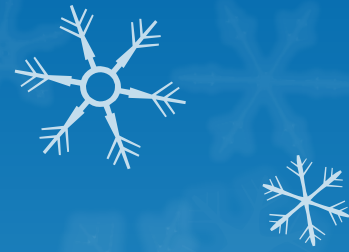


Course Name:
Database Management
Systems



Lecture 11

Topics to be covered

- ❑ Examples of Relational Algebra and Other Operations



Introduction

- This is a procedural query language which consists of set of operations that take one or two relations as input and produce a new relation as result.

Division of the Topic

- Set intersection operation
- Natural join
- Division operator
- Assignment operator
- Aggregate functions



Additional Operations

- Additional Operations
 - Set intersection
 - Natural join
 - Aggregation
 - Outer Join
 - Division
- All above, other than aggregation, can be expressed using basic operations we have seen earlier

Set-Intersection Operation – Example

- Relation r, s :

A	B
α	1
α	2
β	1

r

A	B
α	2
β	3

s

- $r \cap s$

A	B
α	2

Natural Join Operation – Example

- Relations r , s :

A	B	C	D
α	1	α	a
β	2	γ	a
γ	4	β	b
α	1	γ	a
δ	2	β	b

r

B	D	E
1	a	α
3	a	β
1	a	γ
2	b	δ
3	b	ϵ

s

$n \quad r \bowtie s$

A	B	C	D	E
α	1	α	a	α
α	1	α	a	γ
α	1	γ	a	α
α	1	γ	a	γ
δ	2	β	b	δ

Natural-Join Operation

n Notation $r \bowtie s$

- Let r and s be relations on schemas R and S respectively. Then, $r \bowtie s$ is a relation on schema $R \cup S$ obtained as follows:
 - Consider each pair of tuples t_r from r and t_s from s .
 - If t_r and t_s have the same value on each of the attributes in $R \cap S$, add a tuple t to the result, where
 - t has the same value as t_r on r
 - t has the same value as t_s on s

Example:

$R = (A, B, C, D)$

$S = (E, B, D)$

- Result schema = (A, B, C, D, E)
- $r \bowtie s$ is defined as:

$$\Pi_{r.A, r.B, r.C, r.D, s.E} (\sigma_{r.B = s.B \wedge r.D = s.D} (r \times s))$$

Bank Example Queries

- Find the largest account balance
 - Strategy:
 - Find those balances that are *not* the largest
 - Rename *account* relation as *d* so that we can compare each account balance with all others
 - Use set difference to find those account balances that were *not* found in the earlier step.
 - The query is:

$$\Pi_{balance}(account) - \Pi_{account.balance}(\sigma_{account.balance < d.balance} (account \times \rho_d(account)))$$

account

<i>account_number</i>
<i>branch_name</i>
<i>balance</i>

Aggregate Functions and Operations

- **Aggregation function** takes a collection of values and returns a single value as a result.

avg: average value
min: minimum value
max: maximum value
sum: sum of values
count: number of values

- **Aggregate operation** in relational algebra

$$G_1, G_2, \dots, G_n \mathcal{G}_{F_1(A_1), F_2(A_2), \dots, F_n(A_n)}(E)$$

E is any relational-algebra expression

- G_1, G_2, \dots, G_n is a list of attributes on which to group (can be empty)
- Each F_i is an aggregate function
- Each A_i is an attribute name

Aggregate Operation – Example

- Relation r :

A	B	C
α	α	7
α	β	7
β	β	3
β	β	10

- $g_{\text{sum}(c)}(r)$

$\text{sum}(c)$
27

- Question: Which aggregate operations cannot be expressed using basic relational operations?

Aggregate Operation – Example

- Relation *account* grouped by *branch-name*:

<i>branch_name</i>	<i>account_number</i>	<i>balance</i>
Perryridge	A-102	400
Perryridge	A-201	900
Brighton	A-217	750
Brighton	A-215	750
Redwood	A-222	700

branch_name \mathcal{G} **sum**(*balance*) (*account*)

<i>branch_name</i>	sum (<i>balance</i>)
Perryridge	1300
Brighton	1500
Redwood	700

Aggregate Functions (Cont.)

