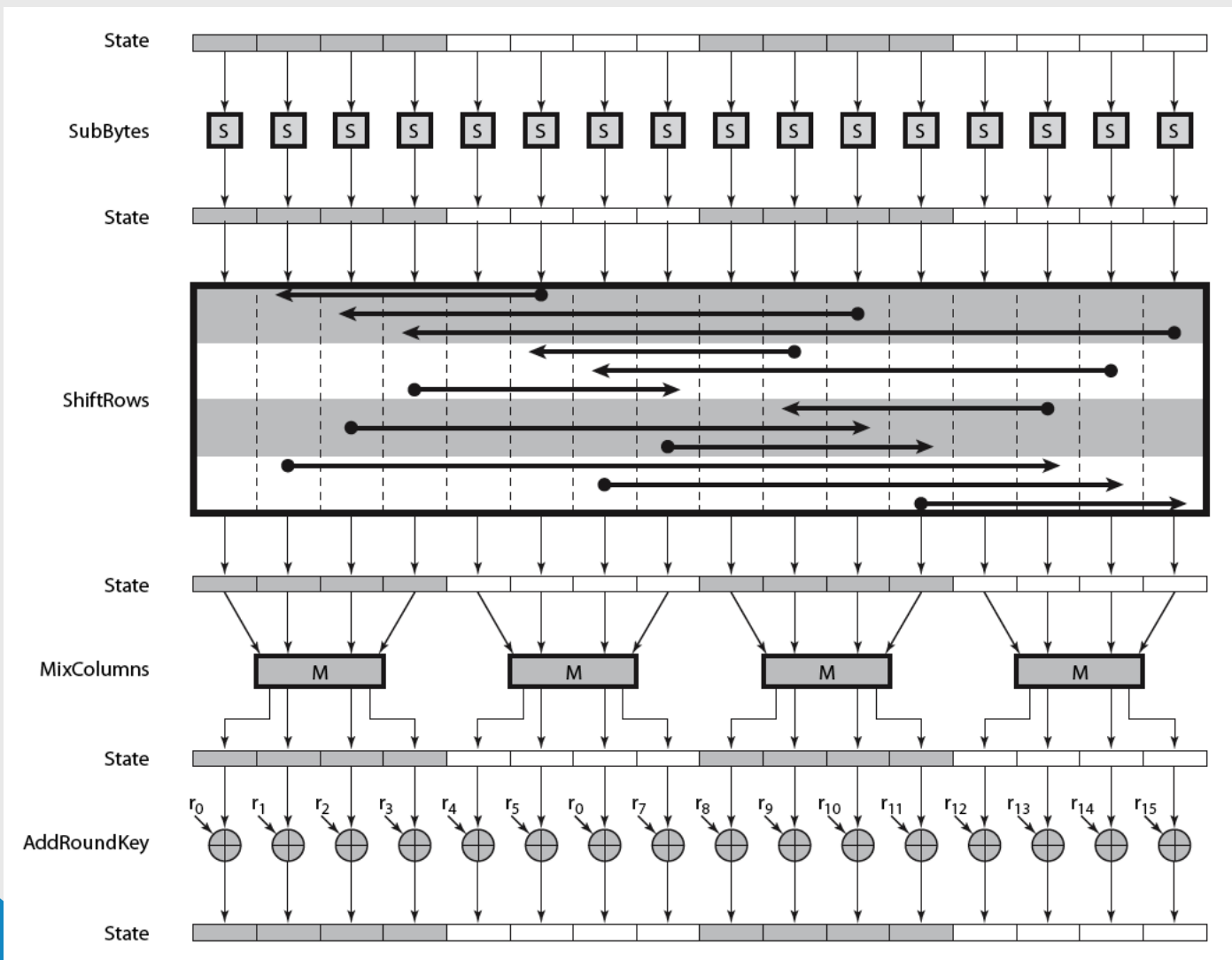
\oplus

| | | | |
|-------|-----------|-----------|-----------|
| w_i | w_{i+1} | w_{i+2} | w_{i+3} |
|-------|-----------|-----------|-----------|

