Compiler Design



Lecture-4

Introdution to Lexical Analysis

Topics Covered

- n Approaches to implement a lexical analyzer
- n The role of the lexical analyzer
- n Transition Diagram
- n Finite Automata

Section 0 Approaches to implement a lexical analyzer

1. Simple approach

 Construct a diagram that illustrates the structure of the tokens of the source language, and then to hand-translate the diagram into a program for finding tokens
 Notes: Efficient lexical analyzers can be produced in this manner

Section 0 Approaches to implement a lexical analyzer

2. Pattern-directed programming approach

- Pattern Matching technique
- Specify and design program that execute actions triggered by patterns in strings
- Introduce a pattern-action language called Lex for specifying lexical analyzers
 - Patterns are specified by regular expressions
 - A compiler for Lex can generate an efficient finite automation recognizer for the regular expressions

First phase of a compiler

- 1. Main task
 - To read the input characters
 - To produce a sequence of tokens used by the parser for syntax analysis
 - As an assistant of parser

2. Interaction of lexical analyzer with parser



3. Processes in lexical analyzers

- Scanning
 - Pre-processing
 - Strip out comments and white space
 - Macro functions
- Correlating error messages from compiler with source program
 - A line number can be associated with an error message
- Lexical analysis

CHAPTER 3 LEXICAL ANALYSIS Section 1 The role of the lexical analyzer

- Terms of the lexical analyzer
 –Token
 - Types of words in source program
 - Keywords, operators, identifiers, constants, literal strings, punctuation symbols(such as commas, semicolons)
 - -Lexeme
 - Actual words in source program
 - -Pattern
 - A rule describing the set of lexemes that can represent a particular token in source program
 - Relation {<.<=,>,>=,==,<>}

- 5. Attributes for Tokens
 - –A pointer to the symbol-table entry in which the information about the token is kept
 - E.g $E=M^*C^{**}2$
 - <id, pointer to symbol-table entry for E> <assign_op,>
 - <id, pointer to symbol-table entry for M> <multi_op,>
 - <id, pointer to symbol-table entry for C>
 - <exp_op,>
 - <num,integer value 2>

6. Lexical Errors

- Deleting an extraneous character
- Inserting a missing character
- Replacing an incorrect character by a correct character
- Transposing two adjacent characters(such as , fi=>if)
- Pre-scanning

7. Input Buffering

- Two-buffer input scheme to look ahead on the input and identify tokens
- Buffer pairs
- Sentinels(Guards)

Regular Definition of Tokens Defined in regular expression

e.g. Id \rightarrow letter(letter|digit)

letter \rightarrow A|B|...|Z|a|b|...|z **digit** \rightarrow 0|1|2|...|9

Notes: Regular expressions are an important notation for specifying patterns. Each pattern matches a set of strings, so regular expressions will serve as as names for sets of strings.

- 2. Regular Expression & Regular language
 - Regular Expression
 - A notation that allows us to define a pattern in a high level language.
 - Regular language
 - Each regular expression r denotes a language L(r) (the set of sentences relating to the regular expression r)

Notes: Each word in a program can be expressed in a regular expression

- 3. The rule of regular expression over alphabet $\boldsymbol{\Sigma}$
 - 1) ϵ is a regular expression that denote $\{\epsilon\}$
 - ϵ is regular expression
 - $\{\epsilon\}$ is the related regular language
 - 2) If *a* is a symbol in Σ , then *a* is a regular expression that denotes $\{a\}$
 - a is regular expression
 - {a} is the related regular language

- 3. The rule of regular expression over alphabet $\boldsymbol{\Sigma}$
 - 3) Suppose α and β are regular expressions, then $\alpha|\beta, \alpha\beta, \alpha^*, \beta^*$ is also a regular expression

Notes: Rules 1) and 2) form the basis of the definition; rule 3) provides the inductive step.