- Result of aggregation does not have a name
 - Can use rename operation to give it a name
 - For convenience, we permit renaming as part of aggregate operation

branch_name ***g*** ***sum***(*balance*) ***as*** *sum_balance*
(*account*)

Outer Join

- An extension of the join operation that avoids loss of information.
- Computes the join and then adds tuples from one relation that does not match tuples in the other relation to the result of the join.
- Uses *null* values:
 - *null* signifies that the value is unknown or does not exist
 - All comparisons involving *null* are (roughly speaking) **false** by definition.
 - We shall study precise meaning of comparisons with nulls later

Outer Join – Example

- Relation *loan*

<i>loan_number</i>	<i>branch_name</i>	<i>amount</i>
L-170	Downtown	3000
L-230	Redwood	4000
L-260	Perryridge	1700

- n Relation *borrower*

<i>customer_name</i>	<i>loan_number</i>
Jones	L-170
Smith	L-230
Hayes	L-155

Outer Join – Example

- Join

loan ⋈ *borrower*

<i>loan_number</i>	<i>branch_name</i>	<i>amount</i>	<i>customer_name</i>
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith

n Left Outer Join

loan ⋈_n *borrower*

<i>loan_number</i>	<i>branch_name</i>	<i>amount</i>	<i>customer_name</i>
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith
L-260	Perryridge	1700	<i>null</i>

Outer Join – Example

n Right Outer Join

$loan \bowtie_{\text{R}} borrower$

<i>loan_number</i>	<i>branch_name</i>	<i>amount</i>	<i>customer_name</i>
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith
L-155	<i>null</i>	<i>null</i>	Hayes

n Full Outer Join

$loan \bowtie_{\text{F}} borrower$

<i>loan_number</i>	<i>branch_name</i>	<i>amount</i>	<i>customer_name</i>
L-170	Downtown	3000	Jones
L-230	Redwood	4000	Smith
L-260	Perryridge	1700	<i>null</i>
L-155	<i>null</i>	<i>null</i>	Hayes

n **Question:** can outerjoins be expressed using basic relational

algebra operations

Null Values

- It is possible for tuples to have a null value, denoted by *null*, for some of their attributes
- *null* signifies an unknown value or that a value does not exist.
- The result of any arithmetic expression involving *null* is *null*.
- Aggregate functions simply ignore null values (as in SQL)
- For duplicate elimination and grouping, null is treated like any other value, and two nulls are assumed to be the same (as in SQL)



Null Values

- Comparisons with null values return the special truth value: *unknown*
 - If *false* was used instead of *unknown*, then $not (A < 5)$ would not be equivalent to $A \geq 5$
- Three-valued logic using the truth value *unknown*:
 - OR: $(unknown \text{ or } true) = true,$
 $(unknown \text{ or } false) = unknown$
 $(unknown \text{ or } unknown) = unknown$
 - AND: $(true \text{ and } unknown) = unknown,$
 $(false \text{ and } unknown) = false,$
 $(unknown \text{ and } unknown) = unknown$
 - NOT: $(not \text{ unknown}) = unknown$
 - In SQL "*P is unknown*" evaluates to true if predicate *P* evaluates to *unknown*
- Result of select predicate is treated as *false* if it evaluates to *unknown*

Division Operation

- Notation: $r \div s$
- Suited to queries that include the phrase “for all”.
- Let r and s be relations on schemas R and S respectively where
 - $R = (A_1, \dots, A_m, B_1, \dots, B_n)$
 - $S = (B_1, \dots, B_n)$

The result of $r \div s$ is a relation on schema

$$R - S = (A_1, \dots, A_m)$$

$$r \div s = \{ t \mid t \in \Pi_{R-S}(r) \wedge \forall u \in s (tu \in r) \}$$

Where tu means the concatenation of tuples t and u to produce a single tuple