=

| | | | |
|------------|------------|------------|------------|
| $s'_{0,0}$ | $s'_{0,1}$ | $s'_{0,2}$ | $s'_{0,3}$ |
| $s'_{1,0}$ | $s'_{1,1}$ | $s'_{1,2}$ | $s'_{1,3}$ |
| $s'_{2,0}$ | $s'_{2,1}$ | $s'_{2,2}$ | $s'_{2,3}$ |
| $s'_{3,0}$ | $s'_{3,1}$ | $s'_{3,2}$ | $s'_{3,3}$ |

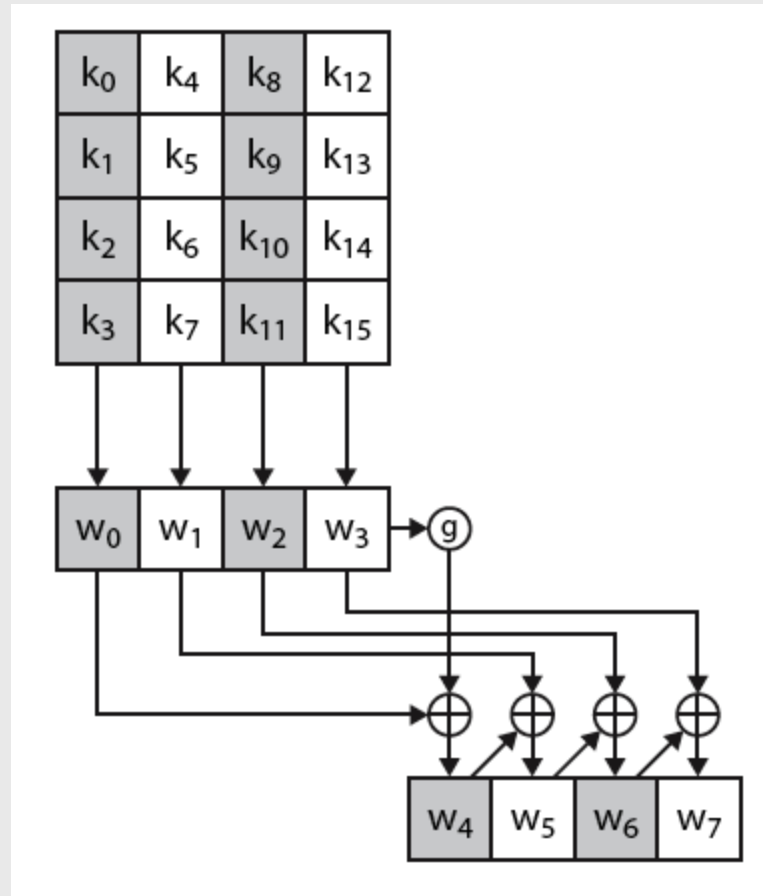
AES Round



AES Key Expansion

- takes 128-bit (16-byte) key and expands into array of 44/52/60 32-bit words
- start by copying key into first 4 words
- then loop creating words that depend on values in previous & 4 places back
 - in 3 of 4 cases just XOR these together
 - 1st word in 4 has rotate + S-box + XOR round constant on previous, before XOR 4th back

AES Key Expansion



Key Expansion Rationale

- designed to resist known attacks
- design criteria included
 - knowing part key insufficient to find many more
 - invertible transformation
 - fast on wide range of CPU's
 - use round constants to break symmetry
 - diffuse key bits into round keys
 - enough non-linearity to hinder analysis
 - simplicity of description

AES Example Key Expansion

| Key Words | Auxiliary Function |
|--|---|
| w0 = 0f 15 71 c9 w1 = 47 d9 e8 59 w2 = 0c b7 ad w3 = af 7f 67 98 | RotWord(w3)= 7f 67 98 af = x1 SubWord(x1)= d2 85 46 79 = y1 Rcon(1)= 01 00 00 00 y1 ⊕ Rcon(1)= d3 85 46 79 = z1 |
| w4 = w0 ⊕ z1 = dc 90 37 b0 w5 = w4 ⊕ w1 = 9b 49 df e9 w6 = w5 ⊕ w2 = 97 fe 72 3f w7 = w6 ⊕ w3 = 38 81 15 a7 | RotWord(w7)= 81 15 a7 38 = x2 SubWord(x4)= 0c 59 5c 07 = y2 Rcon(2)= 02 00 00 00 y2 ⊕ Rcon(2)= 0e 59 5c 07 = z2 |
| w8 = w4 ⊕ z2 = d2 c9 6b b7 w9 = w8 ⊕ w5 = 49 80 b4 5e w10 = w9 ⊕ w6 = de 7e c6 61 w11 = w10 ⊕ w7 = e6 ff d3 c6 | RotWord(w11)= ff d3 c6 e6 = x3 SubWord(x2)= 16 66 b4 8e = y3 Rcon(3)= 04 00 00 00 y3 ⊕ Rcon(3)= 12 66 b4 8e = z3 |
| w12 = w8 ⊕ z3 = c0 af df 39 w13 = w12 ⊕ w9 = 89 2f 6b 67 w14 = w13 ⊕ w10 = 57 51 ad 06 w15 = w14 ⊕ w11 = b1 ae 7e c0 | RotWord(w15)= ae 7e c0 b1 = x4 SubWord(x3)= e4 f3 ba c8 = y4 Rcon(4)= 08 00 00 00 y4 ⊕ Rcon(4)= ec f3 ba c8 = z4 |
| w16 = w12 ⊕ z4 = 2c 5c 65 f1 w17 = w16 ⊕ w13 = a5 73 0e 96 w18 = w17 ⊕ w14 = f2 22 a3 90 w19 = w18 ⊕ w15 = 43 8c dd 50 | RotWord(w19)= 8c dd 50 43 = x5 SubWord(x4)= 64 c1 53 1a = y5 Rcon(5)= 10 00 00 00 y5 ⊕ Rcon(5)= 74 c1 53 1a = z5 |
| w20 = w16 ⊕ z5 = 58 9d 36 eb w21 = w20 ⊕ w17 = fd ee 38 7d w22 = w21 ⊕ w18 = 0f cc 9b ed w23 = w22 ⊕ w19 = 4c 40 46 bd | RotWord(w23)= 40 46 bd 4c = x6 SubWord(x5)= 09 5a 7a 29 = y6 Rcon(6)= 20 00 00 00 y6 ⊕ Rcon(6)= 29 5a 7a 29 = z6 |
| w24 = w20 ⊕ z6 = 71 c7 4c c2 w25 = w24 ⊕ w21 = 8c 29 74 bf w26 = w25 ⊕ w22 = 83 e5 ef 52 w27 = w26 ⊕ w23 = cf a5 a9 ef | RotWord(w27)= a5 a9 ef cf = x7 SubWord(x6)= 06 d3 df 8a = y7 Rcon(7)= 40 00 00 00 y7 ⊕ Rcon(7)= 46 d3 df 8a = z7 |
| w28 = w24 ⊕ z7 = 37 14 93 48 w29 = w28 ⊕ w25 = bb 3d e7 f7 w30 = w29 ⊕ w26 = 38 d8 08 a5 w31 = w30 ⊕ w27 = f7 7d a1 4a | RotWord(w31)= 7d a1 4a f7 = x8 SubWord(x7)= ff 32 d6 68 = y8 Rcon(8)= 80 00 00 00 y8 ⊕ Rcon(8)= 7f 32 d6 68 = z8 |
| w32 = w28 ⊕ z8 = 48 26 45 20 w33 = w32 ⊕ w29 = f3 1b a2 d7 w34 = w33 ⊕ w30 = cb c3 aa 72 w35 = w34 ⊕ w32 = 3c be 0b 38 | RotWord(w35)= be 0b 38 3c = x9 SubWord(x8)= ae 2b 07 eb = y9 Rcon(9)= 1b 00 00 00 y9 ⊕ Rcon(9)= b5 2b 07 eb = z9 |
| w36 = w32 ⊕ z9 = fd 0d 42 cb w37 = w36 ⊕ w33 = 0e 16 e0 1c w38 = w37 ⊕ w34 = c5 d5 4a 6e w39 = w38 ⊕ w35 = f9 6b 41 56 | RotWord(w39)= 6b 41 56 f9 = x10 SubWord(x9)= 7f 83 b1 99 = y10 Rcon(10)= 36 00 00 00 y10 ⊕ Rcon(10)= 49 83 b1 99 = z10 |
| w40 = w36 ⊕ z10 = b4 8e f3 52 w41 = w40 ⊕ w37 = ba 98 13 4e w42 = w41 ⊕ w38 = 7f 4d 59 20 w43 = w42 ⊕ w39 = 86 26 18 76 | |

