LECTURE 11

Introductory Lecture on Section C -Semiconductors

Topics to be covered

• Continuity Equation

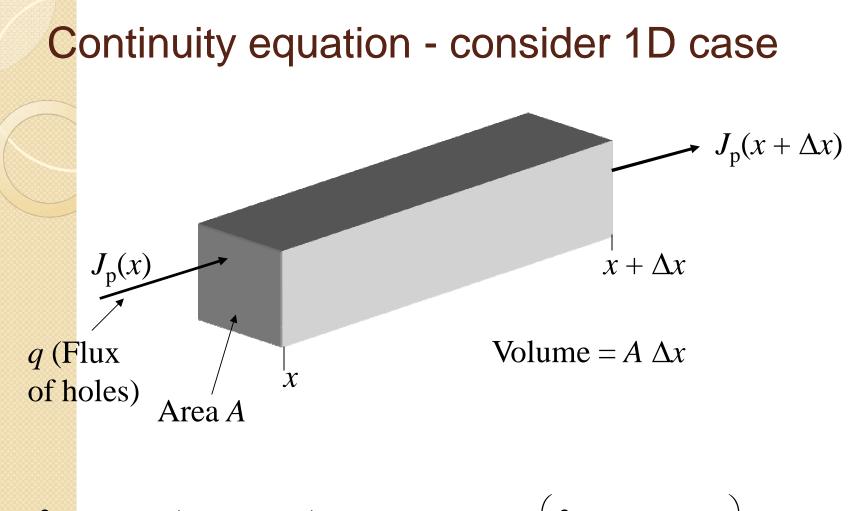
Continuity equation

• The continuity equation satisfies the condition that particles should be conserved! Electrons and holes cannot mysteriously appear or disappear at a given point, but must be transported to or created at the given point via some type of carrier action.

Inside a given volume of a semiconductor,

$$\frac{\partial p}{\partial t} = \frac{\partial p}{\partial t}|_{\text{drift}} + \frac{\partial p}{\partial t}|_{\text{diffusion}} + \frac{\partial p}{\partial t}|_{\text{thermal}} + \frac{\partial p}{\partial t}|_{\text{others}}$$

There is a corresponding equation for electrons.



$$\frac{\partial p}{\partial t}A\Delta x = \frac{A}{q}J_{p}(x) - \frac{A}{q}J_{p}(x+\Delta x) + A\Delta x \left(\frac{\partial p}{\partial t}/_{\text{thermal R-G}}\right)$$
$$= \frac{A}{q}J_{p}(x) - \frac{A}{q}\left[J_{p}(x) + \frac{\partial J_{p}(x)}{\partial x}\Delta x\right] + A\Delta x \left(\frac{\partial p}{\partial t}|_{\text{thermal R-G}}\right)_{4}$$

$$\frac{\partial p}{\partial t} A\Delta x = -\frac{A}{q} \frac{\partial J}{\partial x} \Delta x + A\Delta x \left(\frac{\partial p}{\partial t}/_{\text{thermal } R-G,}\right)$$
light etc.

$$\frac{\partial p}{\partial t} = -\frac{1}{q} \frac{\partial J}{\partial x} + \frac{\partial p}{\partial t}/_{\text{thermal } R-G,}$$
light etc.

$$\frac{\partial p}{\partial t} = -\frac{1}{q} \frac{\partial J}{\partial x} + \frac{\partial p}{\partial t}/_{\text{thermal } + \frac{\partial p}{\partial t}}/_{\text{others } R-G}$$
light...

$$\frac{\partial n}{\partial t} = \frac{1}{q} \frac{\partial J}{\partial x} + \frac{\partial n}{\partial t}/_{\text{thermal } + \frac{\partial n}{\partial t}}/_{\text{others } R-G}$$
Continuity eqn. for holes

$$\frac{\partial n}{\partial t} = \frac{1}{q} \frac{\partial J}{\partial x} + \frac{\partial n}{\partial t}/_{\text{thermal } + \frac{\partial n}{\partial t}}/_{\text{others } R-G}$$
Continuity eqn. for electrons
R-G
Light...

These are general equations for one dimension, indicating that particles are conserved.

