

Structural Analysis-I

Unit-1

Introduction to structural Analysis

- **Structural analysis** is the determination of the effects of [loads](#) on physical [structures](#) and their [components](#). Structures subject to this type of analysis include all that must withstand loads
- Structural Analysis can be briefly described as the study of the behaviour of structures using the knowledge of mechanics. Such a description needs some understanding of the terms “structure” and “mechanics”. Structures include a wide variety of systems, such as buildings, bridges, dams, aircrafts, etc., that are built to serve some specific human needs (for example, habitation, transportation, storage, etc.).
- Structural analysis incorporates the fields of [applied mechanics](#), [materials science](#) and [applied mathematics](#) to compute a structure's [deformations](#), internal [forces](#), [stresses](#), support reactions, accelerations, and [stability](#).

Properties of Materials: Elasticity and Plasticity

- **Elasticity:** It is the property of a material by virtue of which it regains its original shape and size after removal of external load applied on it.
- **Plasticity:** It is the property of a material by virtue of which it deforms permanently (doesn't regain its original shape and size) after removal of external load applied on it.

Properties of Materials: Ductility, Malleability and Brittleness

- **Ductility** is a solid material's ability to deform under [tensile](#) stress; this is often characterized by the material's ability to be stretched into a wire.
- **Malleability**, a similar property, is a material's ability to deform under [compressive](#) stress; this is often characterized by the material's ability to form a thin sheet by hammering or rolling.
- Both of these mechanical properties are aspects of [plasticity](#), the extent to which a solid material can be plastically deformed without [fracture](#).
- A [material](#) is **brittle** if, when subjected to [stress](#), it breaks without significant deformation ([strain](#)). Brittle materials absorb relatively little [energy](#) prior to fracture, even those of high [strength](#).

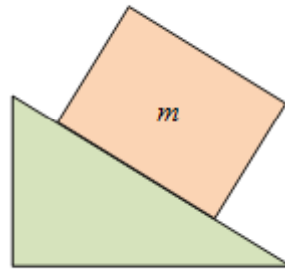
Properties of Materials: Toughness and Strength

- **Toughness** is the ability of a material to absorb energy and plastically deform without fracturing. Also it is defined sometimes as the amount of [energy](#) per volume that a material can absorb before [rupturing](#). It is also defined as the resistance to [fracture](#) of a material when [stressed](#).
- **Strength** is ability of the material to resist deformation under load.

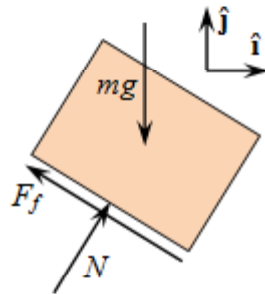
Basics of Engineering Mechanics

- **Free body diagram:** A **free body diagram**, sometimes called a force diagram, is a pictorial device, often a working sketch, used by engineers to analyze the forces and moments acting on a body.

