

**TSN: Lecture 23**  
**Introduction to**  
**Traffic Engineering**

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# Topics Covered

- Statistical Analysis
- Call Arrivals
- Objective of Traffic Engineering
- Blocking

# Basic Concept

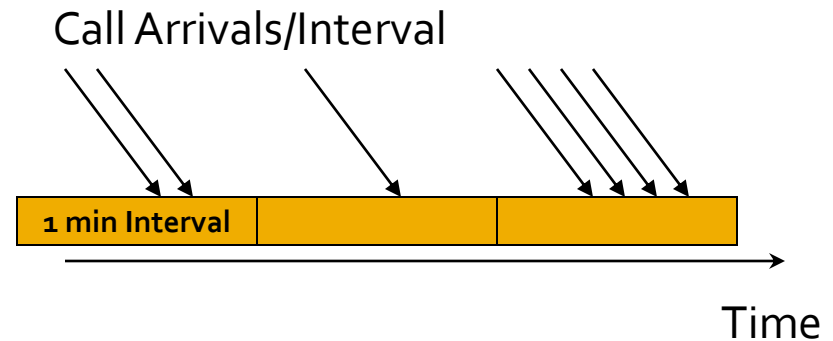
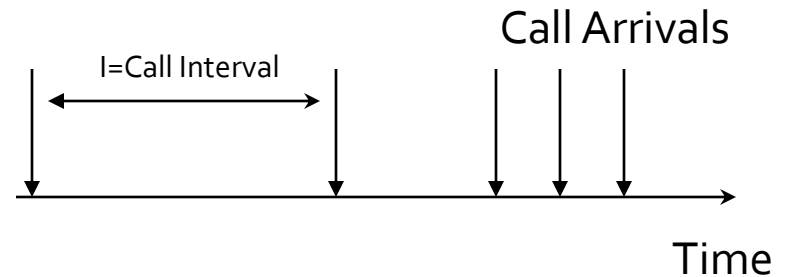
- **Performance analysis methods applied to telephony are usually referred to as traffic engineering**
- **Motivated by two factors**
  - **Unpredictable behavior of users**
    - **You never know when they call!**
  - **Users have to share resources**
    - **Users have to be happy!**

# Statistical Analysis

- We cannot exactly predict what users do!
- We can statistically tell what users may do!
- Looking at the traffic pattern we can see
  - Number of callers arrived in one hour = 20/hr
  - Average length of calls = 3 min/call
- Statistics on voice and data communications are very different
  - Data tends to be bursty
  - Voice is continuous with known average length

# Call Arrivals

- Calls arrive randomly!
  - But how?
- Looking at call arrivals
  - Average call interval ( $I=2\text{sec}/\text{call}$ )
  - Number of calls per unit interval ( $A=10\text{call}/\text{min}$ )
  - Note that  $I$  is inversely proportional to  $A$

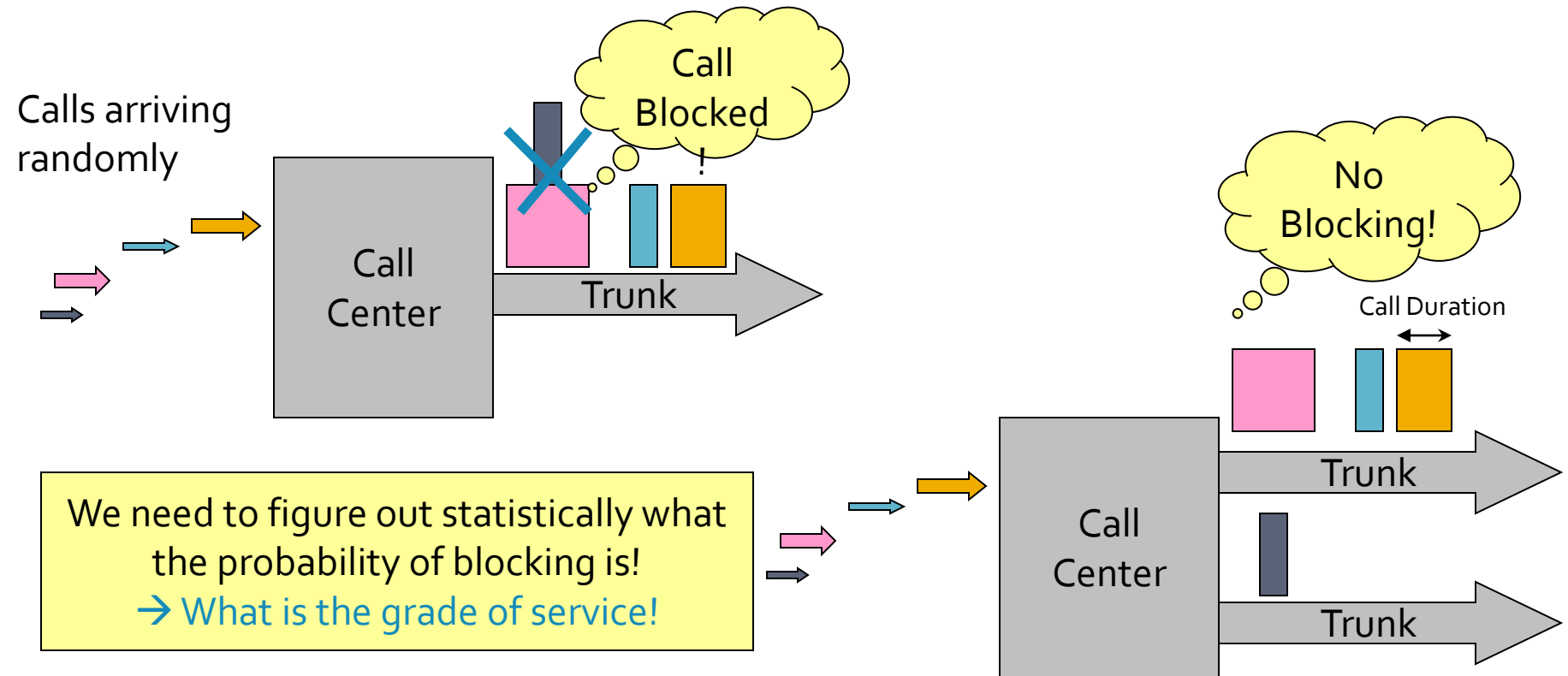


More Calls → Shorter time between successive calls

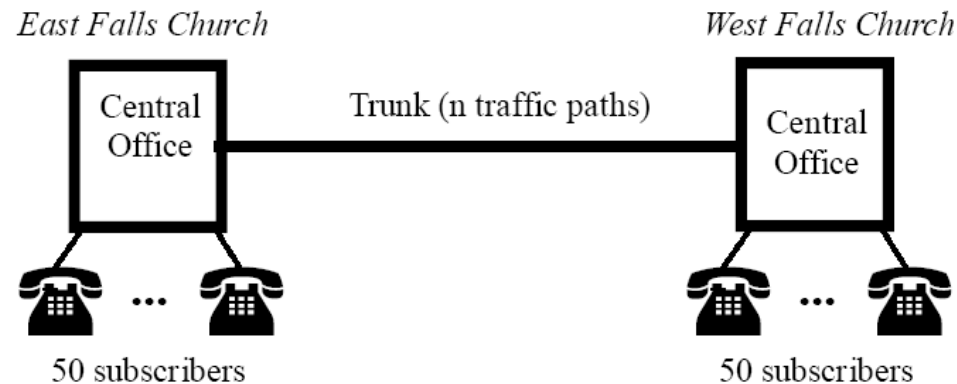
# Objective of Traffic Engineering

- **Given expected traffic (+ growth assumptions)...**
- **Provision resources (trunks, switches)...**
- **To minimize cost ...**
- **Subject to minimum acceptable quality of service requirements.**
  
- **Available tools:**
  - Mathematical tools
    - Equations and formulas / Statistical tools
  - Simulation tools
    - OPNE; OMNET; etc.

# What is Blocking?



# The challenge



- **Provisioning must be done by telephone companies**
- **In the example, consider connection between 2 COs**
  - **$n = 50$  channels ensures no blocking, but too costly**
  - **$n = 1$  channel good cost option, but subscribers will be unhappy (high blocking probability)**
  - **how do we determine the appropriate compromise?**

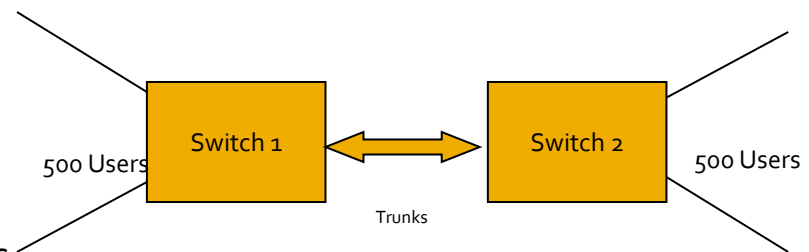


# Traffic Model Tool

- Calls arrive randomly
- All calls are independent
- Traffic models
  - Idea: telephone usage and sizing the network
  - Difference: What to do when blocking happens
  - Objective: calculate the Grade of Service (GOS)
    - If GOS is 0.01 (P.01) → 1 call will be blocked out of 100 attempted calls!
    - Defined formally as the number of lost calls over offered calls
- Two common models
  - Erlang C
    - Call arrival behavior follows a Poisson distribution
    - blocked calls may be retried at anytime
  - Erlang B Model
    - When a call is blocked it is cleared and will only be tried later
    - The load does not consider blocked calls

# Traffic Characteristics

- It is all about sharing effectively:
  - Telephone traffic is the aggregate of telephone calls over a group of circuits or trunks with regard of the number and duration of calls.
- Units:
  - Call arrival rate / hour (A)
  - Average service time or hold time (tm) / hour
    - Duration of the call
  - An *Erlang* (E) is a unit of telecommunications traffic measurement.
    - Strictly speaking, an Erlang represents the continuous use of one voice path.
    - In practice, it is used to describe the total traffic volume of one hour
    - Expresses the traffic intensity (dimensionless)
    - $E = A \times t_m$  (in Erlang)



# Traffic Characteristics

- Common units used in North America:
  - CS : calls-second per second
  - CCS : hundred (centrum) calls-second per hour
  - 1 Erlang =  $(60)(60)/100 = 36 \text{ CCS} = 3600 \text{ CS}$
- Capacity of a single channel is one Erlang
  - Interpretation: a telephone that is busy 10% of the time represents a load of 0.1 Erlang on that particular line
- **Example:** 1000 calls/hour each has an average length of 5 min:  $1000 \times (5/60) = 83.33 \text{ Erlang}$ ; note the total capacity is 100!
  - What is CS and CCS?

# Using Erlang B Formula

- **Assumptions:**

- Poisson arrivals (infinite # of sources)
- equal traffic density per source
- lost calls cleared

- **Probability of blockage at the switch due to congestion or “all trunks busy”:**

- E is the mean of the offered traffic [Erlangs], s is the number of trunks

$$P_{Blocking} = \frac{E^s}{s! + \sum_{k=0}^{s-1} \frac{E^k}{k!}}$$

# Using Erlang B Formula

**Example:** Suppose our expected traffic in the busy hour is 10 erlangs and we require blocking probability of 1 call in 200 (or better).

- What is the grade of service?
- How many trunks should we use?
- What is the efficiency of the system?

→  $1/200 = P_{0.005} = \text{GOS}$

→ 20 Trunks

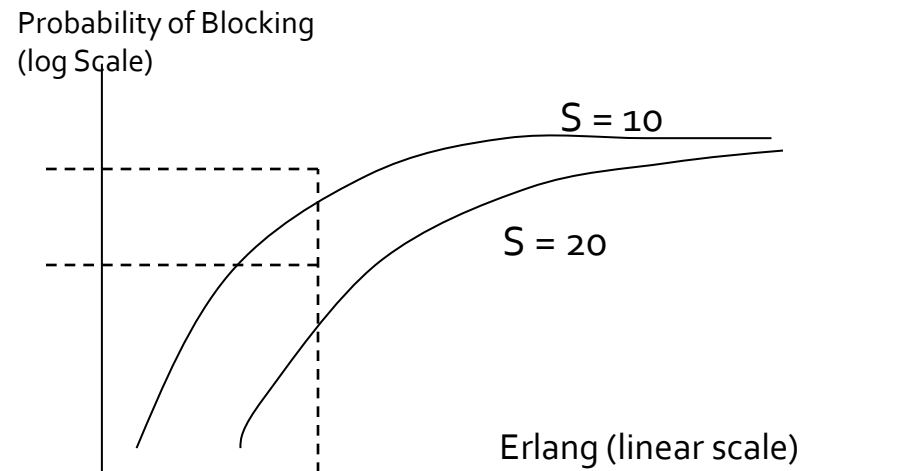
→ Efficiency =

$$\text{Erlang/Number of Trunks (x100)} = 10/20 \\ (\text{x100}) = 50\%$$

Trunks	P=0.001	P=0.005	P=0.01	P=0.05
1	.001	.005	.01	.05
5	.76	1.13	1.36	2.22
10	3.09	3.96	4.46	6.22
15	6.08	7.38	8.11	10.63
20	9.41	11.09	12.03	15.25
25	12.97	15	16.12	19.99

# Erlang B Behavior

- The Y axis is typically expressed in log scale
- $S$  is the number of trunks
- Blocking is between 0-1
- Note that eventually blocking will approach 1
- Larger  $S$  (more trunks result in lower blocking)
- As the load increases (higher Erlang) more blocking is expected
- Higher load can be due to longer hold time or more call arrivals



# References

- [http://www.cisco.com/univercd/cc/td/doc/cisintwk/intsolns/voipsol/ta\\_isd.htm](http://www.cisco.com/univercd/cc/td/doc/cisintwk/intsolns/voipsol/ta_isd.htm) on traffic analysis
- <http://www.tarrani.net/mike/docs/TrafficEngineering.pdf> good information on traffic engineering and statistical calculations
- Tools to calculate Erlang B
  - <http://personal.telefonica.terra.es/web/vr/erlang/eng/mcerlb.htm>
  - <http://www.erlang.com/calculator/erlb/> (this one may be simpler to use!)