Minority carrier diffusion

Apply **Octomations** at the following assumptions:

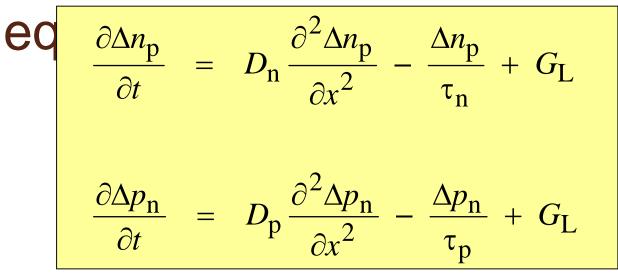
- Electric field E = 0 at the region of analysis
- Equilibrium minority carrier concentrations are not functions of position, i.e., $n_0 \neq n_0(x)$; $p_0 \neq p_0(x)$
- Low-level injection
- The dominant R-G mechanism is thermal R-G process
- The only external generation process is photo generation

Minority carrier diffusion Conside Conside Conside Conside Conside Conside Conside Constants (Constants) and make the following simplifications:

$$J_{n} = q\mu_{n}nE + qD_{n}\frac{\partial n}{\partial x} \approx qD_{n}\frac{\partial n}{\partial x}$$
$$\frac{\partial n}{\partial x} = \frac{\partial}{\partial x}(n_{0} + \Delta n) = \frac{\partial\Delta n}{\partial x}$$
$$\frac{\partial n}{\partial t}/_{\text{thermal }R-G} = -\frac{\Delta n}{\tau_{n}} \text{ and } \frac{\partial n}{\partial t}/_{\text{tight etc.}} = G_{L}$$
$$\frac{\partial n}{\partial t} = \frac{\partial}{\partial t}(n_{0} + \Delta n) = \frac{\partial\Delta n}{\partial t}$$

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Minority carrier diffusion



The subscripts refer to type of materials, either n-type or p-type.

Why are these called "diffusion equations"? Why are these called "minority carrier" diffusion equations?

Example 1

Consider an n-type Si uniformly illuminated such that the excess carrier generation rate is G_L e-h pairs / (s cm³). Use MCDE to predict how excess carriers decay after the light is turned-off.

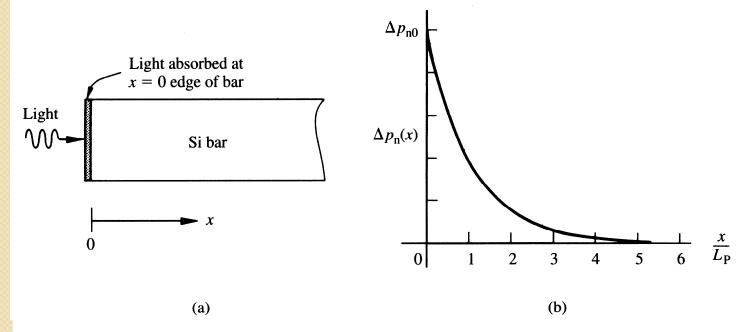
<u>t < 0</u>: uniform $\rightarrow d/dx$ is zero; steady state $\rightarrow d/dt = 0$ So, applying to holes, $\Delta p(t < 0) = G_L \tau_P$

<u>t > 0</u>: $G_L = 0$; uniform $\rightarrow d/dx = 0$;

$$\frac{\partial \Delta p_{\rm n}}{\partial t} = -\frac{\Delta p_{\rm n}}{\tau_{\rm p}} \quad \text{so,} \quad \Delta p_{\rm n} = \Delta p_{\rm n}(0) \exp\left(-t/\tau\right)$$
$$\Delta p(t>0) = G_{\rm L}\tau_{\rm P} \exp\left(-\frac{t}{\tau_{\rm p}}\right) \quad \text{since} \quad \Delta p(0) = G_{\rm L}\tau_{\rm p}$$

Example 2

Consider a uniformly doped Si with $N_{\rm D}=10^{15}$ cm⁻³ is illuminated such that $\Delta p_{\rm n0}=10^{10}$ cm⁻³ at x=0. No light penetrates inside Si. Determine $\Delta p_{\rm n}(x)$. (see page 129 in text)



Solution is:

$$\Delta p_{\rm n}(x) = \Delta p_{\rm n0} \exp\left(-\frac{x}{L_{\rm p}}\right)$$
 where $L_{\rm p} = \sqrt{D_{\rm p}\tau_{\rm p}}$

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Minority carrier diffusion Length In the previous example, the exponential falloff in the excess carrier concentration is characterized by a decay length L which appears

concentration is characterized by a decay length, L_p , which appears often in semiconductor analysis.

 $L_{\rm p} = (D_{\rm p} \tau_{\rm p})^{1/2}$ associated with minority carrier holes in n-type materials

 $L_{\rm n} = (D_{\rm n} \tau_{\rm n})^{1/2}$ associated with minority carrier electrons in ptype materials

Physically L_n and L_p represent the average distance minority carriers can diffuse into a sea of majority carriers before being annihilated. What are typical values for L_p and L_n ?