A block on a ramp

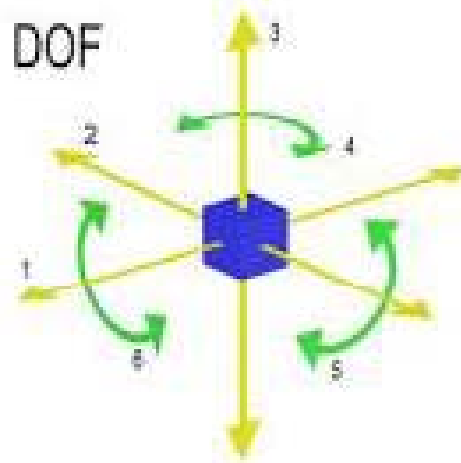


Free body diagram
of just the block



Basics of Engineering Mechanics

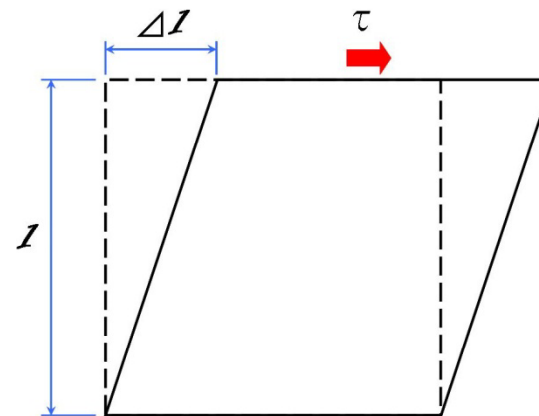
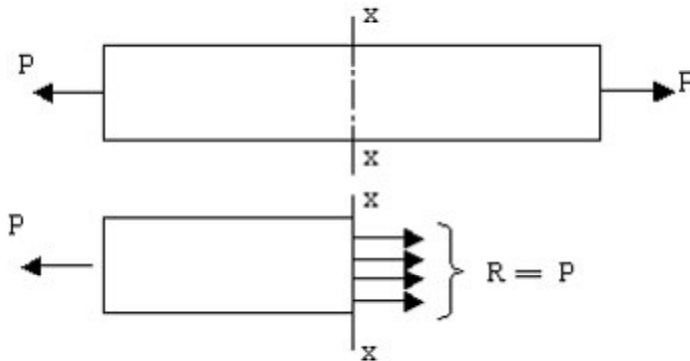
- **Degree of freedom:** Degrees of freedom of a system is the number of parameters of the system that may vary independently. For example, the position of a figure in the plane has three degrees of freedom.



Stresses

Stress may be defined as normal component of force per unit area $p = (P/A)$.

- Unit of stress N/m²
- There are following king of stresses:
 - Normal Stresses
 - Tensile stress
 - Compressive stress
 - Shear stress or tangential stress
 - Bending stress
 - Torsional stress
 - Bearing stress



Strain

- It may defined as change in length per unit length of any object on which loads are acting.

$$e = \Delta L / L$$

Unit of strain: Unitless

Hooke's Law:

- Hooke's law states that within elastic limits, stress is directly proportional to strain:

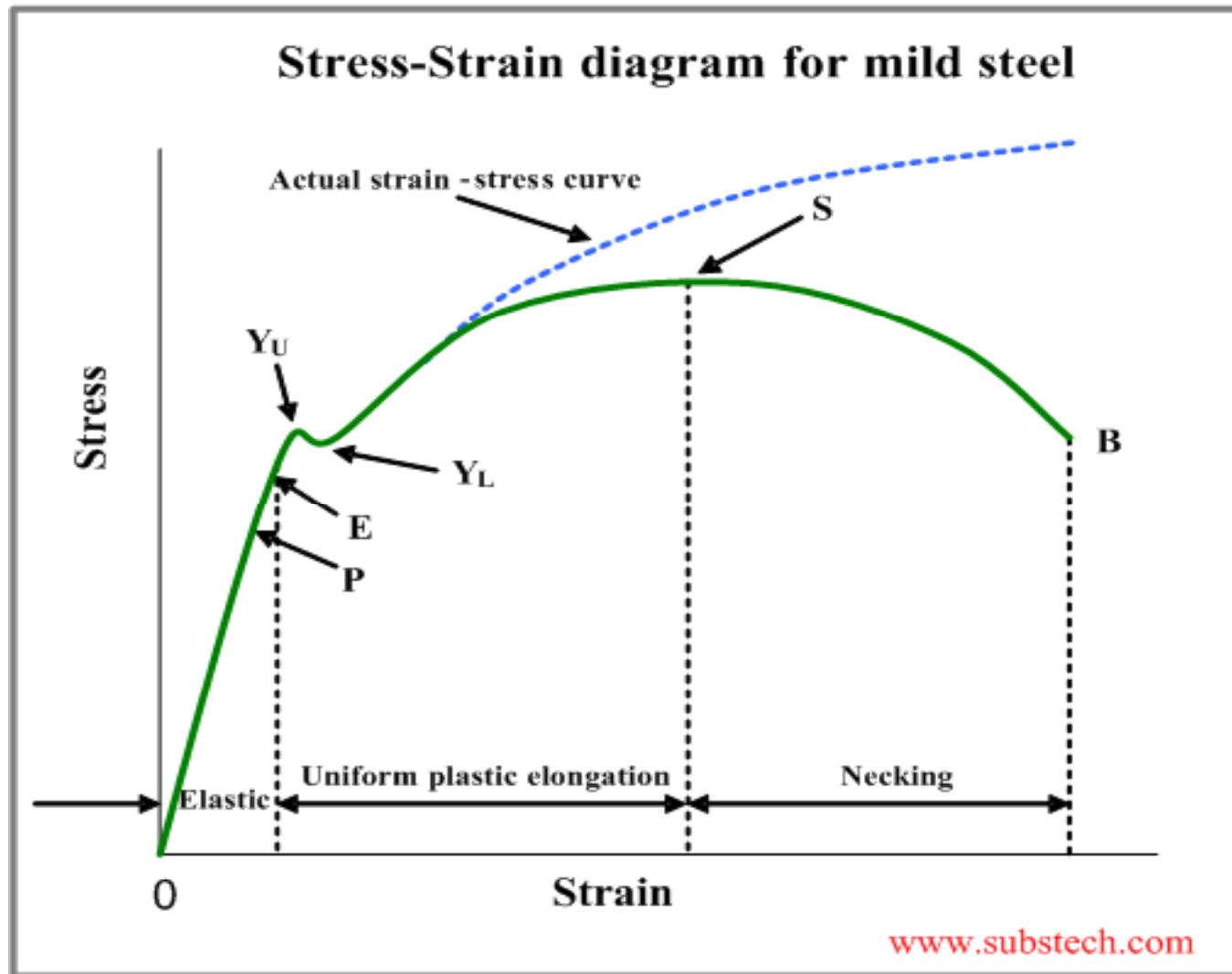
$$p \propto e$$

or $p = E e$

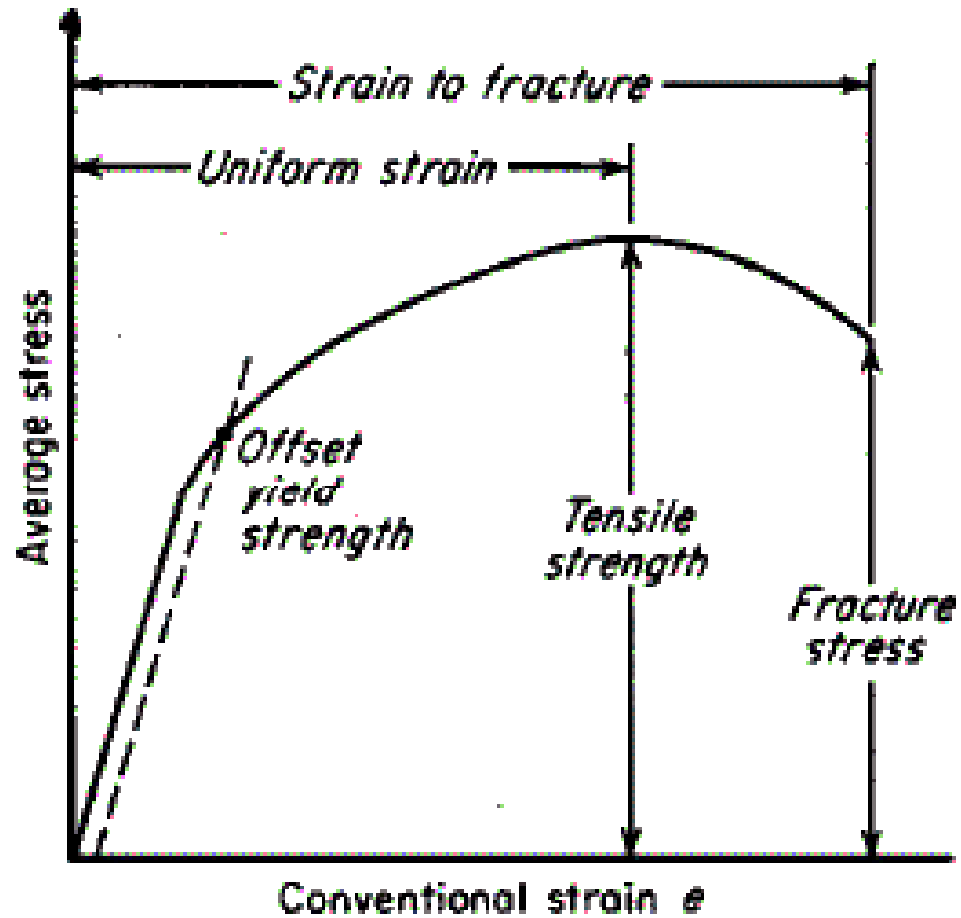
$p = (P/A)$ and $e = \Delta L/L$

Hence $\Delta L = (PL)/(AE)$

Stress strain diagram (Ductile Material):



Typical stress-strain curve for brittle materials:



Composite Sections:

- Sections in parallel:
- Sections in series: