## LECTURE 12

## Digital Logic Families




$$
\begin{aligned}
& A_{\text {next }}=A_{\text {present }} X+B_{\text {present }} X \\
& B_{\text {next }}=A_{\text {present }}^{\prime} X \\
& Y=\left(A_{\text {present }}+B_{\text {present }}\right) X^{\prime}
\end{aligned}
$$

## ImpaxtstEiqutationssf

 input and present stateOutput in terms of input and present state

| Present State |  | Input | Next State |  | Output |
| :--- | :--- | :--- | :--- | :---: | :---: |
| A | B | X | A | B | Y |
| 0 | 0 | 0 | 0 | 0 | StateoTable |
| 0 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 |
| 0 | 1 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 0 | 1 |
| 1 | 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 | 0 |



## Mealy and Moore Models

- Preceding Example: Output depends on present state and input. This is called the Mealy Model
- Another kind of circuit: Output only depends on present state. This is called the Moore Model


| $X$ | $Y$ | $A_{\text {present }}$ | $A_{\text {next }}$ |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 |




Flip-flops



- 1. Specification
- 2. Formulation: Draw a state diagram
- 3. Assign state number for each state
- 4. Draw state table
- 5. Derive input equations
- 5. One D flip-flop for each state bit


## How to Design a Sequential Circuit

- Design a sequential circuit to recognize the input sequence 1101.
- That is, output 1 if the sequence 1101 has been read, output 0 otherwise.


## Example



- 4 states, so we need 2 bits


| Present State |  | Input | Next State |  | Output |
| :--- | :--- | :--- | :--- | :---: | :---: |
| A | B | X | A | B | Y |
| 0 | 0 | 0 | 0 | Draw | StateoTable |
| 0 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 1 | 1 |
|  |  |  |  |  |  |

$$
\begin{aligned}
& A_{\text {next }}=A^{\prime} B X+A B^{\prime}
\end{aligned}
$$

$$
\begin{aligned}
& Y=A B X
\end{aligned}
$$