4. Algebraic laws of regular expressions 1) $\alpha |\beta = \beta |\alpha$ 2) $\alpha |(\beta|\gamma) = (\alpha|\beta)|\gamma \quad \alpha(\beta\gamma) = (\alpha \beta)\gamma$ 3) $\alpha(\beta|\gamma) = \alpha\beta | \alpha\gamma$ ($\alpha|\beta)\gamma = \alpha\gamma | \beta\gamma$ 4) $\varepsilon \alpha = \alpha \varepsilon = \alpha$ $(\alpha^{*})^{*} = \alpha^{*}$ 6) $\alpha^* = \alpha^+ | \epsilon$ $\alpha^+ = \alpha \alpha^* = \alpha^* \alpha$ 7) $(\alpha | \beta)^* = (\alpha^* | \beta^*)^* = (\alpha^* \beta^*)^*$

4. Algebraic laws of regular expressions 8) If $\epsilon \notin L(\gamma)$, then

$$\alpha = \beta | \gamma \alpha \qquad \alpha = \gamma^* \beta$$

$$\alpha = \beta | \alpha \gamma \qquad \alpha = \beta \gamma^*$$

Notes: We assume that the precedence of * is the highest, the precedence of | is the lowest and they are left associative



5. Notational Short-hands a)One or more instances (r)⁺ digit⁺ b)Zero or one instance r? is a shorthand for $r|\epsilon$ (E(+|-)?digits)? c)Character classes [a-z] denotes a|b|c|...|z [A-Za-z] [A-Za-z0-9]

- 1. Task of recognition of token in a lexical analyzer
 - Isolate the lexeme for the next token in the input buffer
 - Produce as output a pair consisting of the appropriate token and attribute-value, such as <id,pointer to table entry> , using the translation table given in the Fig in next page

1. Task of recognition of token in a lexical analyzer

| Regular | Token | Attribute- |
|------------|-------|-------------|
| expression | | value |
| if | if | - |
| id | id | Pointer to |
| | | table entry |
| < | relop | LT |

- 2. Methods to recognition of token
 - Use Transition Diagram

CHAPTER 3 LEXICAL ANALYSIS Section 3 Recognition of Tokens 3. Transition Diagram(Stylized flowchart)

 Depict the actions that take place when a lexical analyzer is called by the parser to get the next token



Notes: Here we use '*' to indicate states on which input retraction must take place

- 4. Implementing a Transition Diagram
 - Each state gets a segment of code
 - If there are edges leaving a state, then its code reads a character and selects an edge to follow, if possible
 - Use nextchar() to read next character from the input buffer



```
Implementing a Transition Diagram
while (1) {
 switch(state) {
  case 0: c=nextchar();
         if (c==blank || c==tab || c==newline){
             state=0;lexeme_beginning++}
         else if (c=='=') state=5;
         else if(c=='>') state=6 else state=fail();
          break
   case 9: c=nextchar();
         if (isletter( c)) state=10;
         else state=fail(); break
 ... }}}
```



- 5. A generalized transition diagram Finite Automation
 - Deterministic or non-deterministic FA
 - Non-deterministic means that more than one transition out of a state may be possible on the the same input symbol

6. The model of recognition of tokens



E.g: The FA simulator for Identifiers is:



– Which represent the rule: identifier=letter(letter|digit)*



1. Usage of FA

- Precisely recognize the regular sets
- A regular set is a set of sentences relating to the regular expression

2. Sorts of FA

- Deterministic FA
- Non-deterministic FA



- 3. Deterministic FA (DFA)
 - DFA is a quintuple, $M(S,\Sigma,move,s_0,F)$
 - S: a set of states
 - $-\Sigma$: the input symbol alphabet
 - move: a transition function, mapping from $S \times \Sigma$ to S, *move(s,a)*=s'
 - s_0 : the *start* state, $s_0 \in S$
 - F: a set of states *F* distinguished as accepting states, F⊆S



3. Deterministic FA (DFA)

Note: 1) In a DFA, no state has an ϵ -transition;

2)In a DFA, for each state *s* and input symbol *a*, there is at most one edge labeled *a* leaving *s*

3)To describe a FA,we use the transition graph or transition table

4) A DFA accepts an input string x if and only if there is some path in the transition graph from start state to some accepting state



E.g. Construct a DFA M, which can accept the strings which begin with a or b, or begin with c and contain at most one a.



So ,the DFA is $M = (\{0, 1, 2, 3, \}, \{a, b, c\}, move, 0, \{1, 2, 3\})$ move: move(0,a)=1 move(0,b)=1move(0,c)=1 move(1,a)=1move(1,b)=1 move(1,c)=1move(2,a)=3 move(2,b)=2move(2,c)=2 move(3,b)=3move(3,c)=3

- 4. Non-deterministic FA (NFA) NFA is a quintuple, $M(S,\Sigma,move,s_0,F)$
 - S: a set of states
 - $-\Sigma$: the input symbol alphabet
 - move: a mapping from $S \times \Sigma$ to S, move(s,a)= 2^{S} , $2^{S} \subseteq S$
 - s_0 : the start state, $s_0 \in S$
 - F: a set of states *F* distinguished as accepting states, F⊆S

4. Non-deterministic FA (NFA)

Note:1) In a NFA, the same character can label two or more transitions out of one state;

2) In a NFA, ε is a legal input symbol.

3) A DFA is a special case of a NFA

4) A NFA accepts an input string x if and only if there is some path in the transition graph from start state to some accepting state. A path can be represented by a sequence of state transitions called moves.

5)The language defined by a NFA is the set of input strings it accepts


e.g. An NFA M= $(\{q_0,q_1\},\{0,1\},move,q_0,\{q_1\})$



The language defined by the NFA is 0*10*|0*10*((1|0)0*10*)*



5. Conversion of an NFA into a DFA a)Reasons to conversion Avoiding ambiguity b)The algorithm idea Subset construction: The following state set of a state in a NFA is thought of as a following STATE of the state in the converted DFA

5. Conversion of an NFA into a DFA c)The pre-process-- ε -closure(T) Obtain ε -closure(T) T \subseteq S (1) ε -closure(T) definition A set of NFA states reachable from NFA state s in T on ε -transitions alone



5. Conversion of an NFA into a DFA c)The pre-process--- ϵ -closure(T) $(2)\varepsilon$ -closure(T) algorithm push all states in T onto stack; initialize ε -closure(T) to T; while stack is not empty do { pop the top element of the stack into t; for each state u with an edge from t to u labeled ε do if u is not in ε -closure(T) {

add u to ε-closure(T) push u into stack}} CHAPTER 3 LEXICAL ANALYSIS Section 4 Finite automata

- 5. Conversion of an NFA into a DFA d)Subset Construction algorithm
 - Input. An NFA N=(S,Σ ,move, S_0,Z)
 - Output. A DFA D= (Q, Σ , δ ,I₀,F), accepting the same language



5. Conversion of an NFA into a DFA d)Subset Construction algorithm $(1)I_0 = \varepsilon$ -closure $(S_0), I_0 \in Q$ (2)For each I_i , $I_i \in Q$, let $I_{t} = \varepsilon$ -closure(move(I_{i}, a)) if $I_{t} \notin Q$, then put I_{t} into Q (3)Repeat step (2), until there is no new state to put into Q (4)Let $F=\{I \mid I \in Q, \exists I \cap Z \iff \Phi\}$



| Ι | а | b |
|------------------------------|------------------------------|------------------------------|
| $I_0 = \{x, 5, 1\}$ | $I_1 = \{5, 3, 1\}$ | $I_2 = \{5, 4, 1\}$ |
| $I_1 = \{5, 3, 1\}$ | $I_3 = \{5, 3, 2, 1, 6, y\}$ | $I_2 = \{5, 4, 1\}$ |
| $I_2 = \{5, 4, 1\}$ | $I_1 = \{5, 3, 1\}$ | $I_4 = \{5, 4, 1, 2, 6, y\}$ |
| $I_3 = \{5, 3, 2, 1, 6, y\}$ | $I_3 = \{5, 3, 2, 1, 6, y\}$ | $I_5 = \{5, 1, 4, 6, y\}$ |
| $I_4 = \{5, 4, 1, 2, 6, y\}$ | $I_6 = \{5, 3, 1, 6, y\}$ | $I_4 = \{5, 4, 1, 2, 6, y\}$ |
| $I_5 = \{5, 1, 4, 6, y\}$ | $I_6 = \{5, 3, 1, 6, y\}$ | $I_4 = \{5, 4, 1, 2, 6, y\}$ |
| $I_6 = \{5, 3, 1, 6, y\}$ | $I_3 = \{5, 3, 2, 1, 6, y\}$ | $I_5 = \{5, 1, 4, 6, y\}$ |



DFA is



5. Conversion of an NFA into a DFA d)Subset Construction algorithm Notes:

1)Both DFA and NFA can recognize precisely the regular sets;

2)DFA can lead to faster recognizers3)DFA can be much bigger than an equivalent NFA

6. Minimizing the number of States of a DFAa)Basic idea

Find all groups of states that can be distinguished by some input string. At beginning of the process, we assume two distinguished groups of states: the group of non-accepting states and the group of accepting states. Then we use the method of partition of equivalent class on input string to partition the existed groups into smaller groups.

Minimizing the number of States of a DFA
 b)Algorithm

- Input. A DFA M={ S,Σ ,move, s_0,F }
- Output. A DFA M' accepting the same language as M and having as few states as possible.

Minimizing the number of States of a DFA b)Algorithm

(1)Construct an initial partition \prod of the set of states with two groups: the accepting states *F* and the non-accepting states *S*-*F*. $\prod_0 = \{I_0^1, I_0^2\}$

6. Minimizing the number of States of a DFA b)Algorithm

(2) For each group / of ∏_i, partition / into subgroups such that two states *s* and *t* of / are in the same subgroup if and only if for all input symbols *a*, states *s* and *t* have transitions on *a* to states in the same group of ∏_i; replace / in ∏_{i+1} by the set of subgroups formed.



6. Minimizing the number of States of a DFA b)Algorithm

- (3) If $\prod_{i+1} = \prod_i$, let $\prod_{final} = \prod_{i+1}$ and continue with step (4). Otherwise, repeat step (2) with \prod_{i+1}
- (4) Choose one state in each group of the partition \prod_{final} as the representative for that group. The representatives will be the states of the reduced DFA M'. Let *s* and *t* be representative states for *s*'s and *t*'s group respectively, and suppose on input *a* there is a transition of *M* from *s* to *t*. Then *M*' has a transition from *s* to *t* on *a*.

Minimizing the number of States of a DFA b)Algorithm

(5) If M' has a dead state(a state that is not accepting and that has transitions to itself on all input symbols), then remove it. Also remove any states not reachable from the start state.

Minimizing the number of States of a DFA b)Algorithm

Notes: The meaning that string *w* distinguishes state *s* from state *t* is that by starting with the DFA M in state *s* and feeding it input *w*, we end up in an accepting state, but starting in state t and feeding it input *w*, we end up in a nonaccepting state, or vice versa.

e.g. Minimize the following DFA.





1. Initialization: $\prod_0 = \{\{0,1,2\},\{3,4,5,6\}\}$

- 2.1 For Non-accepting states in \prod_0 :
 - a: move({0,2},a)={1}; move({1},a)={3}. 1,3 do
 not in the same subgroup of ∏₀.
 - So $\prod_1 = \{\{1\}, \{0,2\}, \{3,4,5,6\}\}$
 - b: move({0},b)={2}; move({2},b)={5}. 2,5 do not in the same subgroup of \prod_1 .
 - So, $\prod_1 = \{\{1\}, \{0\}, \{2\}, \{3,4,5,6\}\}$

2.2 For accepting states in \prod_0 :

- a: move({3,4,5,6},a)={3,6}, which is the subset of {3,4,5,6} in ∏₁"
- b: move({3,4,5,6},b)={4,5}, which is the subset of {3,4,5,6} in ∏₁"
- $-So, \prod_1 = \{\{1\}, \{0\}, \{2\}, \{3,4,5,6\}\}.$

3.Apply the step (2) again to \prod_1 , and get \prod_2 .

- $-\prod_2 = \{\{1\}, \{0\}, \{2\}, \{3, 4, 5, 6\}\} = \prod_1$,
- So, $\prod_{\text{final}} = \prod_{1}$
- 4. Let state 3 represent the state group {3,4,5,6}

So, the minimized DFA is :



1.The reasons about regular expression to a NFA

Strategy for building a recognizer from a regular expression is to construct an NFA from a regular expression and then to simulate the behavior of the NFA on an input string.

- 2. Construction of an NFA from a regular expression
 - a)Basic idea

Syntax-directed in that it uses the syntactic structure of the regular expression to guide the construction process.

- 2. Construction of an NFA from a regular expression
 - a)Algorithm
 - Input. A regular expression r over an alphabet Σ
 - Output. An NFA N accepting L(r)

- 2. Construction of an NFA from a regular expression
 - a)Algorithm
 - Method
 - (1) Parse *r* into its constituent sub-expressions.
 - (2) Use rules in the next pages to construct NFA's for each of the basic symbols in r(those that are either ϵ or an alphabet symbol).
 - (3)Use rules in the next and next page to combine these NFA's inductively, and obtain the NFA for the entire expression.



Rules



2. For a in Σ , --1 a (2)





FA to Regular expression

- 1. Basic ideas
 - Reduce the number of states by merging states
- 2. Algorithm
 - Input: An FA M
 - Output: A regular expression r over an alphabet Σ recognize the same language as FA M



FA to Regular expression

2. Algorithm

- Method:
 - Extend the concept of FA, let the arrows can be marked by regular expressions.
 - Add two nodes x,y to the FA M and get M' that recognize the same regular language.

$$\xrightarrow{x} \varepsilon FA \xrightarrow{\varepsilon} y$$

FA to Regular expression

- 2. Algorithm
 - Method:
 - Use the following rules to combine the regular expression in the FA's inductively, and obtain the entire expression for the FA



E.g. Construct the regular expression for the following DFA M.







Regular Grammar to an NFA

- 1. Basic properties
- n For each regular grammar $G=(V_N,V_T,P,S)$, there is an FA $M=(Q,\Sigma,f,q0,Z)$, and L(G)=L(M).
- n For each FA M, there is a right-linear grammar and a left-linear grammar recognize the same language. L(M)=L(G_R)=L(G_L)



Regular Grammar to an NFA

2. Right-linear grammar to FA

- -Input :G=(V_N,V_T,P,S)
- Output : FA M=(Q, Σ , move, q₀, Z)
- Method :
 - Consider each non-terminal symbol in G as a state, and add a new state T as an accepting state.
 - Let $Q=V_N\cup\{T\}$, $\Sigma = V_T$, $q_0 = S$; if there is the production $S \rightarrow \epsilon$, then $Z=\{S,T\}$, else $Z=\{T\}$;

Regular Grammar to an NFA

- 2. Right-linear grammar to FA
 - Method :
 - For each production, construct the function *move*.
 - a) For the productions similar as $A_1 \rightarrow aA_2$, construct move $(A_1,a) = A_2$.
 - b) For the productions similar as $A_1 \rightarrow a$, construct move $(A_1,a) = T$.
 - c) For each *a* in Σ , move(T,a)= Φ , that means the accepting states do not recognize any terminal symbol.

E.g. A regular grammar $G=({S,A,B},{a,b,c},P,S) P: S \rightarrow aS |aB$ $B\rightarrow bB|bA$ $A \rightarrow cA|c$ Construct a FA for the grammar G.


```
Answer: let M=(Q,\Sigma,f,q_0,Z)

1) Add a state T, So Q=\{S,B,A,T\}; \Sigma =\{a,b,c\};

q_0=S; Z=\{T\}.

2) f:

f(S,a)=S \quad f(S,a)=B

f(B,a)=B \quad f(B,b)=A

f(A,c)=A \quad f(A,c)=T
```



Regular Grammar to an NFA

3. FA to Right-linear grammar

- Input : $M=(S, \Sigma, f, s_0, Z)$
- Output : $Rg=(V_N, V_T, P, s_0)$
- Method :
 - If $s_0 \notin Z$, then the Productions are;
 - a) For the mapping $f(A_i,a)=A_j$ in M, there is a production $A_i \rightarrow aA_j$;
 - b) If $A_j \in Z$, then add a new production $A_i \rightarrow a_j$, then we get $A_i \rightarrow a | aA_j$;

Regular Grammar to an NFA

3. FA to Right-linear grammar

- Method :
 - If s₀∈Z, then we will get the following productions besides the productions we've gotten based on the former rule:
 - For the mapping $f(s_0, \varepsilon) = s_0$, construct new productions, $s_0' \rightarrow \varepsilon | s_0$, and s_0' is the new starting state.

e.g. construct a right-linear grammar for the following DFA M=({A,B,C,D},{0,1},f,A,{B})



Answer:Rg=({A,B,C,D}, {0,1},P,A) $A \rightarrow 0B \mid 1D \mid 0$ $B \rightarrow 1C \mid 0D$ $C \rightarrow 0B \mid 1D \mid 0$ $D \rightarrow 0D \mid 1D$ $L(Rg)=L(M)=0(10)^*$



- Lexical analyzer generator

 A software tool that automatically constructs a lexical analyzer from related language specification
- Typical lexical analyzer generator
 Lex

- 3. Lex
 - a) Lexical analyzer generating tool Lex compiler
 - b)Input specification
 - Lex language program

3. Lex

c) The process that creates a lexical analyzer with Lex



d) Lex specification
A Lex program consists of three parts: declaration
%%
translation rules
%%
auxiliary procedures

Design of a lexical analyzer generator 3. Lex d) Lex specification (1)Declaration Include declarations of variables, manifest constants and regular definitions Notes: A manifest constant is an identifier that is declared to represent a constant

d) Lex specification (1)Declaration %{ /*definitions of manifest constants LT,LE,EQ,GT,GE,IF,THEN,ELSE,ID*/ %} /*regular expression*/ delim [\t\n] {delim}+ WS letter [A-Za-z] digit [0-9] id {letter}({letter}|{digit})*



- 3. Lex
 - d) Lex specification
 (3)auxiliary procedures
 install_id() {

/* procedure to install the lexeme, whose first character is pointed to by yytext and whose length is yyleng, into the symbol table and return a pointer thereto*/

Notes: The auxiliary procedures can be compiled separately and loaded with the lexical analyzer.

```
%{ /* this part is copied literally to the generated C code */
#define IF 5
#define ID 12
#define INTEGER 13
#define REAL 14
%}
delim
              [ \†\n]+
letter
             [A-Za-z]
digit
              [0-91
             {letter}({letter}|{digit})*
id.
             {digit}+
integer
             {digit}+\.({digit}+)?|({digit}+)?\. {digit}+
real
%%
{delim}
             {/* no action and no return */}
             {return IF;}
if.
             {yylval = install_id(); return ID;}
{id}
             {yylval = convert_real(); return REAL:}
{real}
             {yylval = convert_int(); return INTEGER;}
{integer}
%%
install_id()
             { ... procedure to enter or lookup in the symbol table the string
             pointed to by yytext with length yyleng ... }
```

```
%{
/* a lex program that adds line numbers to lines of text,
printing the new text to the standard output */
#include <stdio.h>
int lineno = 1;
%}
line
        .*\n
%%
{line} {printf("%5d %s", lineno++, yytext); }
%%
main()
{ yylex(); return 0;}
```