AES Example Encryption

| Start of round | After SubBytes | After ShiftRows | After MixColumns | Round Key |
|--|--|--|--|--|
| 01 89 fe 76 23 ab dc 54 45 cd ba 32 67 ef 98 10 | | | | 0f 47 0c af 15 d9 b7 7f 71 e8 ad 67 c9 59 d6 98 |
| 0e ce f2 d9 36 72 6b 2b 34 25 17 55 ae b6 4e 88 | ab 8b 89 35 05 40 7f f1 18 3f f0 fc e4 4e 2f c4 | ab 8b 89 35 40 7f f1 05 f0 fc 18 3f c4 e4 4e 2f | b9 94 57 75 e4 8e 16 51 47 20 9a 3f c5 d6 f5 3b | dc 9b 97 38 90 49 fe 81 37 df 72 15 b0 e9 3f a7 |
| 65 0f c0 4d 74 c7 e8 d0 70 ff e8 2a 75 3f ca 9c | 4d 76 ba e3 92 c6 9b 70 51 16 9b e5 9d 75 74 de | 4d 76 ba e3 c6 9b 70 92 9b e5 51 16 de 9d 75 74 | 8e 22 db 12 b2 f2 dc 92 df 80 f7 c1 2d c5 1e 52 | d2 49 de e6 c9 80 7e ff 6b b4 c6 d3 b7 5e 61 c6 |
| 5c 6b 05 f4 7b 72 a2 6d b4 34 31 12 9a 9b 7f 94 | 4a 7f 6b bf 21 40 3a 3c 8d 18 c7 c9 b8 14 d2 22 | 4a 7f 6b bf 40 3a 3c 21 c7 c9 8d 18 22 b8 14 d2 | b1 c1 0b cc ba f3 8b 07 f9 1f 6a c3 1d 19 24 5c | c0 89 57 b1 af 2f 51 ae df 6b ad 7e 39 67 06 c0 |
| 71 48 5c 7d 15 dc da a9 26 74 c7 bd 24 7e 22 9c | a3 52 4a ff 59 86 57 d3 f7 92 c6 7a 36 f3 93 de | a3 52 4a ff 86 57 d3 59 c6 7a f7 92 de 36 f3 93 | d4 11 fe 0f 3b 44 06 73 cb ab 62 37 19 b7 07 ec | 2c a5 f2 43 5c 73 22 8c 65 0e a3 dd f1 96 90 50 |
| f8 b4 0c 4c 67 37 24 ff ae a5 c1 ea e8 21 97 bc | 41 8d fe 29 85 9a 36 16 e4 06 78 87 9b fd 88 65 | 41 8d fe 29 9a 36 16 85 78 87 e4 06 65 9b fd 88 | 2a 47 c4 48 83 e8 18 ba 84 18 27 23 eb 10 0a f3 | 58 fd 0f 4c 9d ee cc 40 36 38 9b 46 eb 7d ed bd |
| 72 ba cb 04 1e 06 d4 fa b2 20 bc 65 00 6d e7 4e | 40 f4 1f f2 72 6f 48 2d 37 b7 65 4d 63 3c 94 2f | 40 f4 1f f2 6f 48 2d 72 65 4d 37 b7 2f 63 3c 94 | 7b 05 42 4a 1e d0 20 40 94 83 18 52 94 c4 43 fb | 71 8c 83 cf c7 29 e5 a5 4c 74 ef a9 c2 bf 52 ef |
| 0a 89 c1 85 d9 f9 c5 e5 d8 f7 f7 fb 56 7b 11 14 | 67 a7 78 97 35 99 a6 d9 61 68 68 0f b1 21 82 fa | 67 a7 78 97 99 a6 d9 35 68 0f 61 68 fa b1 21 82 | ec 1a c0 80 0c 50 53 c7 3b d7 00 ef b7 22 72 e0 | 37 bb 38 f7 14 3d d8 7d 93 e7 08 a1 48 f7 a5 4a |
| db a1 f8 77 18 6d 8b ba a8 30 08 4e ff d5 d7 aa | b9 32 41 f5 ad 3c 3d f4 c2 04 30 2f 16 03 0e ac | b9 32 41 f5 3c 3d f4 ad 30 2f c2 04 ac 16 03 0e | b1 1a 44 17 3d 2f ec b6 0a 6b 2f 42 9f 68 f3 b1 | 48 f3 cb 3c 26 1b c3 be 45 a2 aa 0b 20 d7 72 38 |
| f9 e9 8f 2b 1b 34 2f 08 4f c9 85 49 bf bf 81 89 | 99 1e 73 f1 af 18 15 30 84 dd 97 3b 08 08 0c a7 | 99 1e 73 f1 18 15 30 af 97 3b 84 dd a7 08 08 0c | 31 30 3a c2 ac 71 8c c4 46 65 48 eb 6a 1c 31 62 | fd 0e c5 f9 0d 16 d5 6b 42 e0 4a 41 cb 1c 6e 56 |
| cc 3e ff 3b a1 67 59 af 04 85 02 aa a1 00 5f 34 | 4b b2 16 e2 32 85 cb 79 f2 97 77 ac 32 63 cf 18 | 4b b2 16 e2 85 cb 79 32 77 ac f2 97 18 32 63 cf | 4b 86 8a 36 b1 cb 27 5a fb f2 f2 af cc 5a 5b cf | b4 8e f3 52 ba 98 13 4e 7f 4d 59 20 86 26 18 76 |
| ff 08 69 64 0b 53 34 14 84 bf ab 8f 4a 7c 43 b9 | | | | |

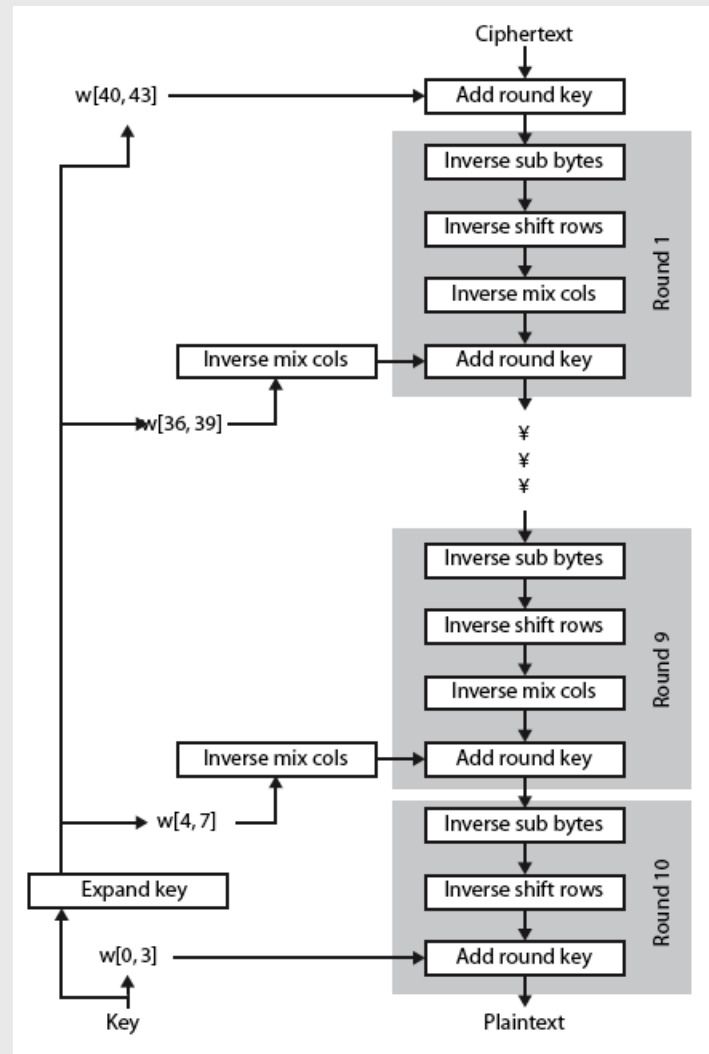
AES Example Avalanche

| Round | | Number of bits that differ |
|-------|--|----------------------------|
| | 0123456789abcdef fedcba9876543210 0023456789abcdef fedcba9876543210 | 1 |
| 0 | 0e3634aece7225b6f26b174ed92b5588 0f3634aece7225b6f26b174ed92b5588 | 1 |
| 1 | 657470750fc7ff3fc0e8e8ca4dd02a9c c4a9ad090fc7ff3fc0e8e8ca4dd02a9c | 20 |
| 2 | 5c7bb49a6b72349b05a2317ff46d1294 fe2ae569f7ee8bb8c1f5a2bb37ef53d5 | 58 |
| 3 | 7115262448dc747e5cdac7227da9bd9c ec093dfb7c45343d689017507d485e62 | 59 |
| 4 | f867aee8b437a5210c24c1974cffeabc 43efdb697244df808e8d9364ee0ae6f5 | 61 |
| 5 | 721eb200ba06206dcbd4bce704fa654e 7b28a5d5ed643287e006c099bb375302 | 68 |
| 6 | 0ad9d85689f9f77bc1c5f71185e5fb14 3bc2d8b6798d8ac4fe36ald891ac181a | 64 |
| 7 | db18a8ffa16d30d5f88b08d777ba4eea 9fb8b5452023c70280e5c4bb9e555a4b | 67 |
| 8 | f91b4fbfe934c9bf8f2f85812b084989 20264e1126b219aef7feb3f9b2d6de40 | 65 |
| 9 | cca104a13e678500ff59025f3bafaa34 b56a0341b2290ba7dfdfbddcd8578205 | 61 |
| 10 | ff0b844a0853bf7c6934ab4364148fb9 612b89398d0600cde116227ce72433f0 | 58 |

AES Decryption

- AES decryption is not identical to encryption since steps done in reverse
- but can define an equivalent inverse cipher with steps as for encryption
 - but using inverses of each step
 - with a different key schedule
- works since result is unchanged when
 - swap byte substitution & shift rows
 - swap mix columns & add (tweaked) round key

AES Decryption



Implementation Aspects

- can efficiently implement on 8-bit CPU
 - byte substitution works on bytes using a table of 256 entries
 - shift rows is simple byte shift
 - add round key works on byte XOR's
 - mix columns requires matrix multiply in $GF(2^8)$ which works on byte values, can be simplified to use table lookups & byte XOR's

Implementation Aspects

- can efficiently implement on 32-bit CPU
 - redefine steps to use 32-bit words
 - can precompute 4 tables of 256-words
 - then each column in each round can be computed using 4 table lookups + 4 XORs
 - at a cost of 4Kb to store tables
- designers believe this very efficient implementation was a key factor in its selection as the AES cipher

Summary

- have considered:
 - the AES selection process
 - the details of Rijndael – the AES cipher
 - looked at the steps in each round
 - the key expansion
 - implementation aspects